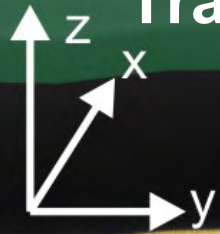


# Nanomechanical resonators

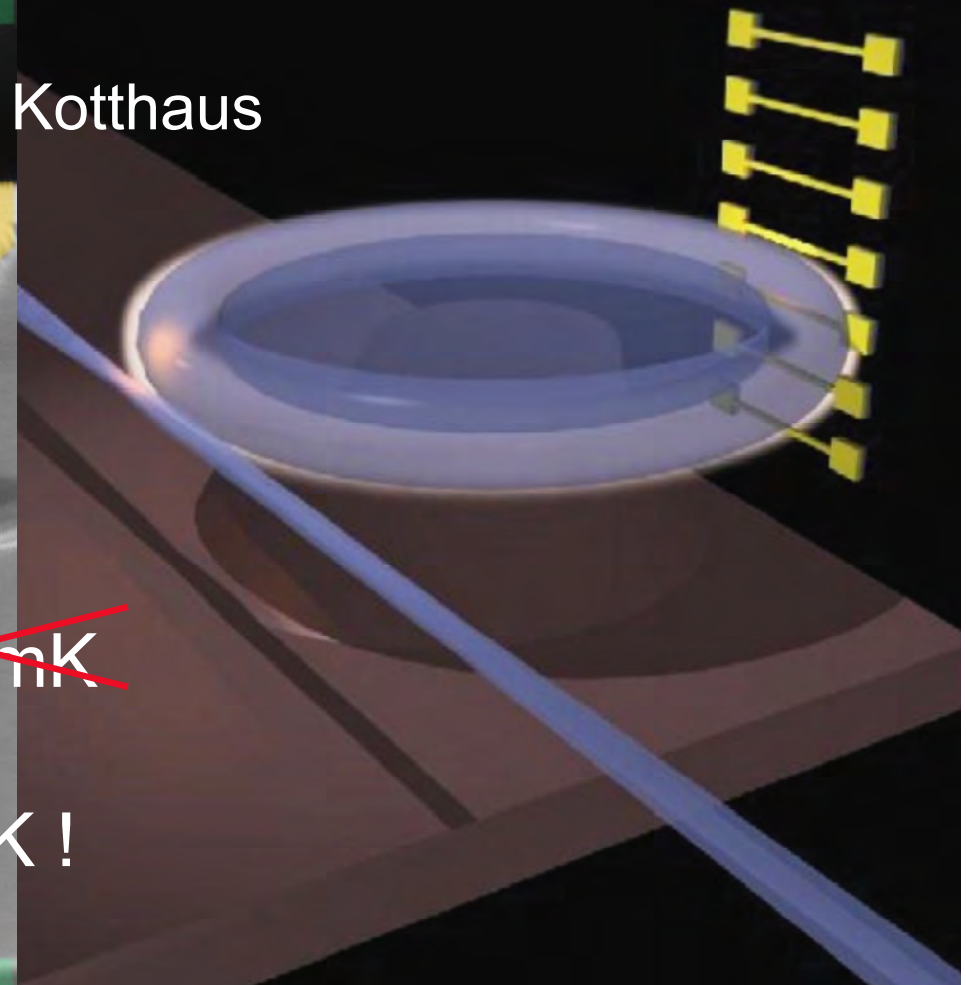
Transduction via electrical and optical gradient forces



Jörg P. Kotthaus

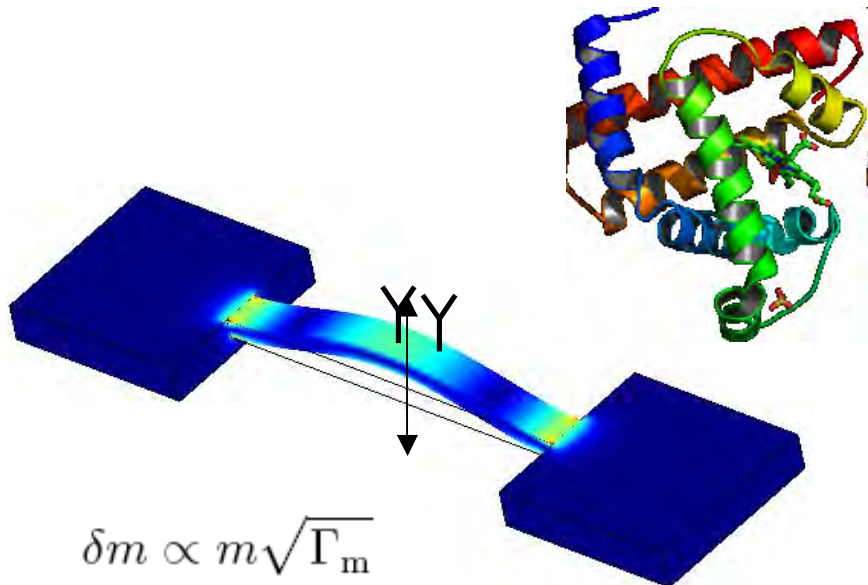
~~300 mK~~

300 K !

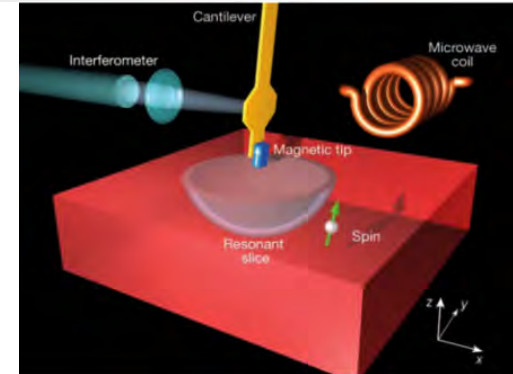


# Why NanoElectroMechanical Systems (NEMS)?

## Sensing of masses, forces, displacements



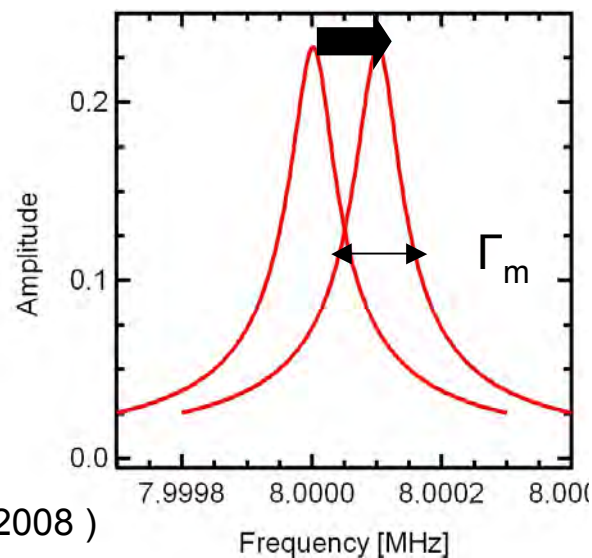
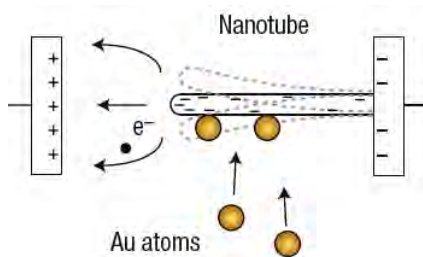
$$\delta F \propto \sqrt{m\Gamma_m}$$



Force sensing with single spin sensitivity  
D. Rugar et al., Nature, **430**, 329 (2004)

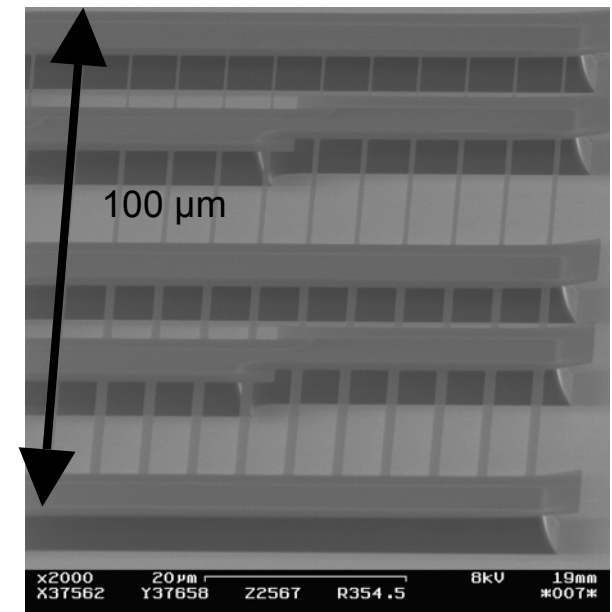
$$\delta m \propto m\sqrt{\Gamma_m}$$

Mass detection  
with single atom  
resolution



K. Jensen et al.,  
Nature Nanotech **3**, 533 (2008)

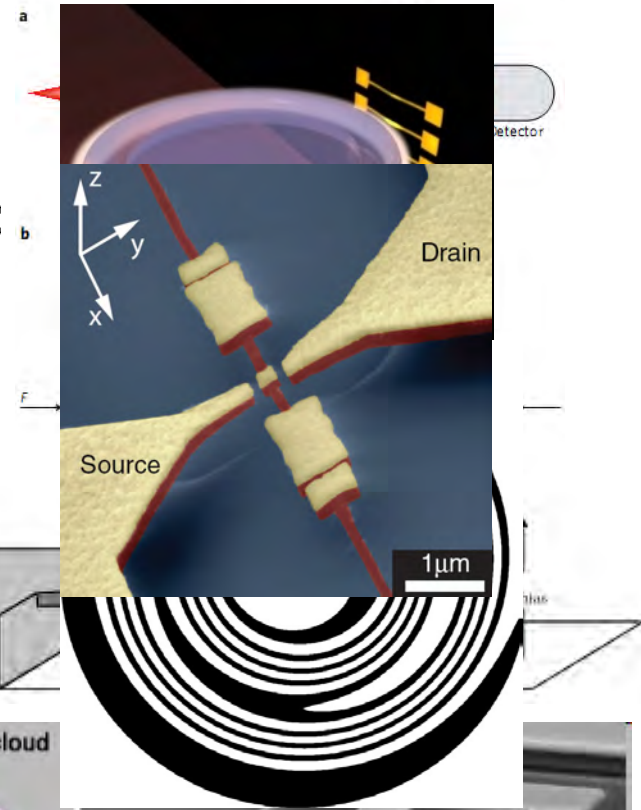
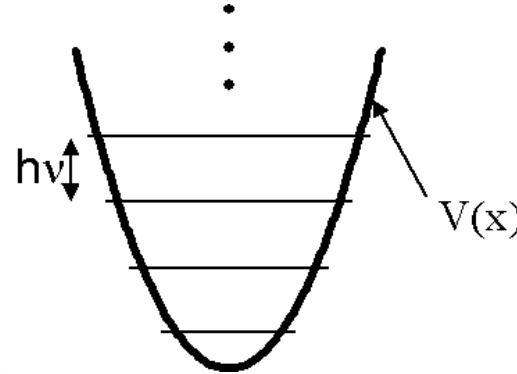
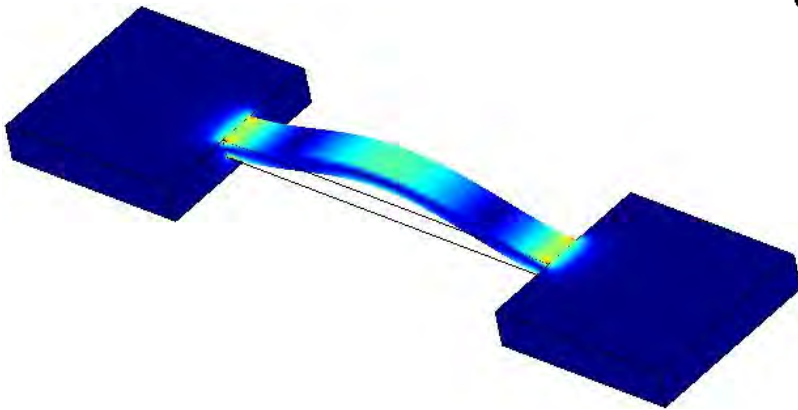
Highly scalable  
here:  $10^4/\text{mm}^2$



