

Coherent oscillations in a Single Cooper-pair Box

1. Introduction

2. Coulomb Staircase

3. Spectroscopy

4. Coherent oscillations

CHALMERS:

Experiment:

Tim Duty

David Gunarsson

Kevin Bladh

Theory:

G. Johansson => Karlsruhe

A. Käck

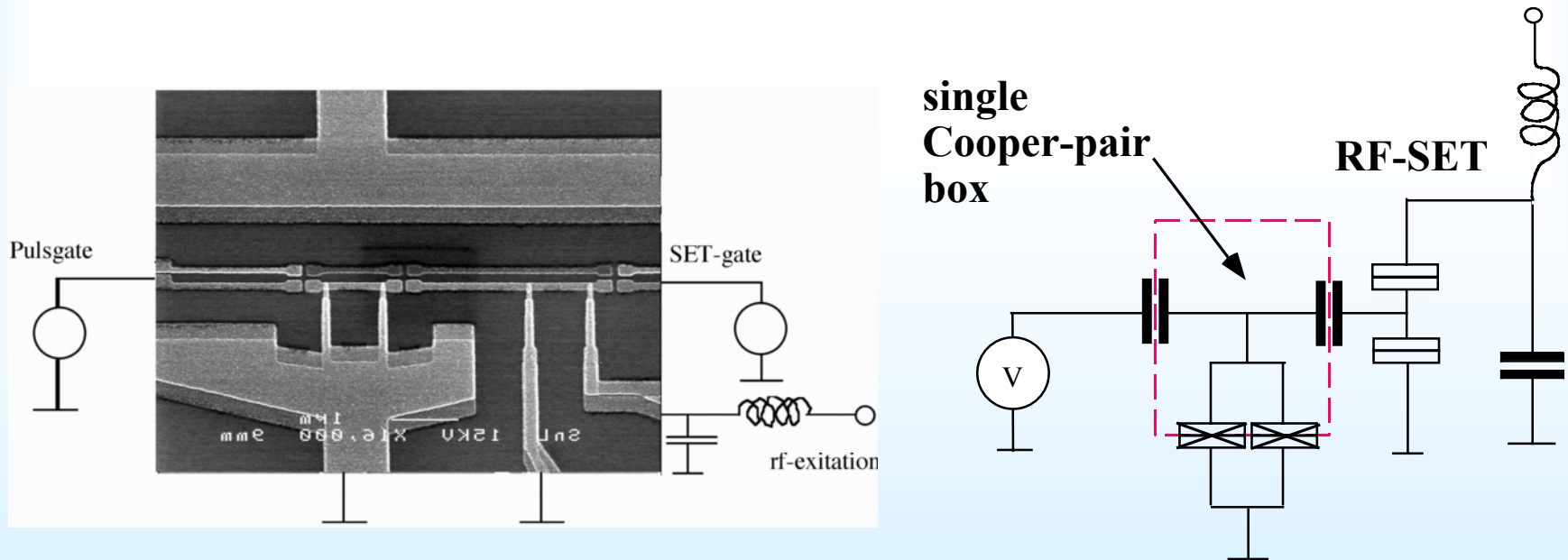
G. Wendin

YALE:

Rob Schoelkopf

Konrad Lehnert => Bolder

A Single Cooper-pair Box Qubit Integrated with an RF-SET Read-out system

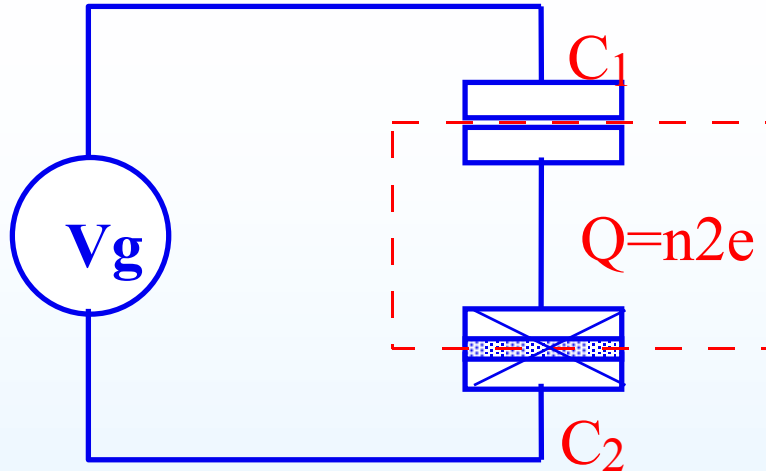


$$\Delta \gg E_C \gg E_J(B) \gg T$$

2.5K 1K 0.5-0.05K 20mK

Bouchiat et al. Physica Scripta (99)
Makhlin et al. Rev. Mod. Phys. (01)
Aassime, PD et al., PRL (01)

The Single Cooper-pair box (SCB)



$$H = \frac{Q^2}{2C_\Sigma} - E_J \cos \theta$$

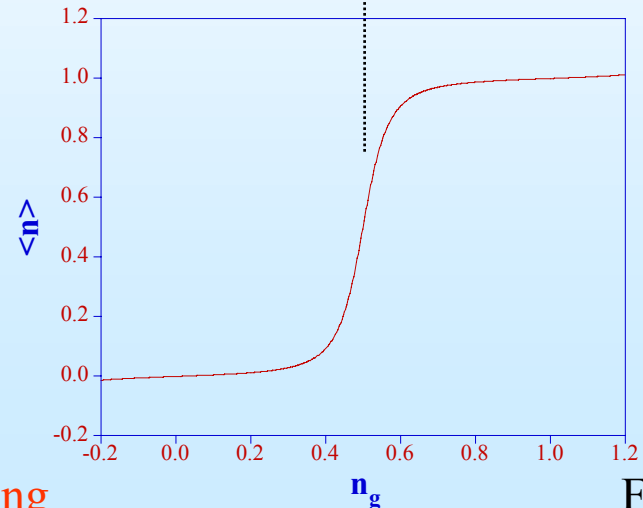
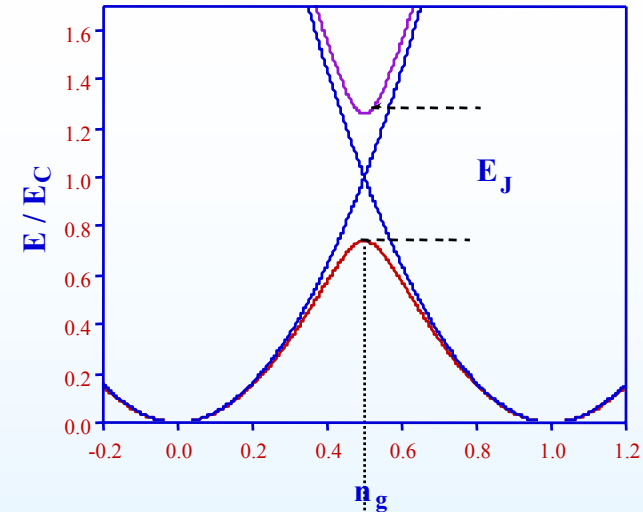
c.f. Hamiltonian for Bloch electrons

$$\frac{p^2}{2m} + U(x)$$

Bouchiat et al., Physica Scripta (98)

Nakamura et al., Nature (99)

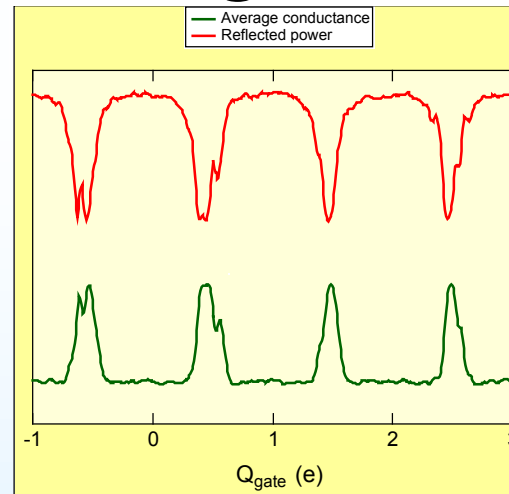
Makhlin et al., Nature (00)



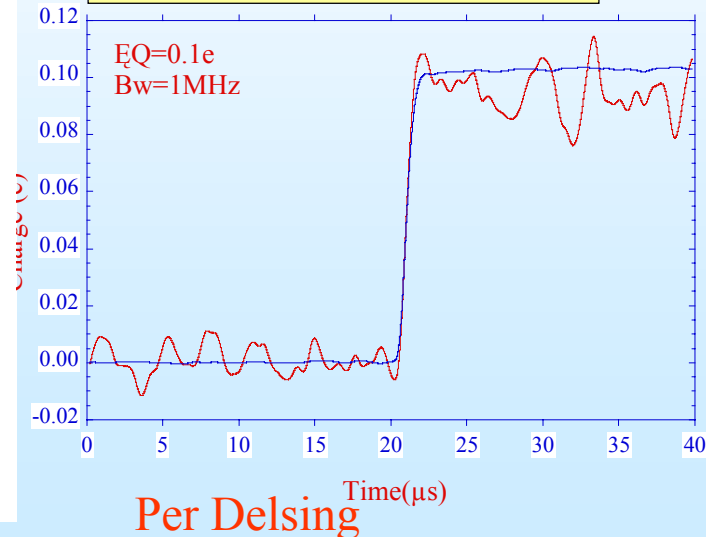
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Fig. 3