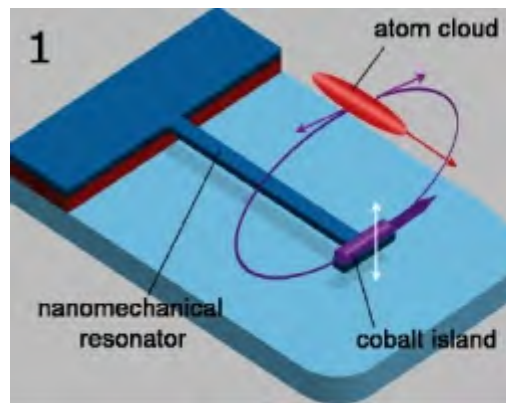
# Why NanoElectroMechanical Systems (NEMS)?

## Some fundamental science problems

### Fundamental Science

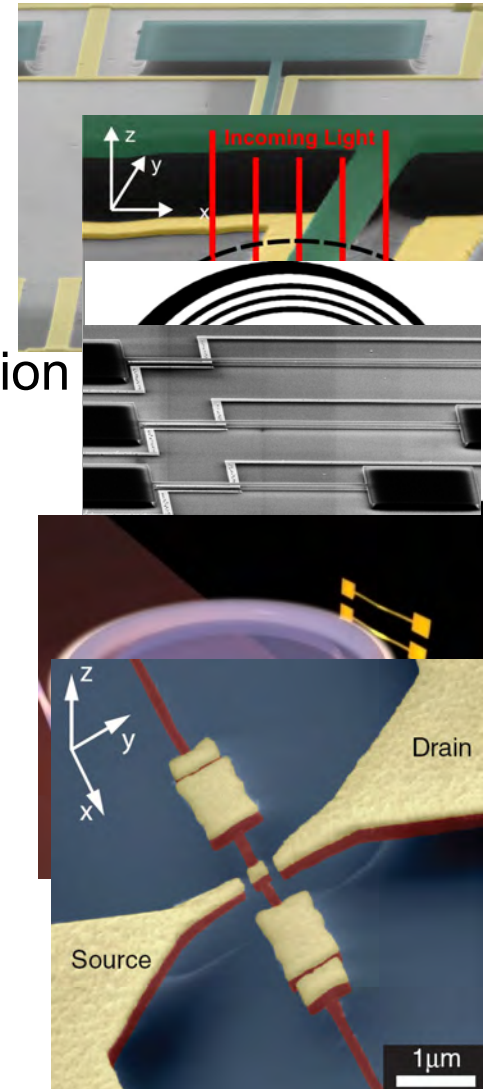


- Zero Point Motion - QNEMS
- Single Electron Shuttle
- Nonlinear Mechanics
- Cavity NanoOptoMechanics
- Hybrid Systems



# Outline

- **Actuation** by electrical gradient fields
- **Detection** on-chip interferometric and self-oscillation
- **Non-linear behavior** and induced switching
- **Damping** and mechanical quality factor
- **Optical gradient field actuation** and
- **Quantum limited detection**
- **Shuttling charge with NEMS**



# On-chip electrical gradient force transduction

---

in collaboration with

Quirin Unterreithmeier   Thomas Faust

Eva M. Weig

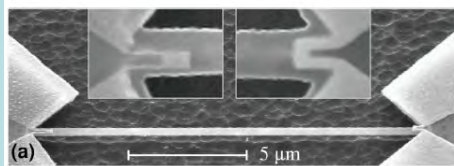
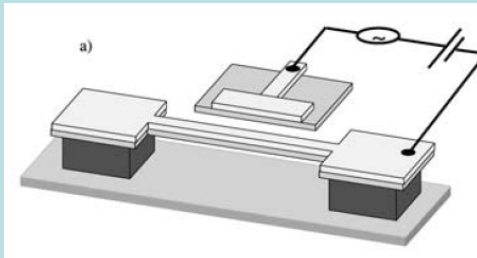


# Actuating nanomechanical resonators

The pros and cons of common schemes

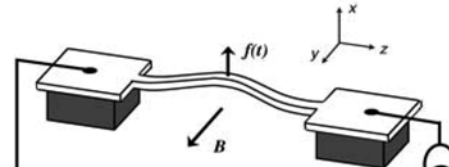
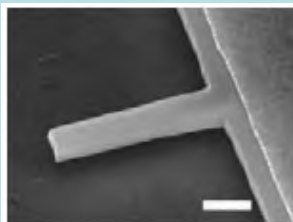
Magnetomotive

Capacitive

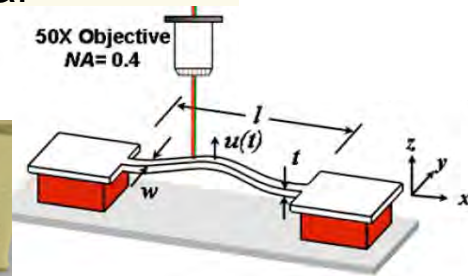


Electrothermal

Piezoelectric  
Material



Photothermal

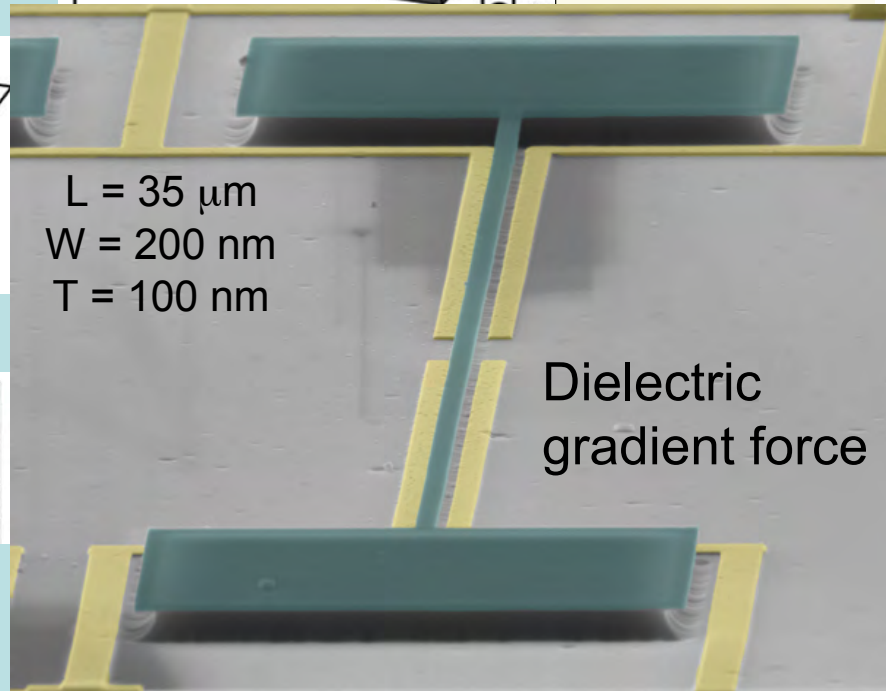


l. Phys. Lett. 88, 223104 (2006)

hybrid inertial drive



g. Ekinci, Small1, 786 (2005)



$L = 35 \mu\text{m}$   
 $W = 200 \text{ nm}$   
 $T = 100 \text{ nm}$

Dielectric  
gradient force

*Local actuation*

- + highly integrable
- + large bandwidth
- material & temperature constraints

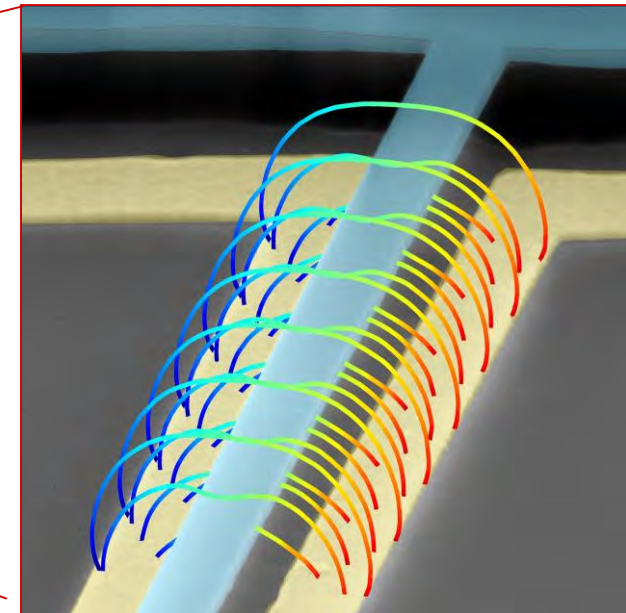
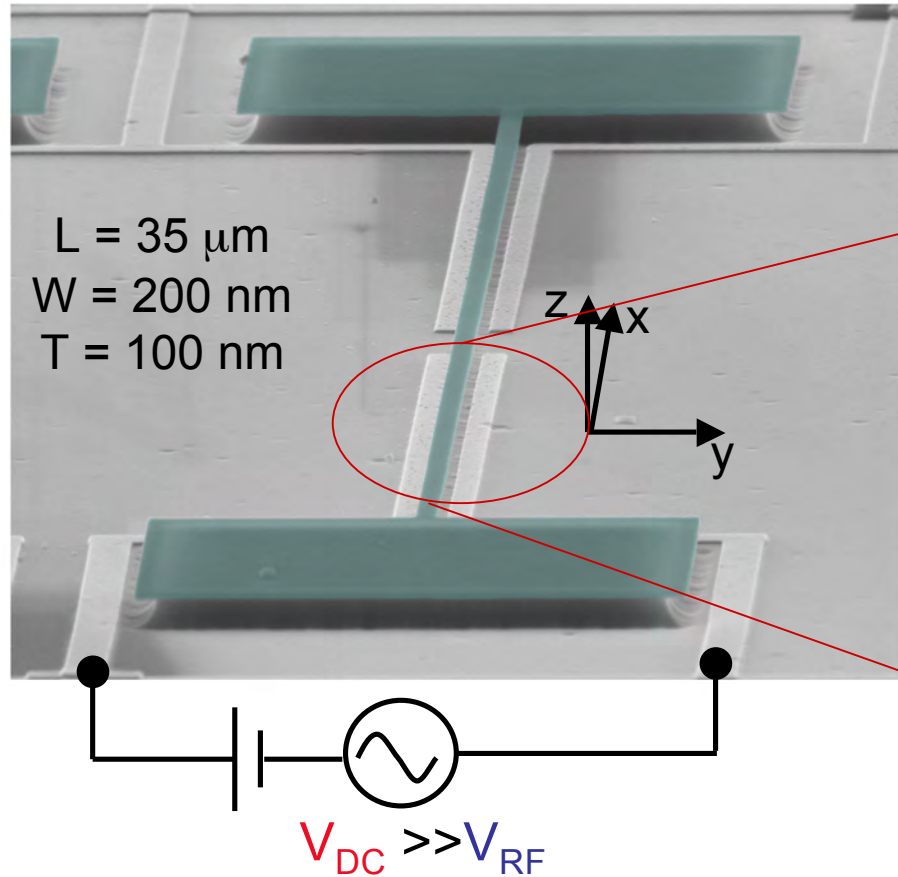
*External actuation*

- + low material constraints (highest Q)
- not integrable
- high frequency limitations



# The principle of dielectric actuation via a gradient force

A polarizable body subject to a gradient field will experience a force



$V_{DC} \rightarrow$  polarization

$V_{RF} \rightarrow$  actuation

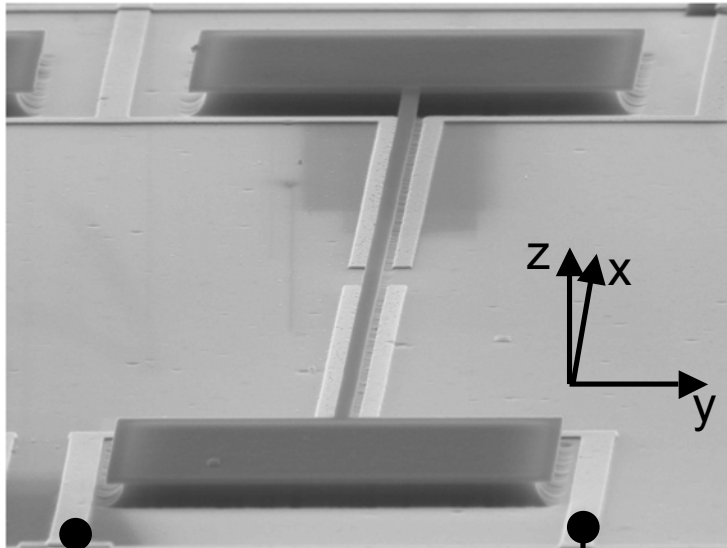
$$F_z = P_y \frac{\partial E_z}{\partial y} \propto E_y E_z$$

Q. Unterreithmeier, E. M. Weig, J. P. Kotthaus, *Nature* 458, 1001 (2009).

see also: S. Schmid et al., *Appl. Phys. Lett.* 89, 163506 (2006)

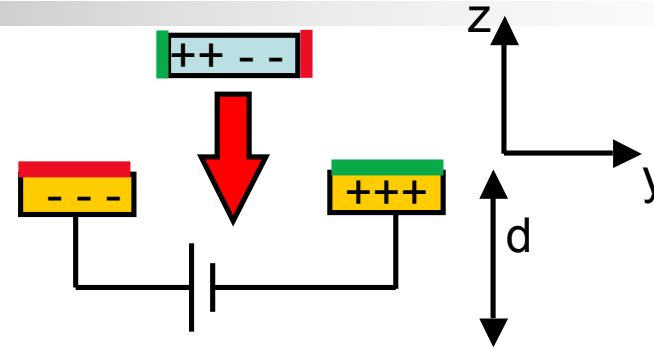
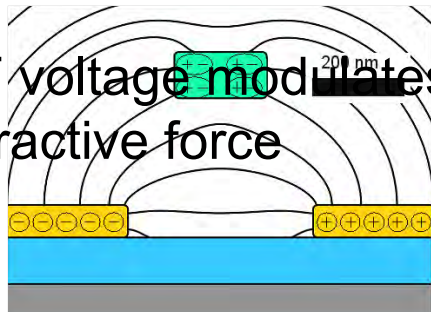


# The principle of dielectric actuation

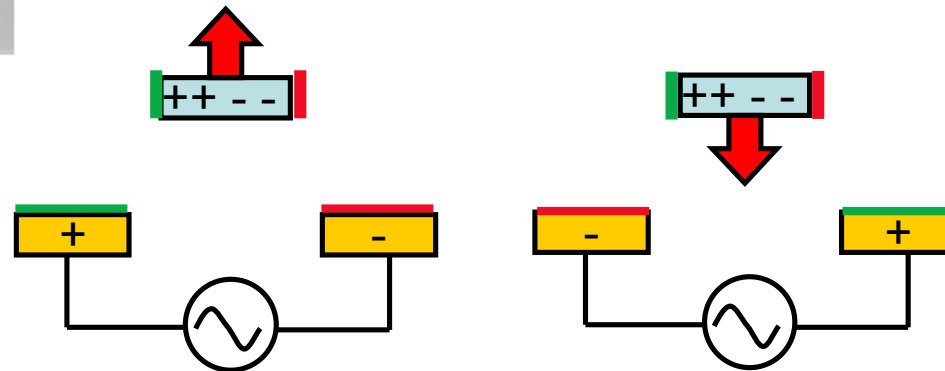


$V_{DC} \gg V_{RF}$   
 DC voltage influences dipolar moment

RF voltage modulates attractive force



$$F_{DC} = P_y \frac{\partial E_y}{\partial z} \propto V_{DC}^2$$

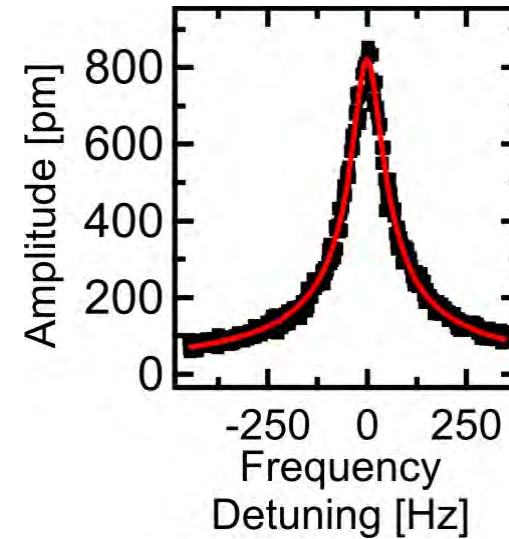
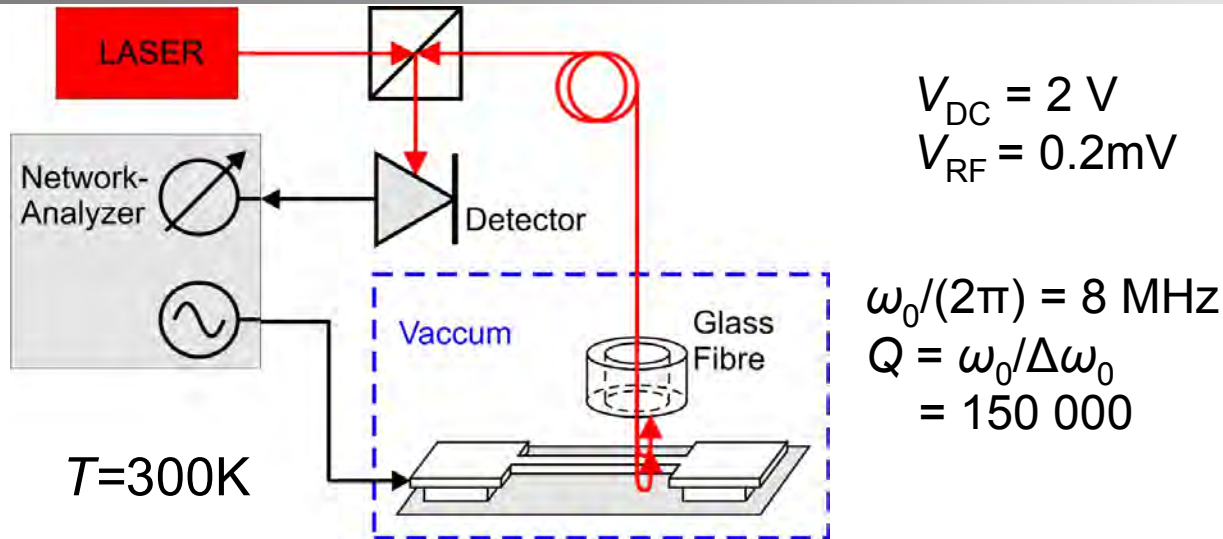


$$F_{RF} = P_y \frac{\partial E_y}{\partial z} \propto V_{DC} V_{RF}$$





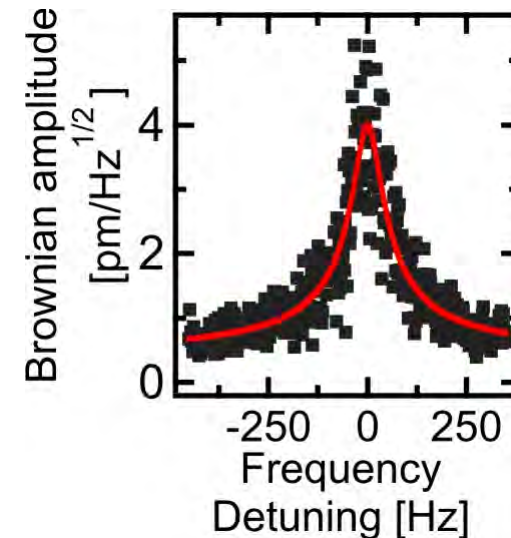
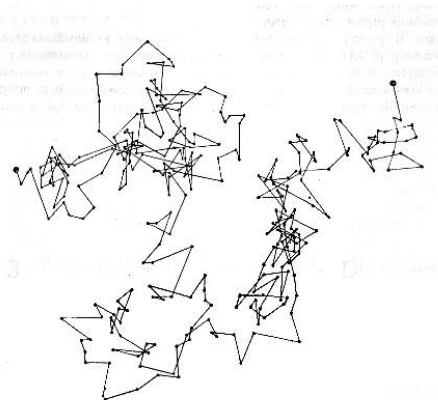
# Dielectric actuation with interferometric detection



$$\frac{\partial^2}{\partial t^2} u[x, t] + \frac{\omega_0}{Q} \frac{\partial}{\partial t} u[x, t] + \omega_0^2 u[x, t] = \frac{F_z}{m} \cos[\omega t]$$