The Radio-Frequency Single Electron Transistor



Very high speed:
137 MHz
R.Schoelkopf, PD et al.
Science (98)



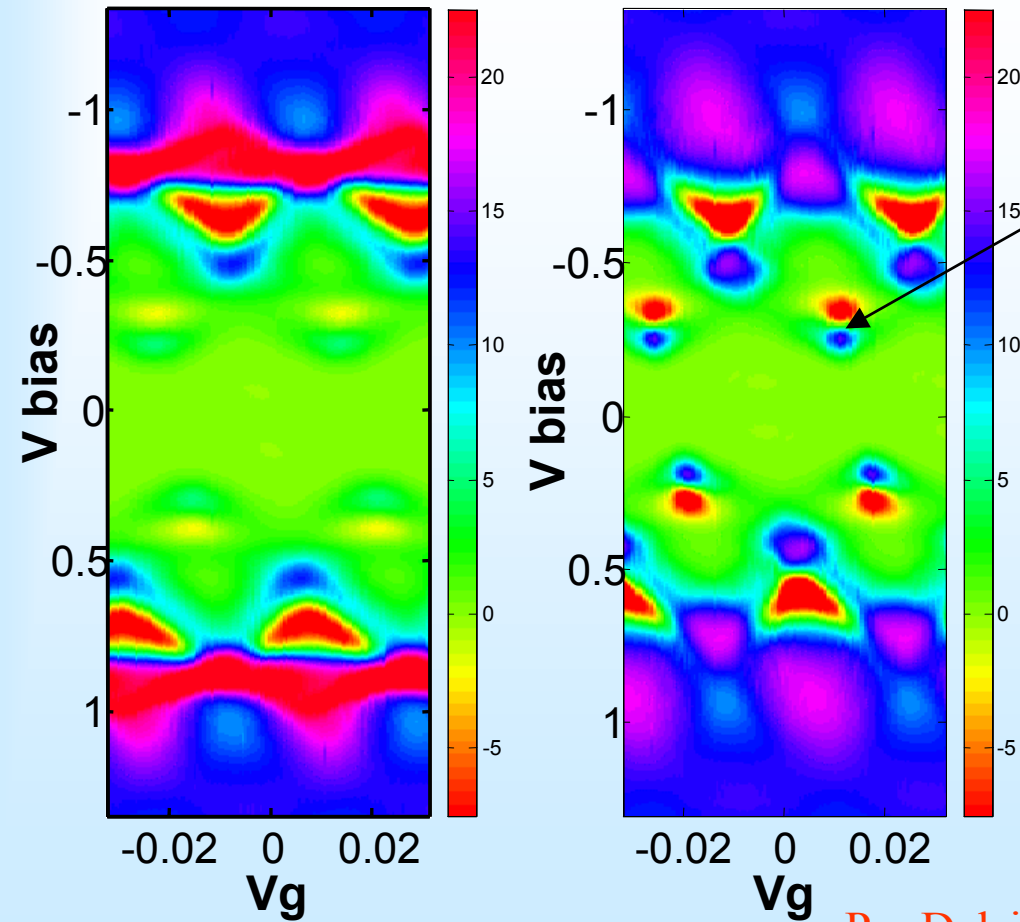
Very high sensitivity:
 $3.2 \mu\text{e}/\sqrt{\text{Hz}}$
A.Aassime, PD et al.
APL (01)

Fig. 4

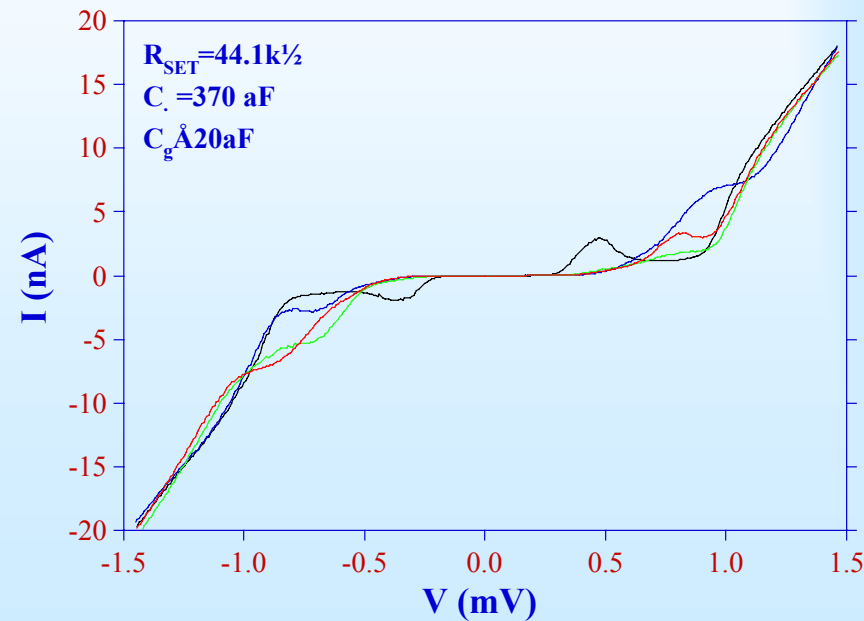
SET IV-characteristics and Conductance vs. V_b and V_g

B=0.0 T

B=0.4 T



Operation point
double JQP



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Fig. 5

The Sample holder

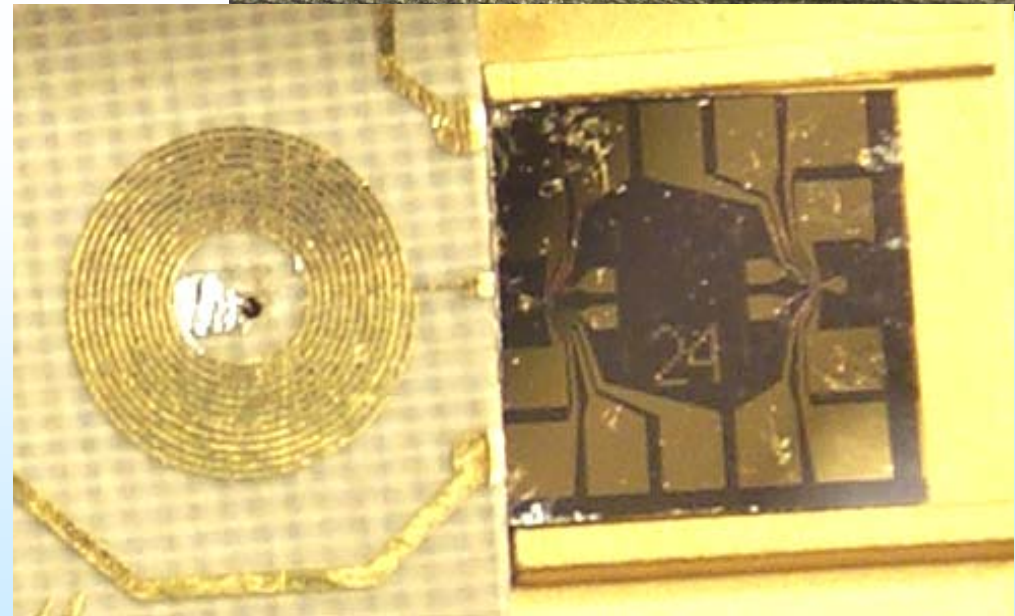
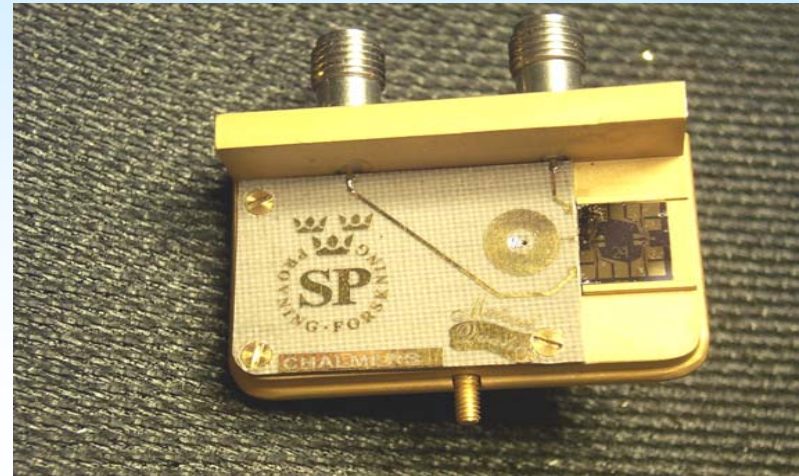
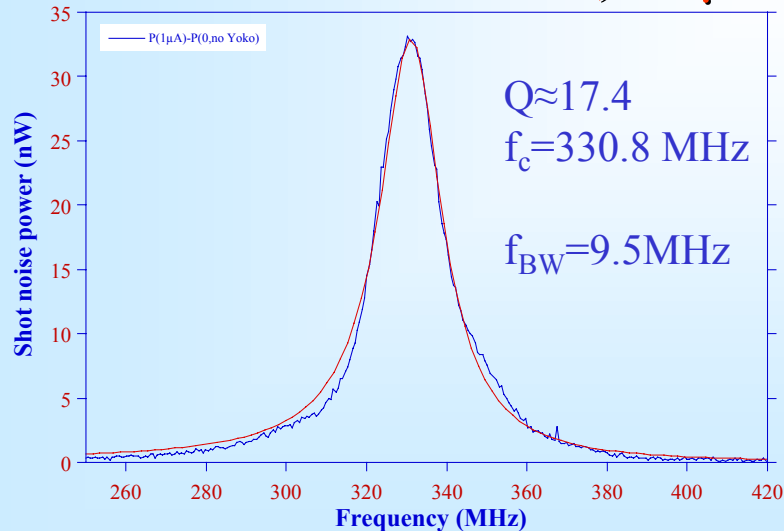
Fabricated in oxygen free high conductivity copper and gold plated

Inductance can be changed by changing the distance to the ground plane with a tuning screw

Inductor can be made Superconducting to minimize losses

Tank circuit : $L \approx 400\text{nH}$, $C_{\text{pad}} \approx 300\text{fF}$

Shot noise from the SET, $I=1\mu\text{A}$



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Fig. 6

Improving sensitivity by adding a SQUID amplifier

Cold HEMT amplifiers has $T_N \approx 2.5$ K

SQUID amplifier has $T_N \approx 50$ mK

Collaboration with Berkeley

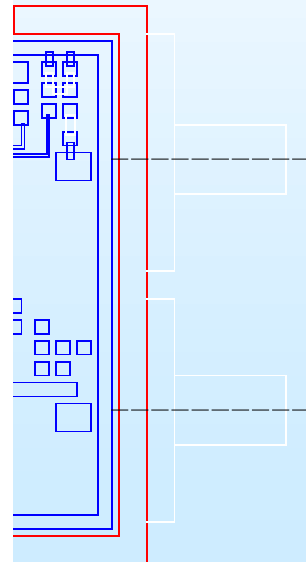
M. Mück, J.B. Kycia, and J. Clarke

Appl. Phys. Lett., 78, 967 (2001)

A transmission RF-SET would then be better

T. Fujisawa and Y. Hirayama

Appl. Phys. Lett., 77, 543 (2000)



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Qubit measurements

Circuit parameters

$$R_{\text{SET}} \approx 45 \text{ k}\Omega$$

$$E_{\text{CSET}} \approx 1.51 \text{ K}$$

$$E_{\text{CBOX}} \approx 1.65 \text{ K}$$

$$E_{\text{J}} \approx 0.6 \text{ K}$$

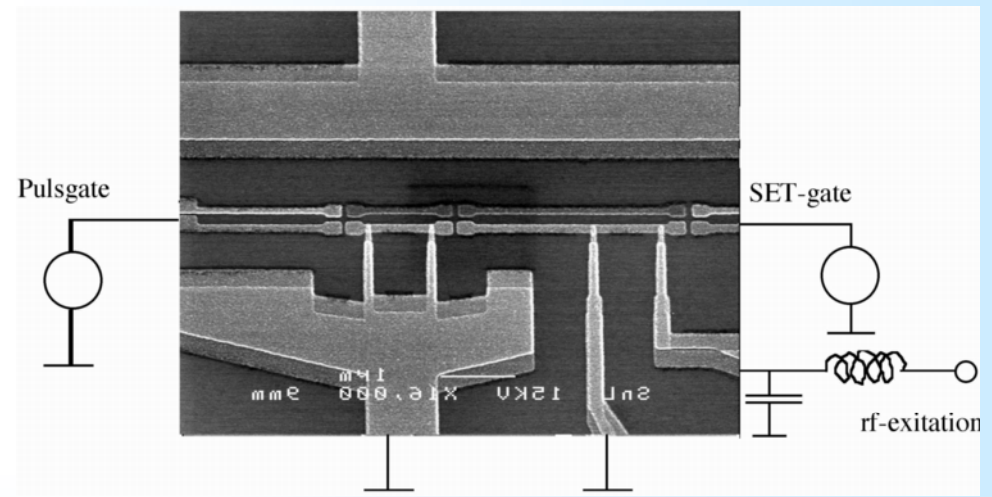
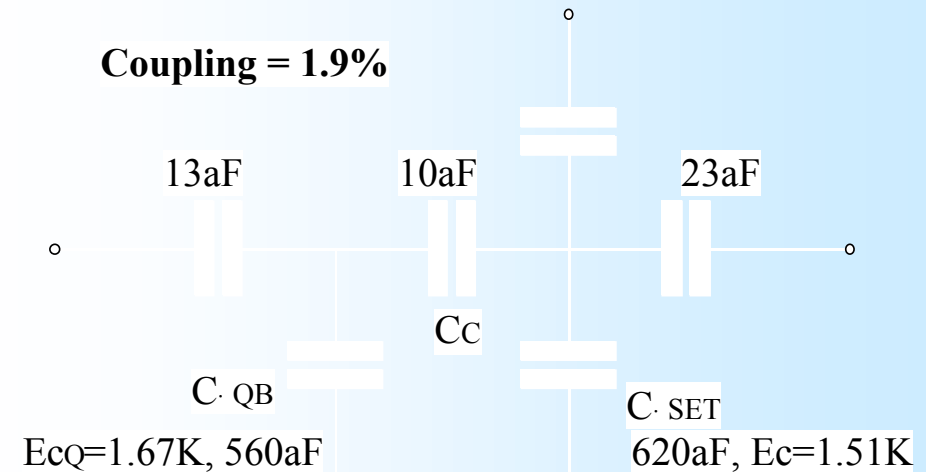
$$\text{Box to SET coupling} = 1.9\%$$

$$\text{B-field parallel to substrate}$$

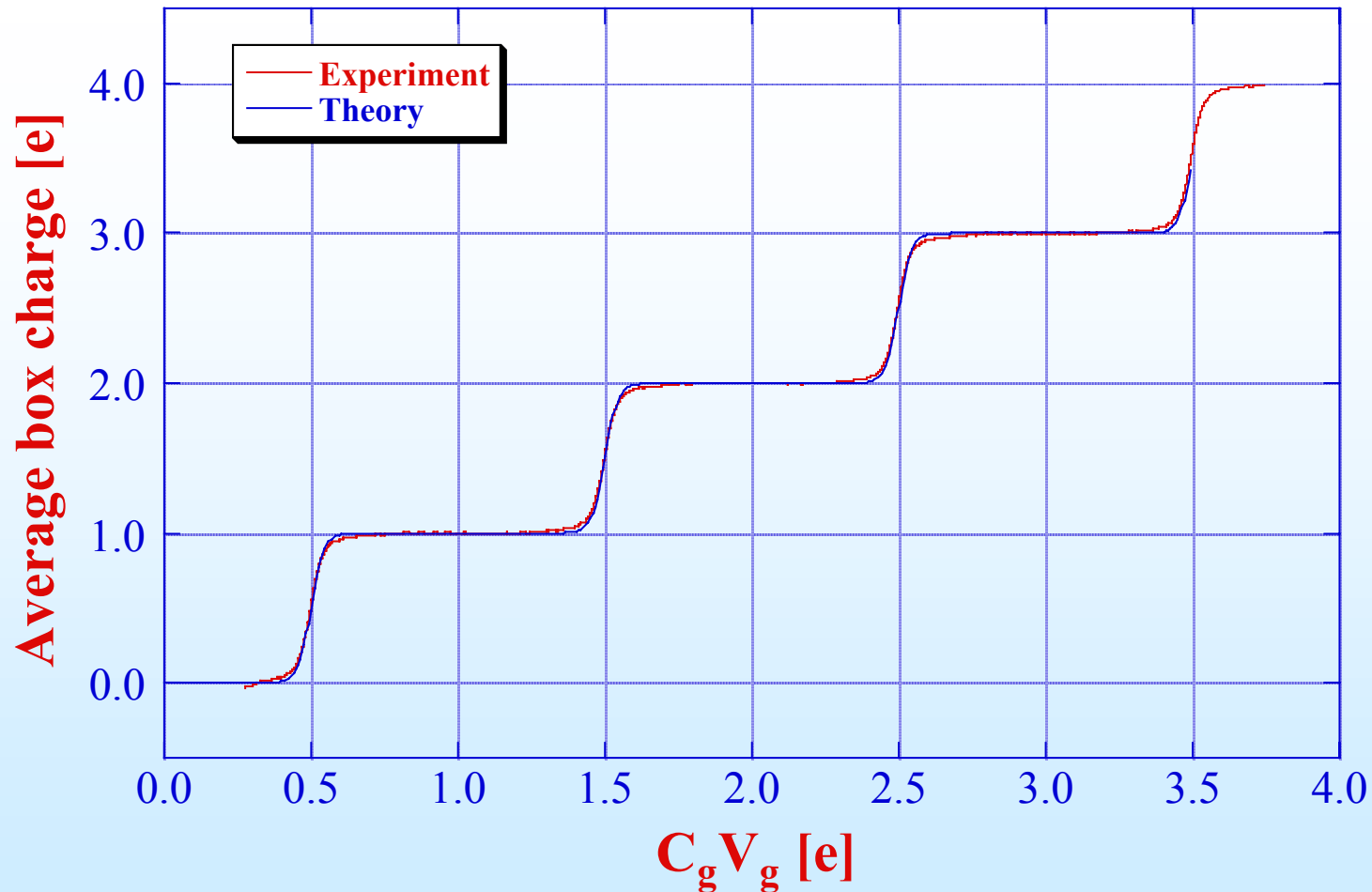
$$f_{\text{carrier}} = 450 \text{ MHz}$$