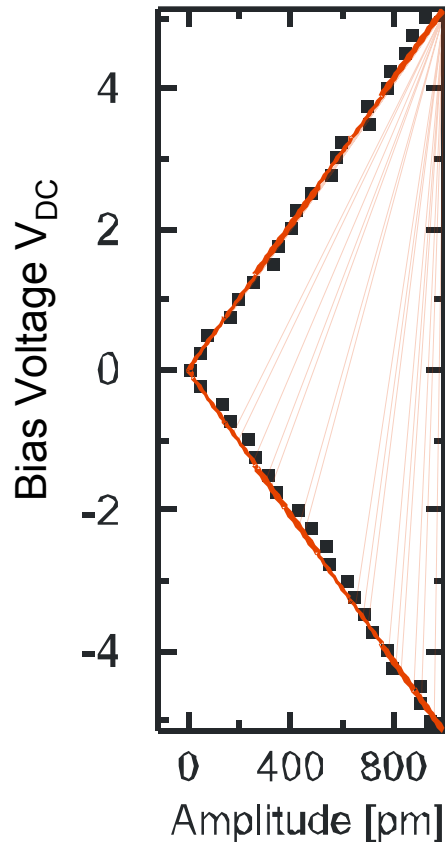
Displacement calibration through Brownian motion

$$\frac{1}{2} k_B T = \frac{1}{2} m \omega_0^2 \langle x^2 \rangle$$

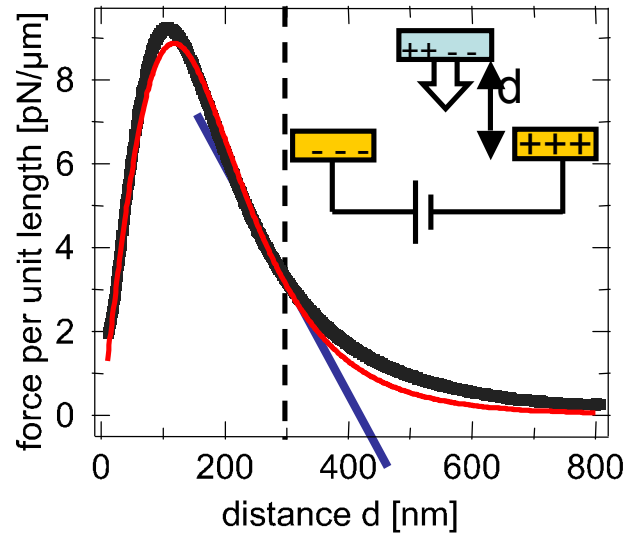


# Dielectric actuation – DC tunability

$$V_{RF} = 0.2 \text{ mV}$$

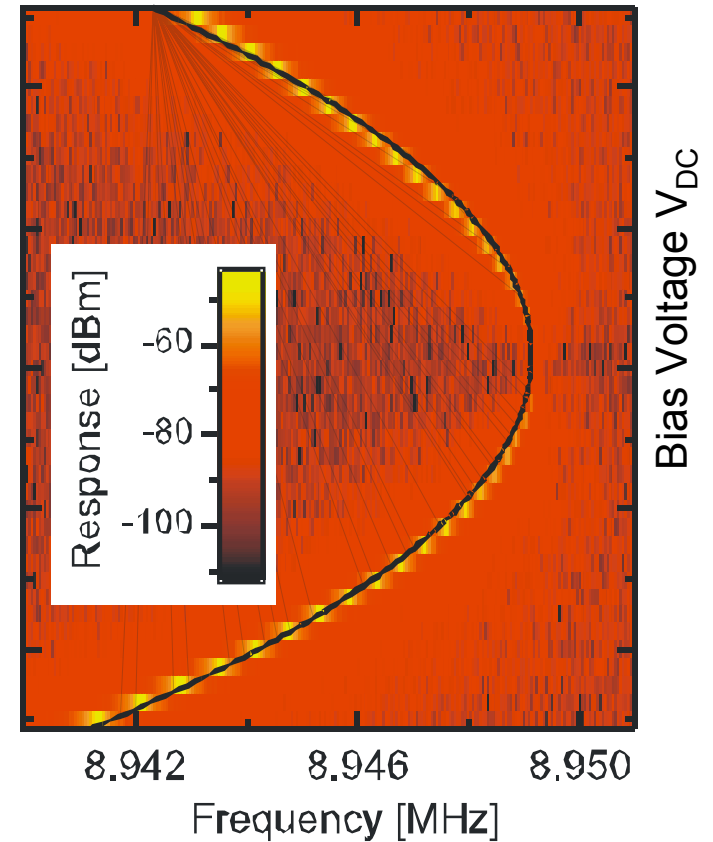


$$F_{RF} \propto V_{DC} V_{RF}$$



The force gradient counteracts the spring constant

$$\frac{\partial F_{DC}}{\partial z} \propto F_{DC} \propto V_{DC}^2$$

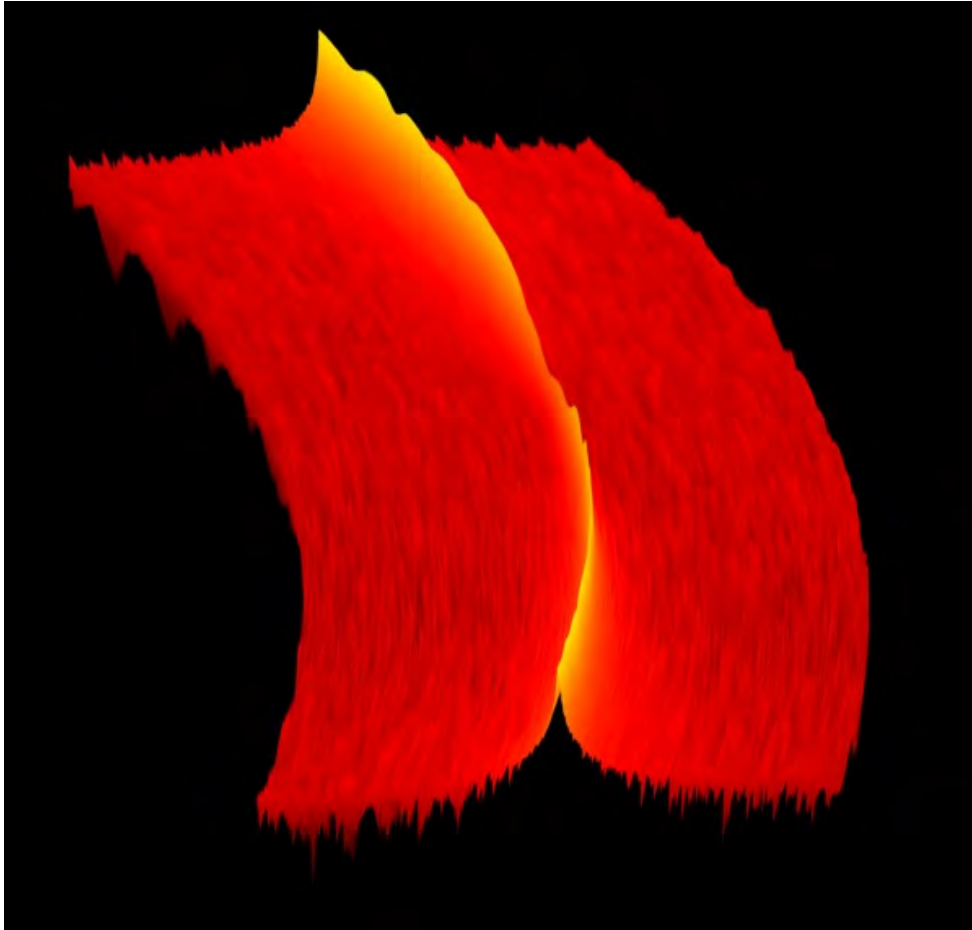


Tunability range ~1000 FWHM



# Dielectric actuation of nanomechanical resonators

Combining the advantages of local and external actuation



+ local, all-electronic, i.e. integrable

+ applicable to most materials  
( $Q = 100,000 - 150,000$ )

+ polarization control via  $V_{DC}$

+ efficient ( $V_{RF} > 5 \mu V$ )

+ scalable to high frequencies

$$R = 50 \Omega$$

$$C_{\text{mutual}} = 1.5 \text{ fF}$$

$$\Rightarrow f_{\text{cutoff}} = 1/(2\pi RC_{\text{mutual}}) \approx 2 \text{ THz}$$

+ frequency tuning  $\sim V_{DC}^2$   
amplitude tuning  $\sim V_{DC}$

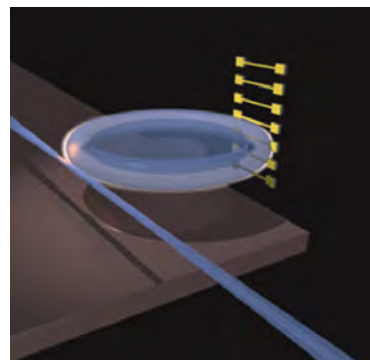
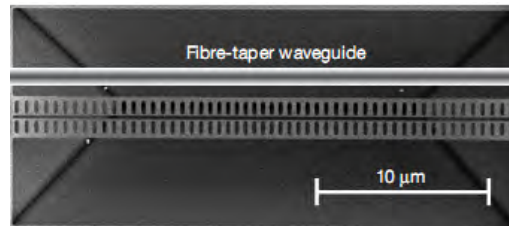
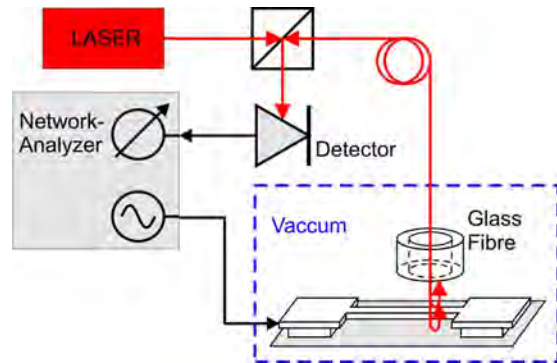
Q. Unterreithmeier, E. M. Weig, J. P. Kotthaus, *Nature* 458, 1001 (2009).