$$\text{RF-amplitude} \approx -100 \text{ dBm}$$

$$\text{Staircase sweep frequency} = 141 \text{ Hz}$$



The Coulomb blockade staircase, normal state



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Fig. 10

The Coulomb blockade staircase, comparing the normal and the superconducting state

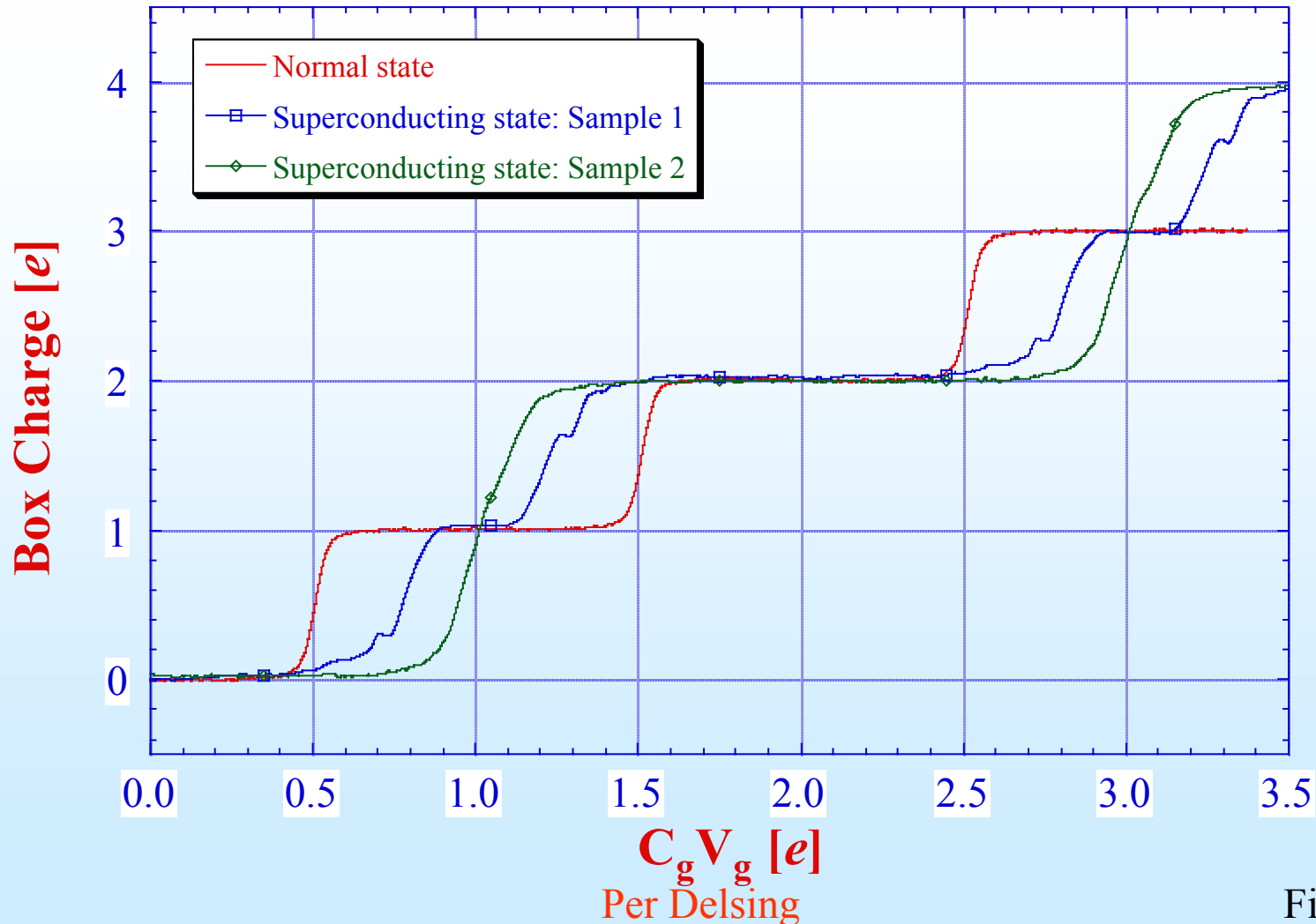
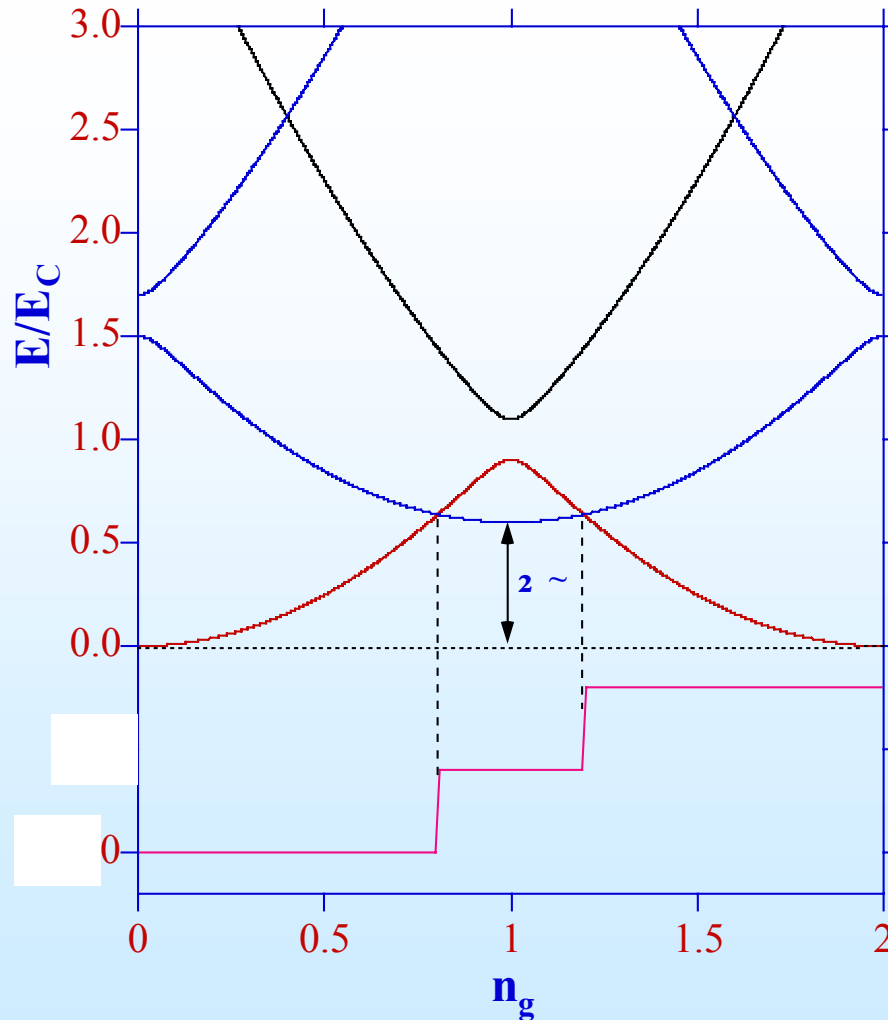