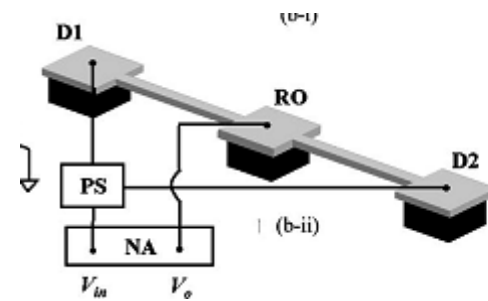
# Towards scalable on-chip detection

## Representative presently employed detection schemes

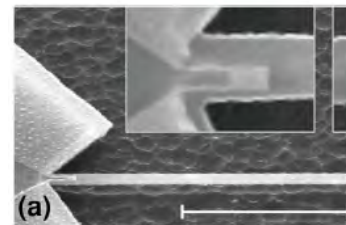
### Optical



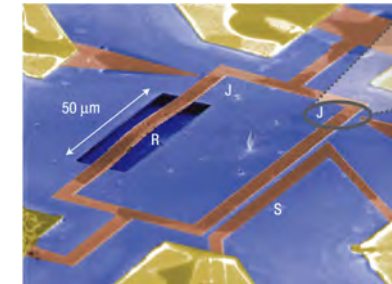
### Electrical



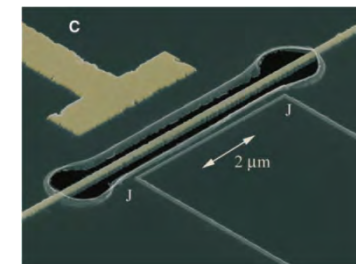
### Magnetomotive



### Piezoresistive



### Flux-modulation



### Single Electron Transistor

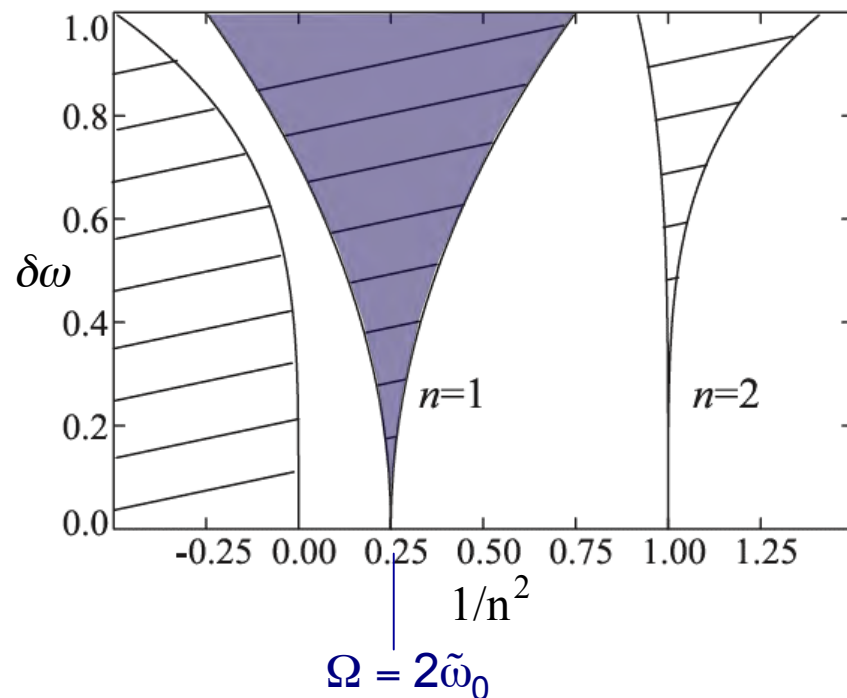


# Parametric actuation

Self-oscillation without externally applied driving force

Modulate resonance frequency of the resonator at twice the resonance frequency:

$$\frac{\partial^2}{\partial t^2} u[x] + \frac{\omega_0}{Q} \frac{\partial}{\partial t} u[x] + \omega_0^2 (1 + \delta \sin(2\omega t)) u[x] = 0$$



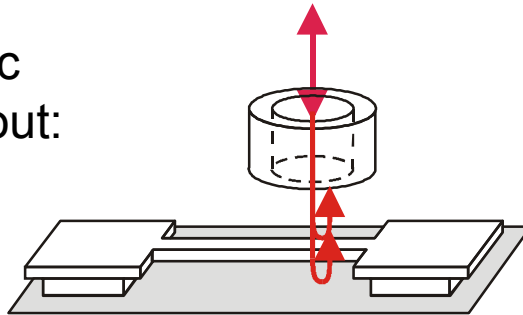
Instability and spontaneous self-oscillation for  $\delta\omega > \frac{\tilde{\omega}_0}{Q}$  .



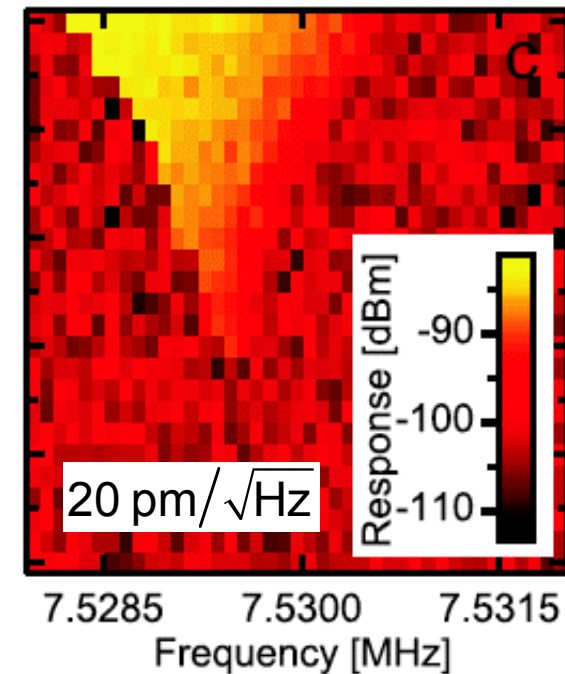
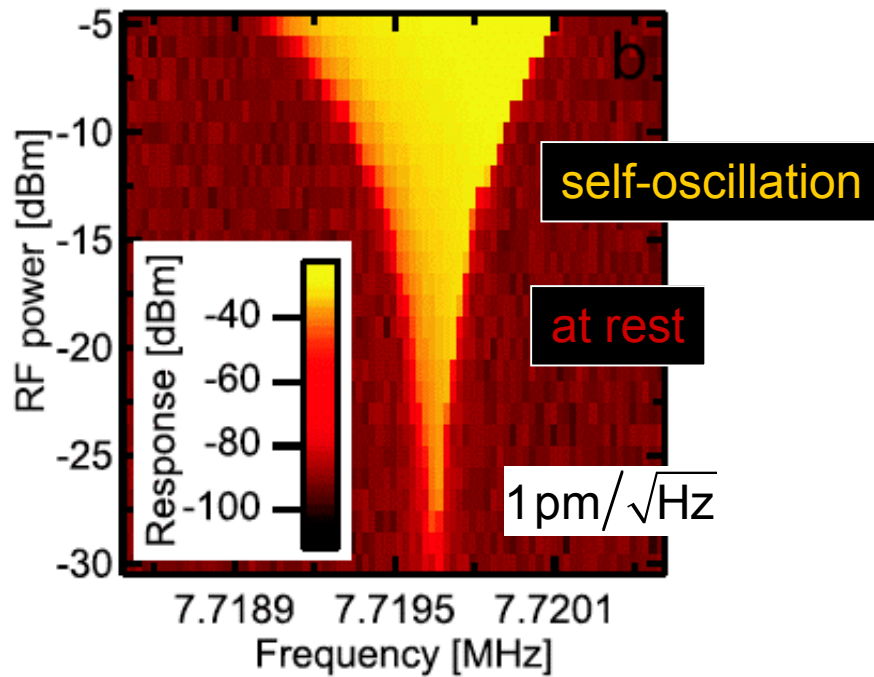
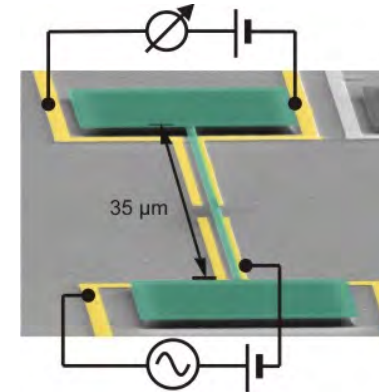
# Parametric actuation and dielectric detection

Modulating the resonance frequency at  $2f_0$  via " $V_{DC}$ " allows to invert the actuation principle

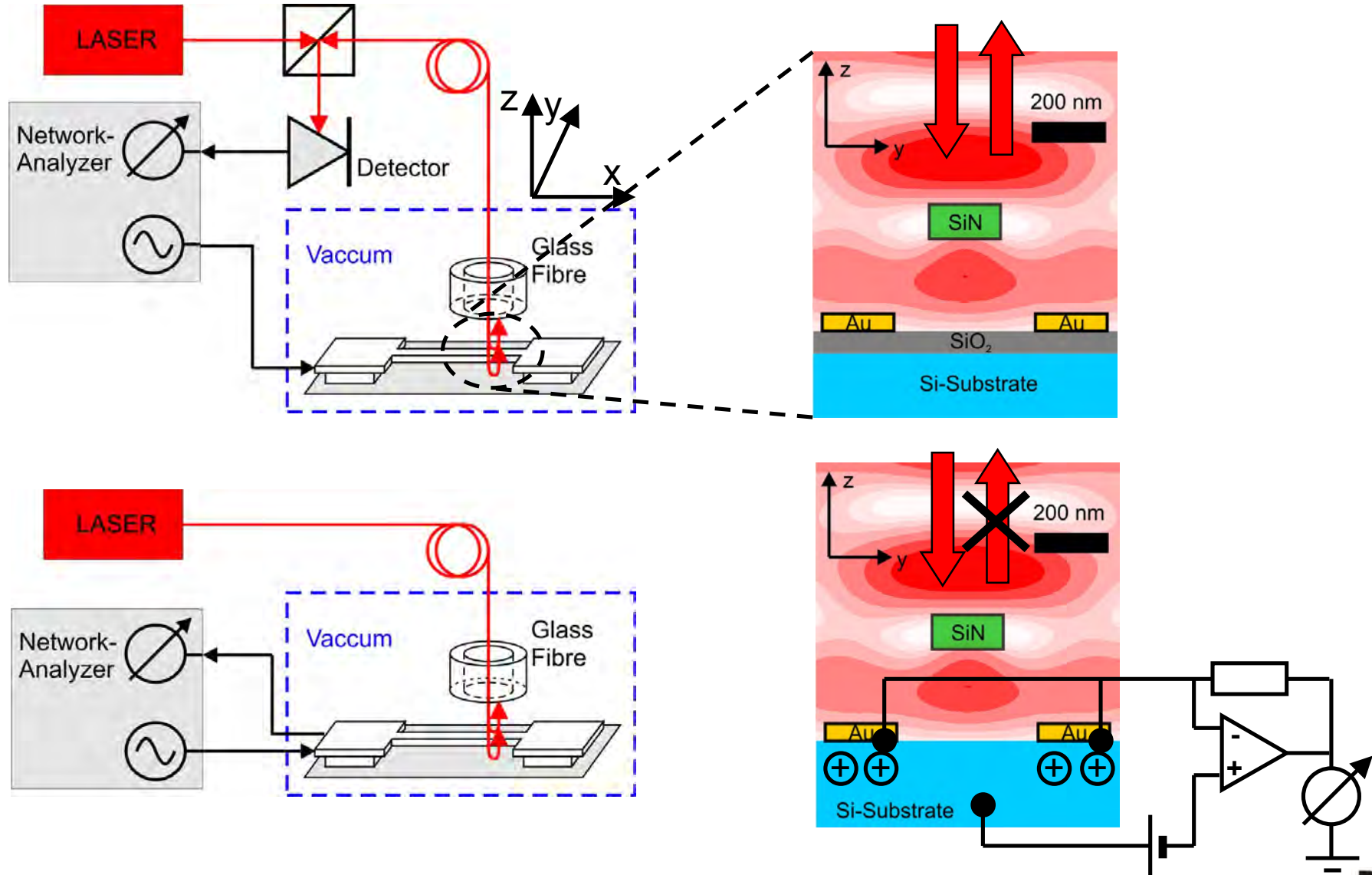
interferometric  
readout:



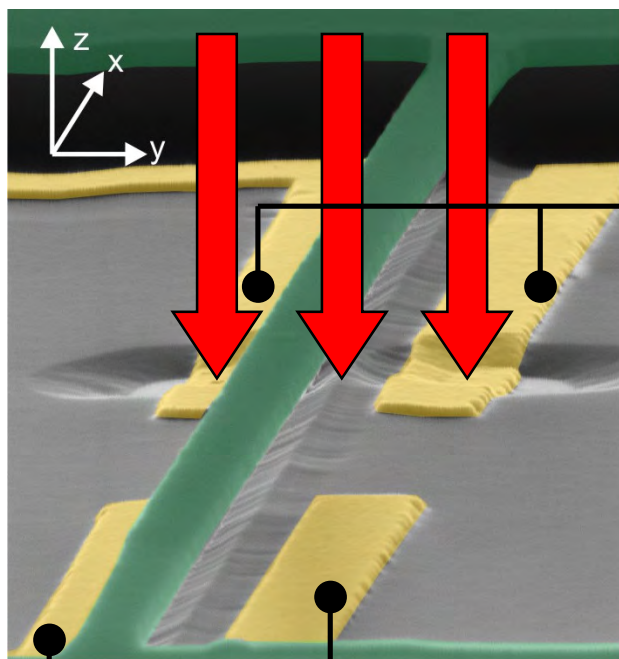
dielectric readout:



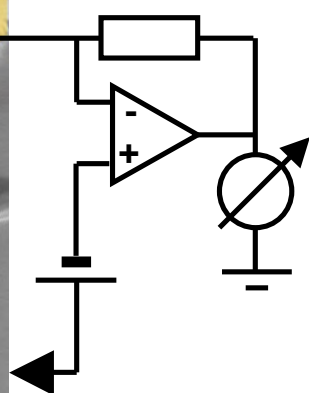
# Concept of on-chip interferometric detection



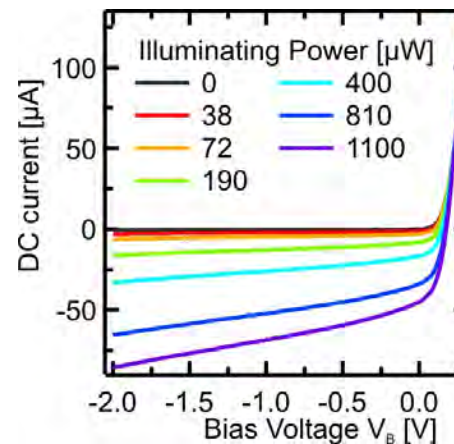
# On-chip interferometric detection with Schottky photodiode



No Q-loading!  
Non-Demolition

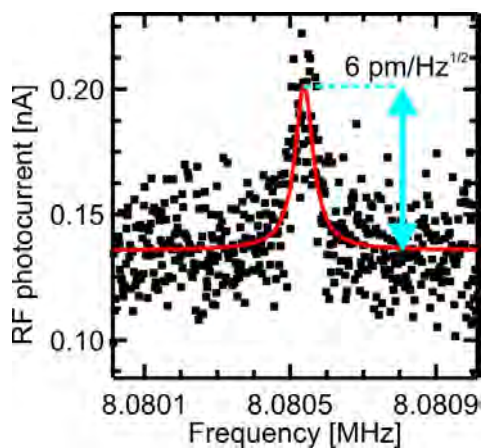


### DC response

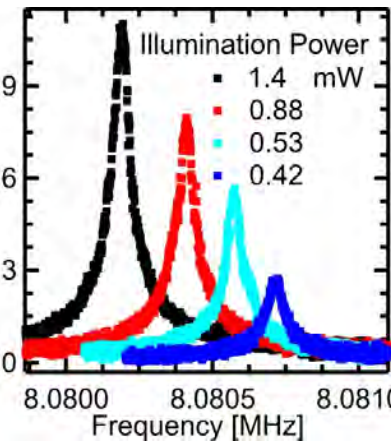
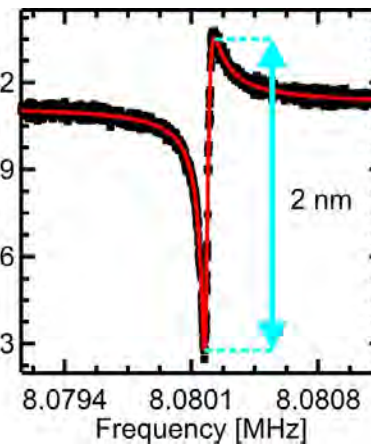


### RF response

#### Brownian

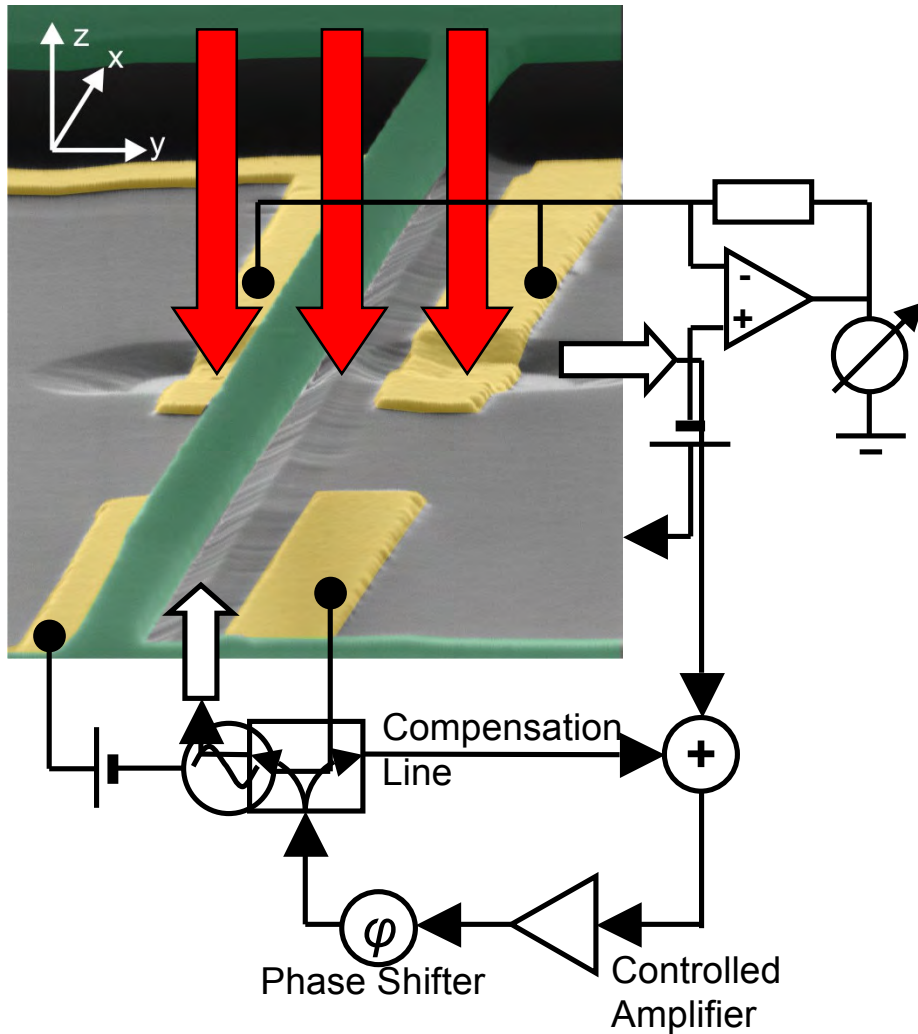


#### Externally actuated

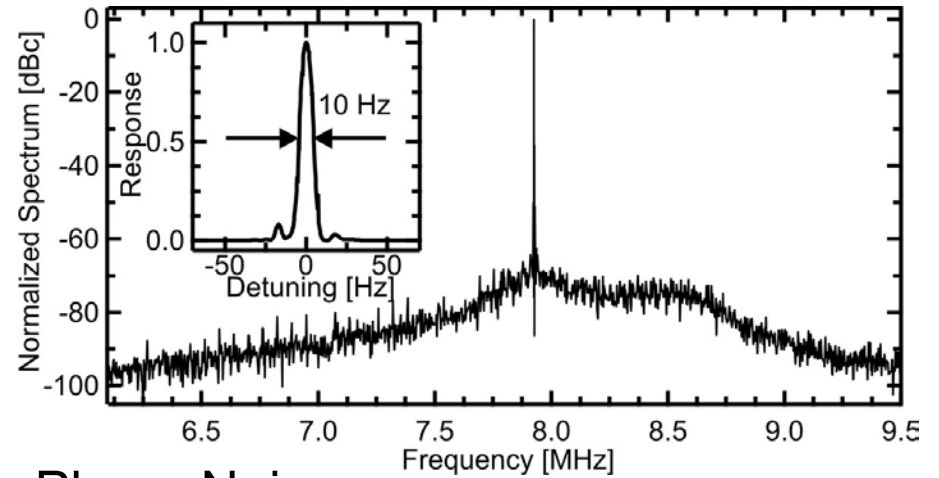




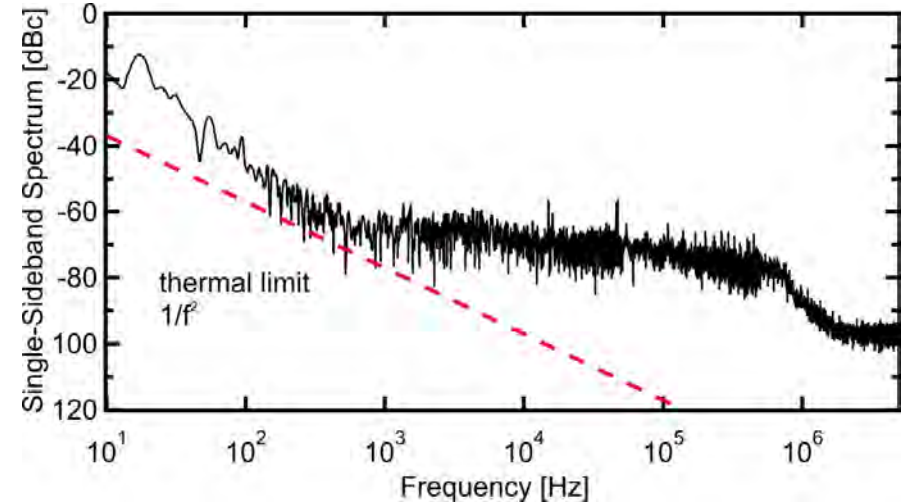
# Feedback-stabilized self-exciting oscillator (PLL)



## Self oscillation



## Phase Noise

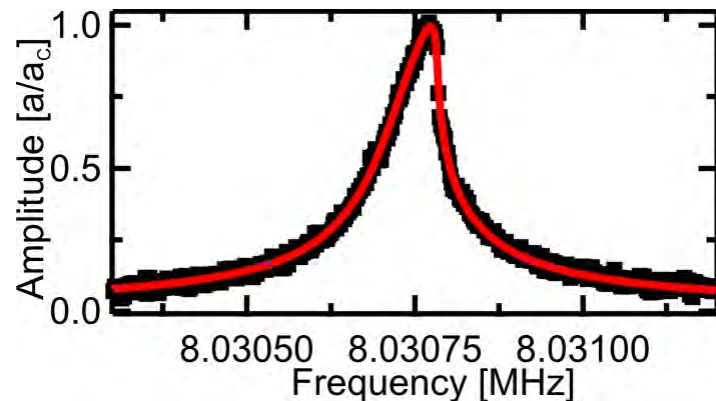


# Non-linear nanomechanical oscillators - quasistatic behavior

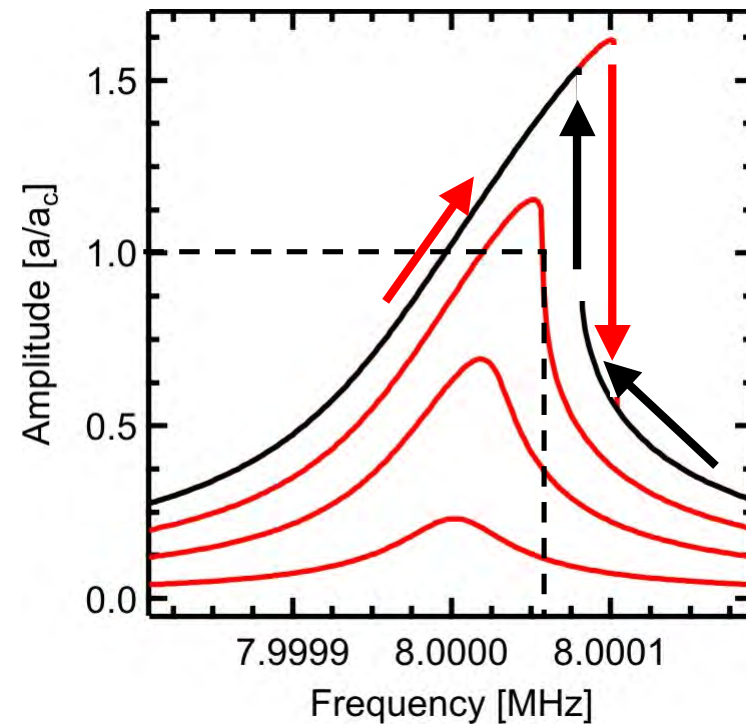
$$\frac{\partial^2}{\partial t^2} u[x] + \frac{\omega_0}{Q} \frac{\partial}{\partial t} u[x] + \omega_0^2 (1 + \alpha u[x]^2) u[x] = \frac{F}{m} \cos[\omega t]$$

Equation of motion of a Duffing oscillator

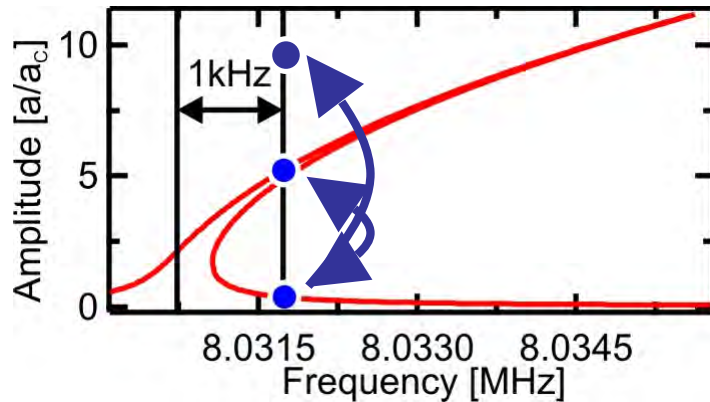
$$u = a[\omega] \cos[\omega t + \gamma[\omega]]$$



-> Fitting yields  $\omega_0, Q, \alpha$

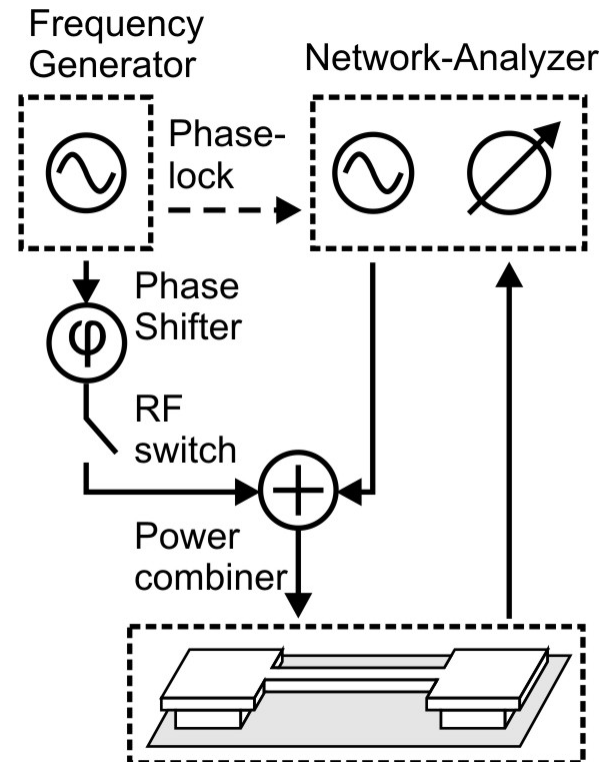


# Nonlinear nanomechanics - dynamical behavior



Driven resonator with  
cw excitation at  $f_0 + \sigma$  ( $\sigma = 1\text{kHz}$ )

Fast switchable memory element  
employing short resonant RF-pulses?

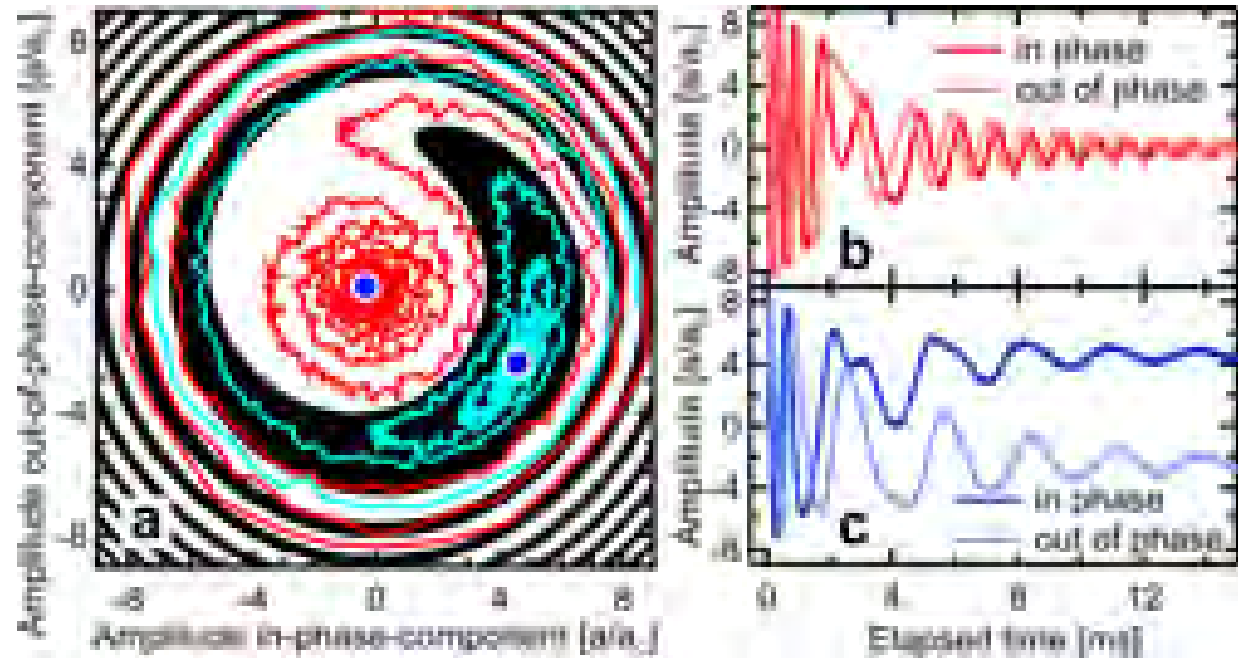
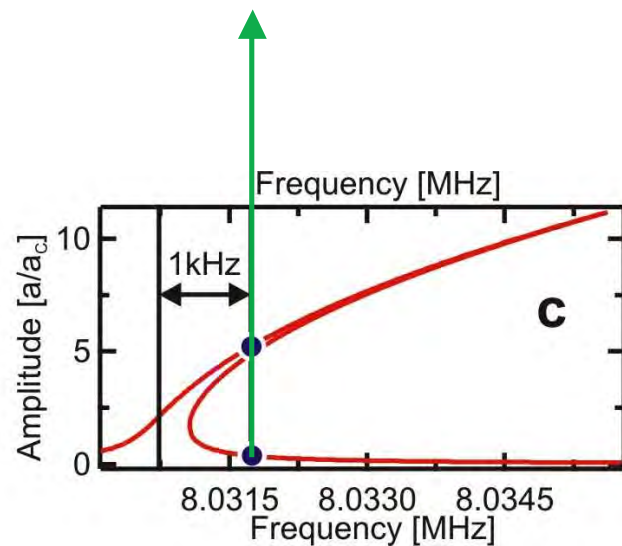