Fig. 11

What would you expect in the superconducting state



$$\tilde{\Delta} \approx \Delta_0 - k_B T \ln(N)$$

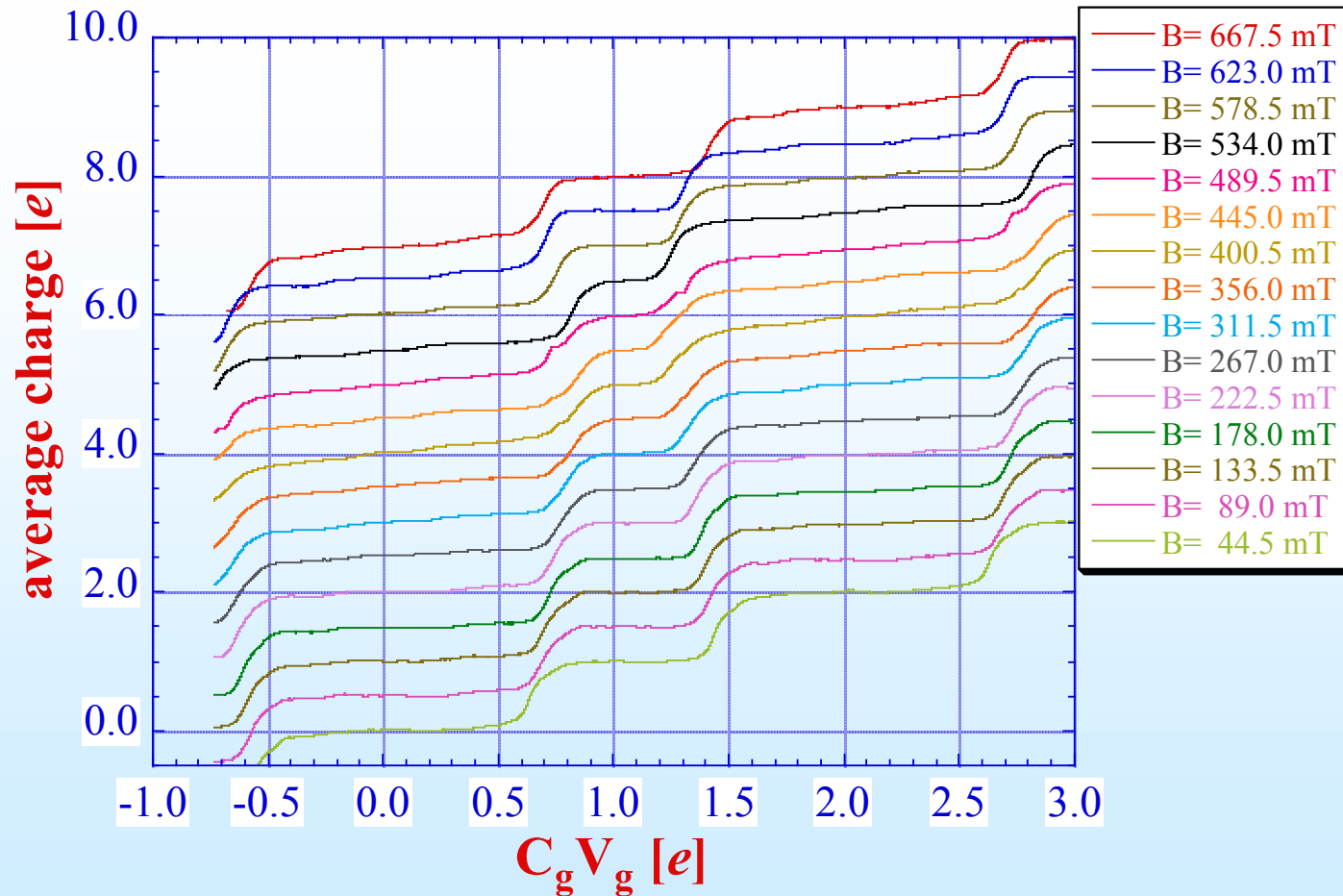
$$\Delta_0 \approx 2.4 \text{ K for Al}$$

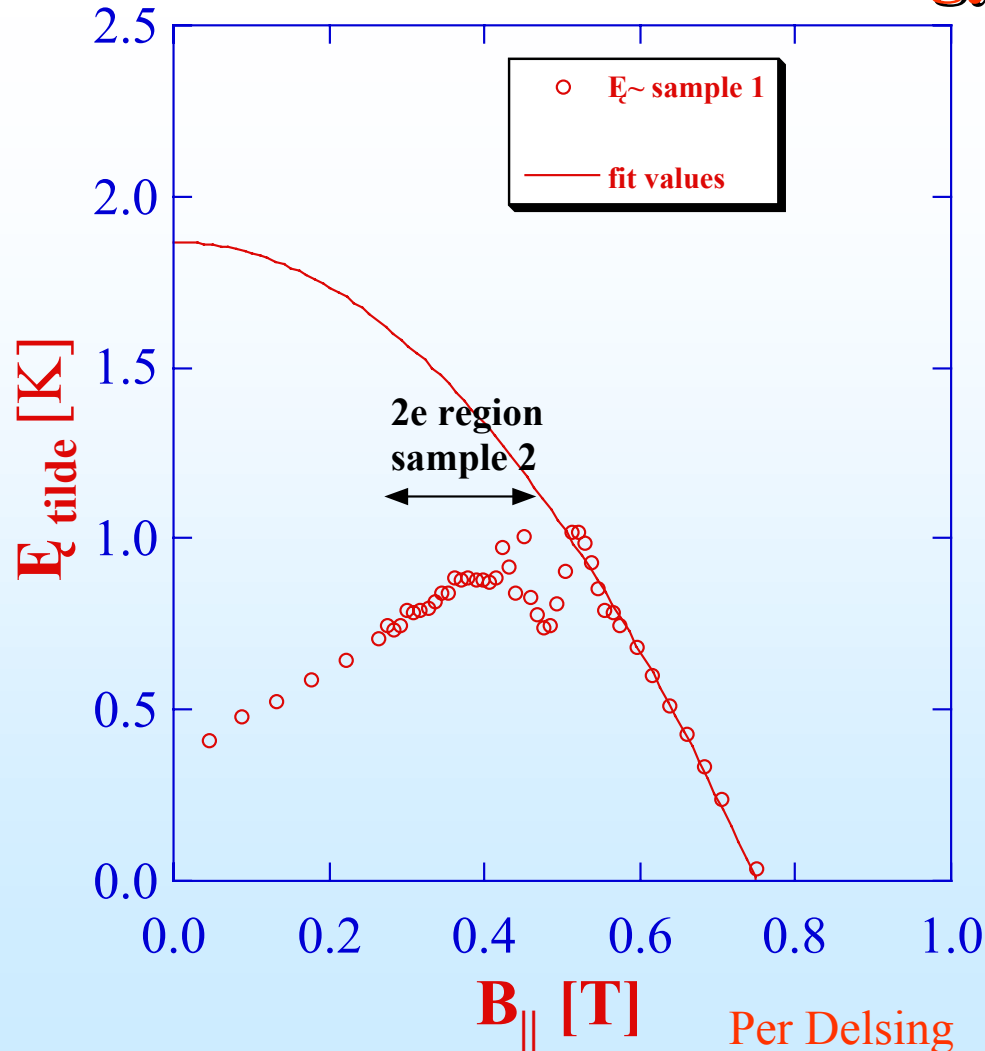
$$\tilde{\Delta} = (L - S) / (L + S)$$

Lafarge et al. Nature (93)

Long Step versus Short Step

Magnetic field dependence of the short step



Extracting $\tilde{\Delta}(B)$:**The odd even energy difference**

$$\tilde{\Delta} \approx \Delta_0 - k_B T \ln(N)$$

$$\Delta_0 \approx 2.4 \text{ K for Al}$$

$$\tilde{\Delta} = (L-S)/(L+S)$$

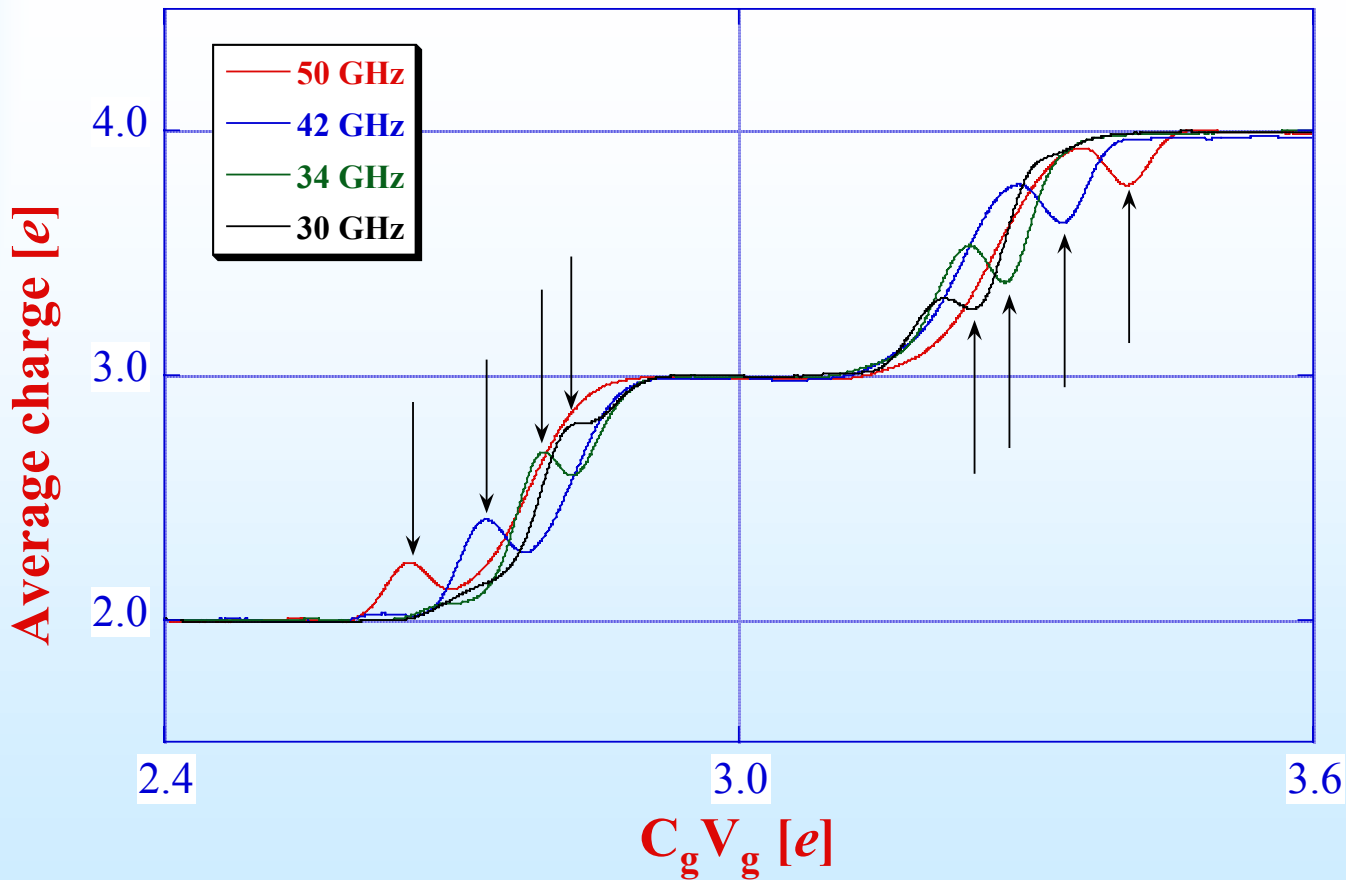
Lafarge et al. Nature (93)

Fig. 15

Spectroscopy

Microwave irradiation of the Cooper-pair box

Frequency dependence



Limited frequency range

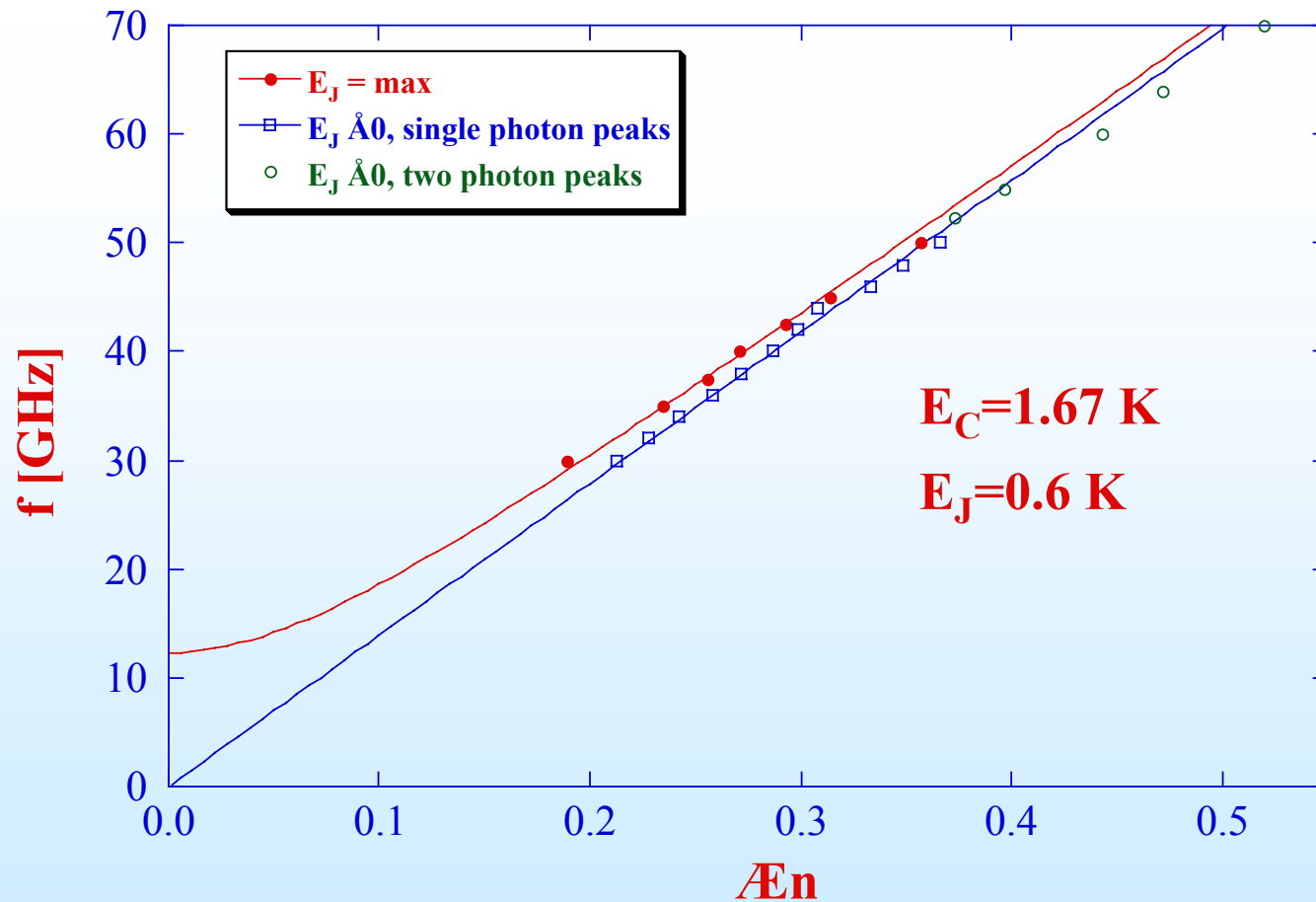
25-50 GHz

Two photon peaks

=> > 50 GHz

(Averaging causes broad peaks)

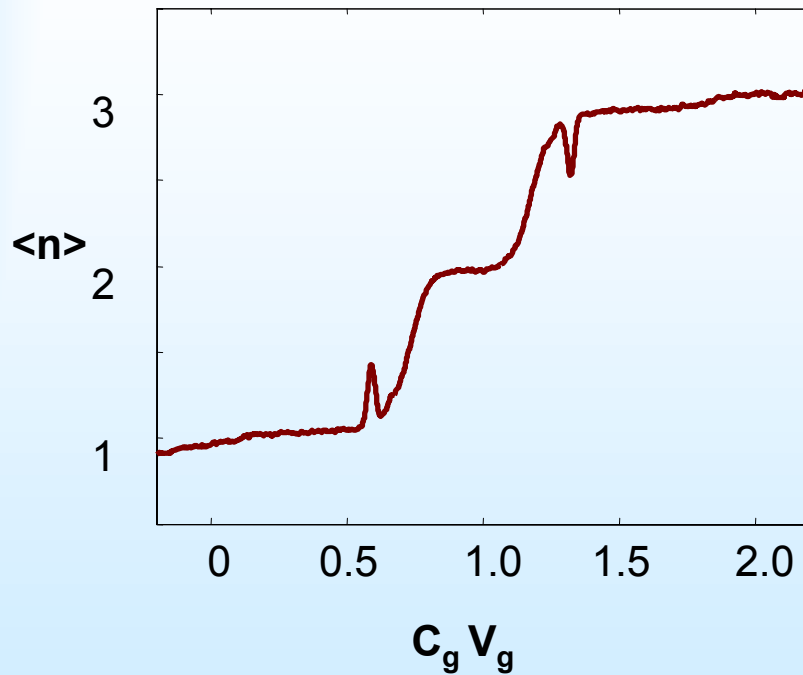
Energy levels extracted from spectroscopy



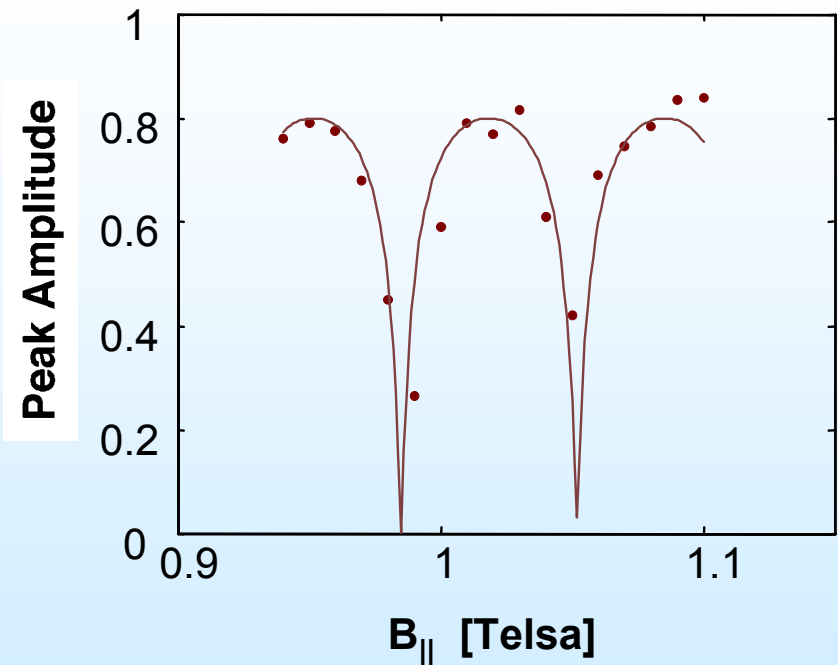
Spectroscopy

B-field dependence

Irradiation by 50 GHz μ -waves

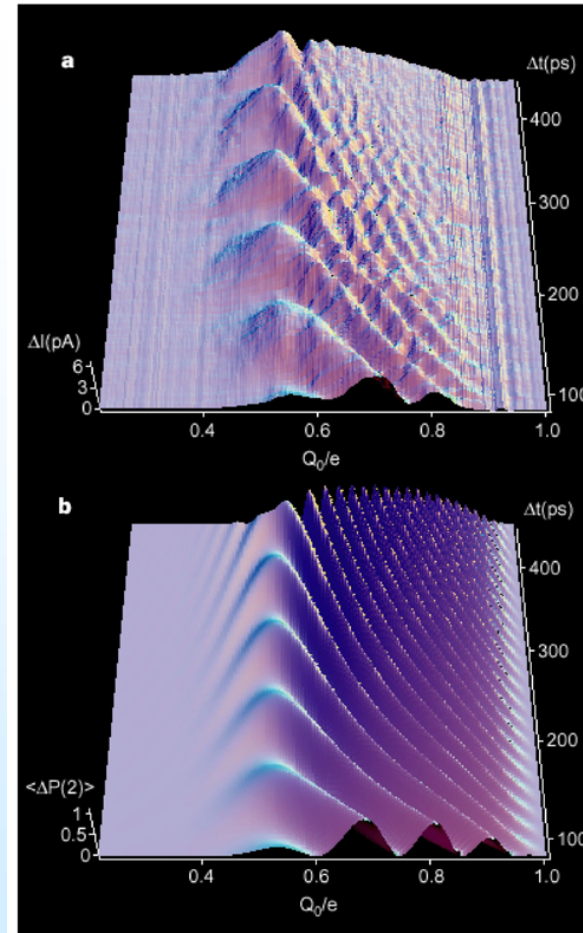
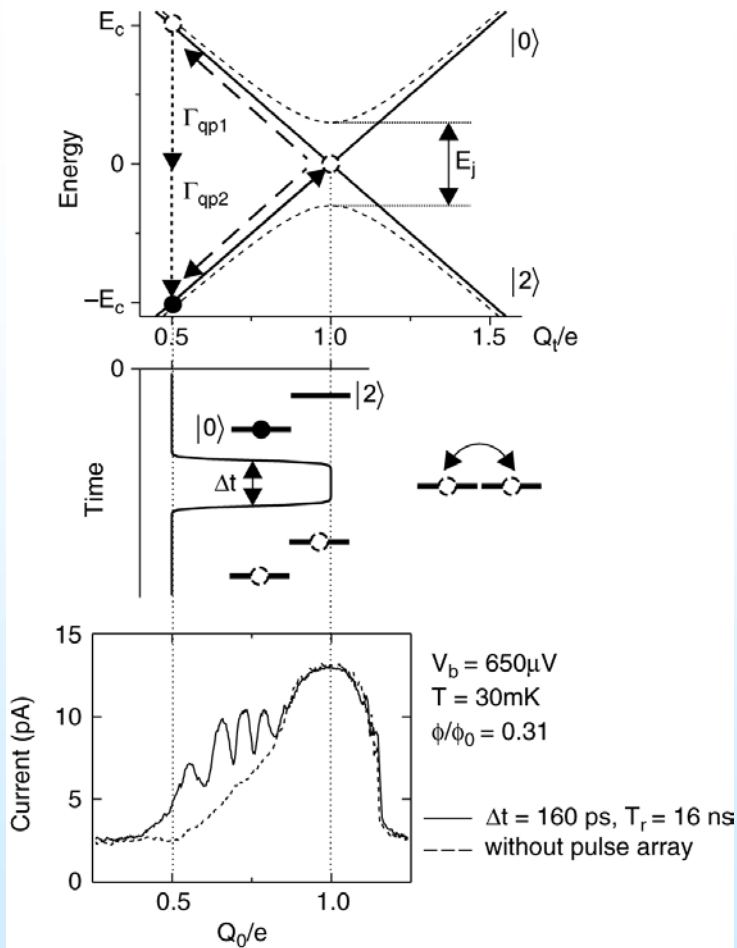


Modulation of E_j with B_{\parallel}



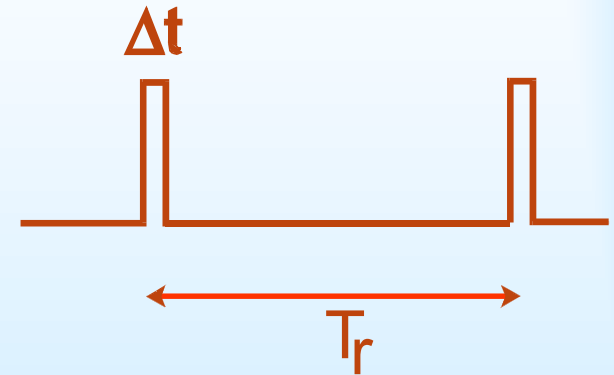
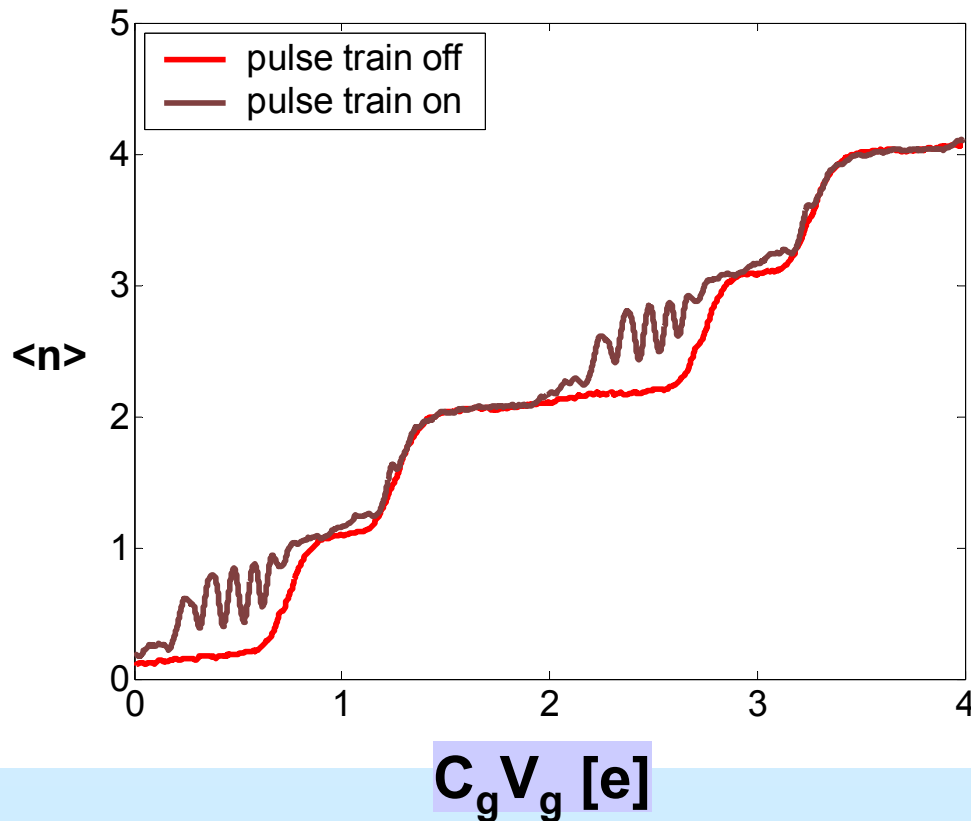
Coherent oscillations

Nakamura, Pashkin and Tsai (1999)

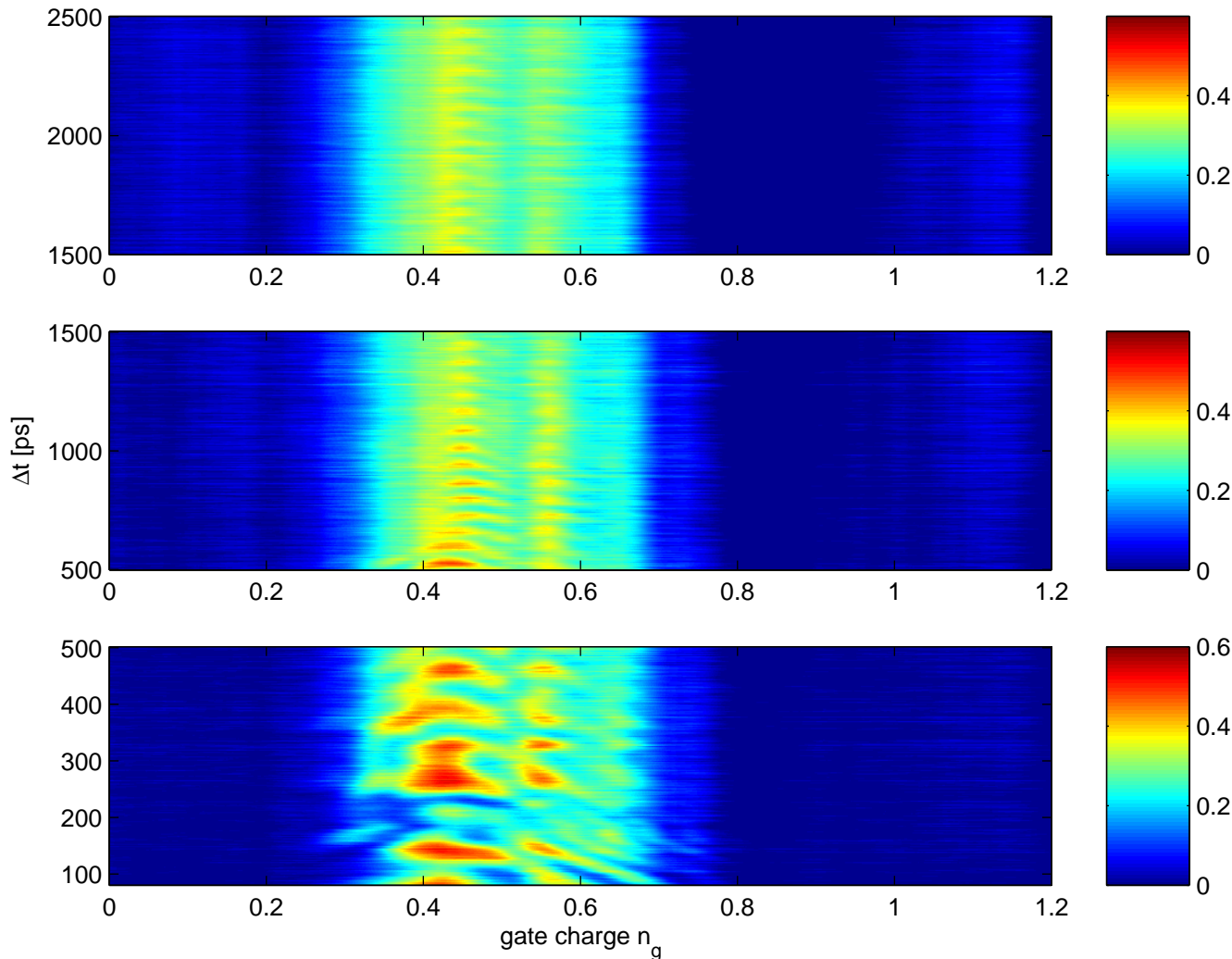


Nakamura et al., Nature (99)

Continuous measurement with $T_r=59\text{ns}$, amplitude $1e$ pulse train



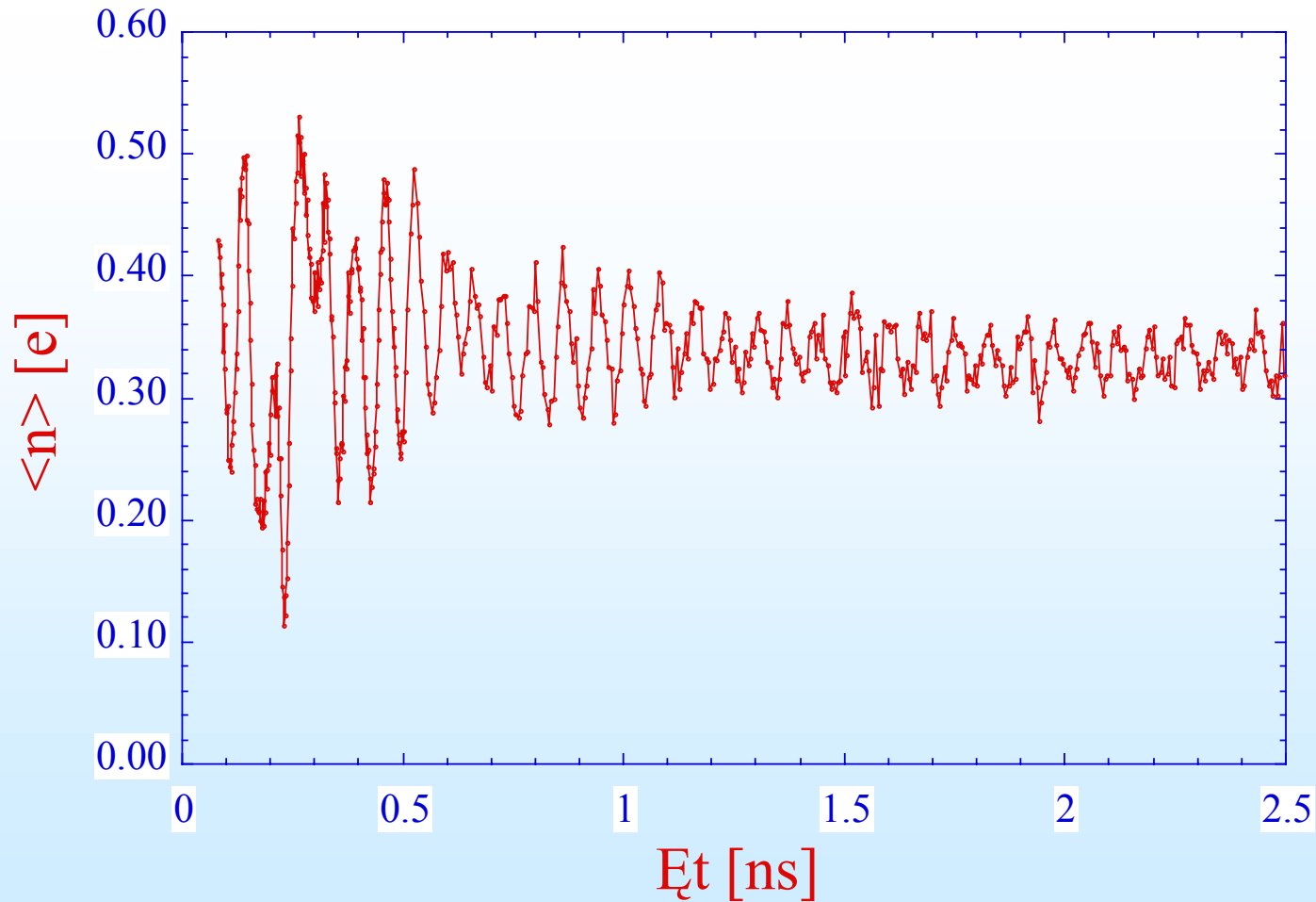
Coherent Oscillations



**Period=70 ps
agrees well
with E_j**

**Color represents
difference between
pulsed staircase and
"unpulsed" staircase**

Signal versus pulse duration



Possible sources of decoherence

- Continuous measurement of course decoheres the system, pulsed measurements should improve the situation.
- Non-equilibrium quasi particles are obviously present in the system.
- Non-perfect dc pulses: the pulse is not perfectly square and thus the system is not exactly at the degeneracy point during the evolution. Therefore background charge noise couples stronger to the system

Summary

- **RF-SET optimized, $\partial Q = 3.2 \mu e / \sqrt{\text{Hz}}$ achieved**
- **Fabrication of integrated Qubit and RF-SET**
- **Characterization of Cooper-pair box**
 - Demonstrated continuous (and pulsed) read-out of box charge.
 - Observation of microwave induced transitions between $|0\rangle$ and $|2\rangle$
 - Determination of E_C and E_J from spectroscopy.
 - Coherent Oscillations observed (reproduced Nakamura's results with RF-SET read-out).