R. L. Badzey et al.,  
Appl. Phys. Lett., **85**, 3587 (2004)



# Nonlinear dynamics - relaxation into basins of attraction

Relaxation of the resonator driven continuously at frequency  $f_0 + \sigma$  after excitation with strong rf pulse ( $\sim 250 \mu\text{s}$  long, 18 x cw-amplitude) of same frequency with amplitude  $a(t)$  and phase  $\gamma(t)$



I. Kozinsky et al.,  
Phys. Rev. Lett. **99**, 207201 (2007)

$$u[t] = a[t] \cos[\omega t + \gamma[t]]$$

$$= I[t] \cos[\omega t] + Q[t] \sin[\omega t]$$

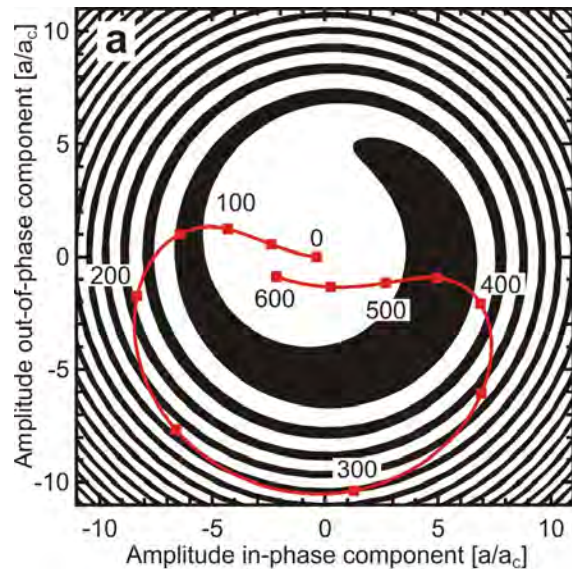
In-phase  
component

Out-of-phase  
component

Q. Unterreithmeier, T. Faust, J.P. Kotthaus,  
Phys. Rev. B **81**, 241405(RC) (2010)

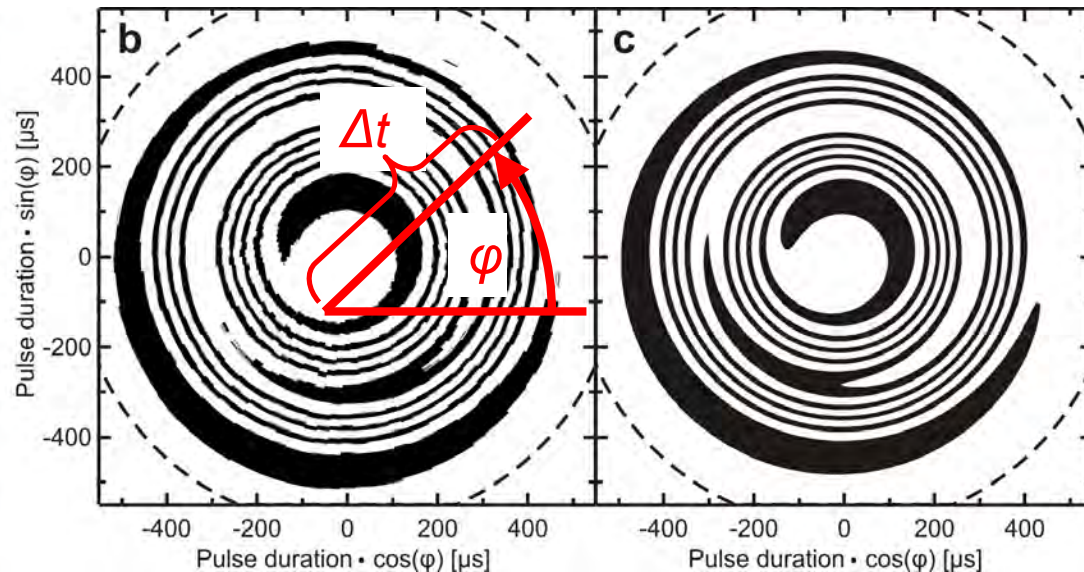


# Time evolution during application of RF pulse



Experiment

Simulation

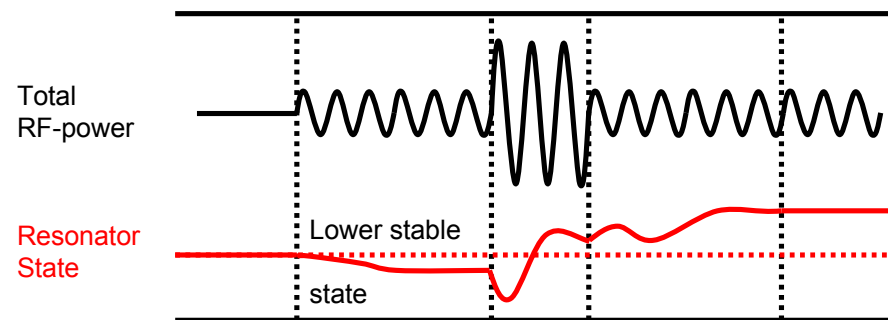


Predicted time evolution vs.  
 pulse duration  $\Delta t$  (in  $\mu s$ ) at given phase  $\phi$   
 $\Delta t$  and  $\phi$  are systematically varied

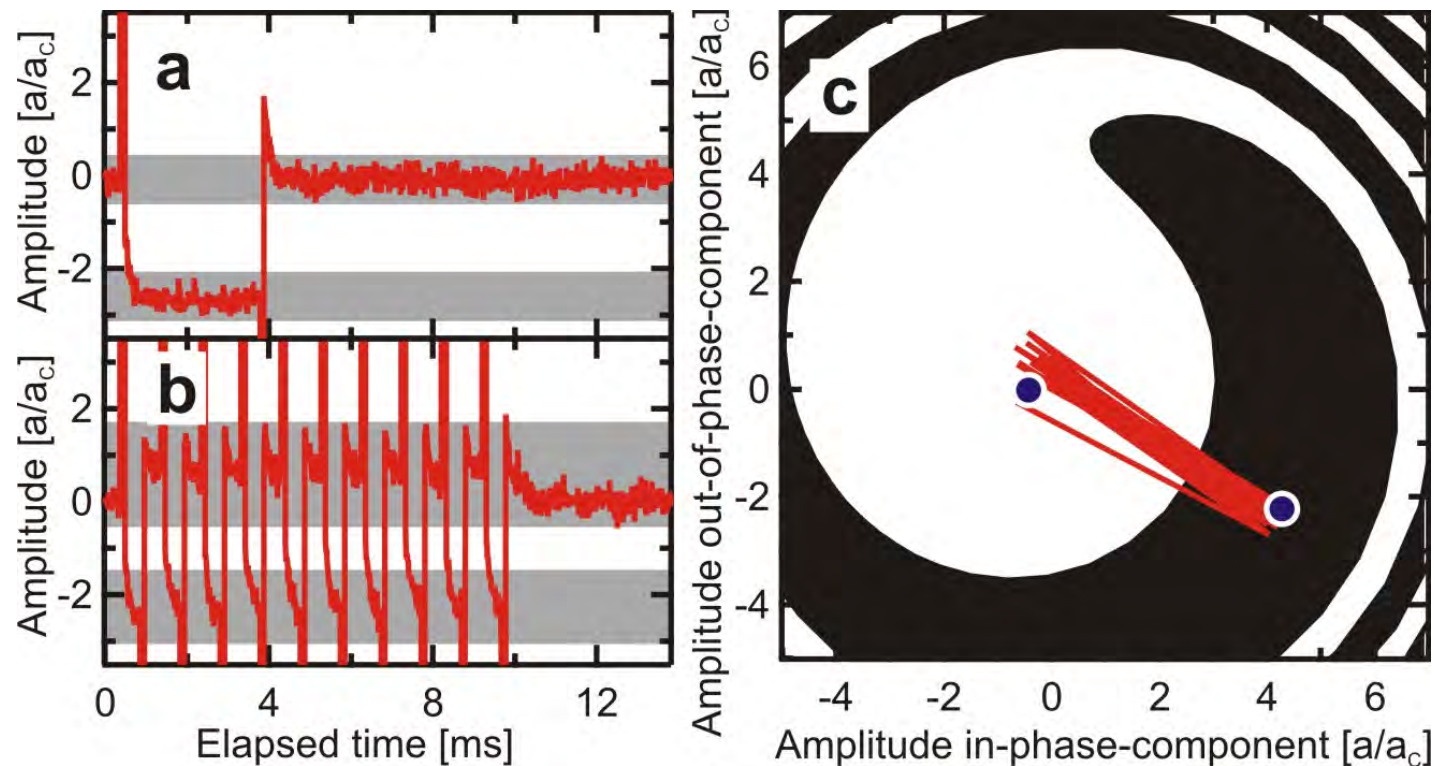
Measurement Protocol:  
 Final state vs. duration  $\Delta t$  and phase  $\phi$  of RF pulse

$$\dot{a}(t) = -\frac{2\pi f_0 a(t)}{2Q} + \frac{k \sin(\gamma(t))}{4\pi f_0}$$

$$\dot{\gamma}(t) = 2\pi\sigma - \frac{3\alpha_3 a(t)^2}{16\pi f_0} + \frac{k \cos(\gamma(t))}{4\pi f_0 a(t)}$$



# A non-adiabatically driven NEMS switch on route to a NEMS memory



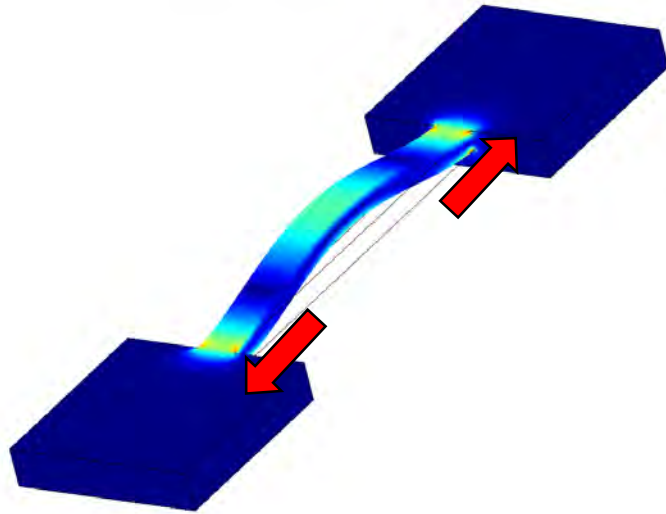
pulse duration 80  $\mu$ s and repetition rate 1kHz, resonator relaxation time  $\sim$  10 ms

-> switching beyond relaxation  
( $10^3$  speed improvement)

Q. Unterreithmeier, T. Faust, J.P. Kotthaus,  
Phys. Rev. B **81**, 241405(RC) (2010)

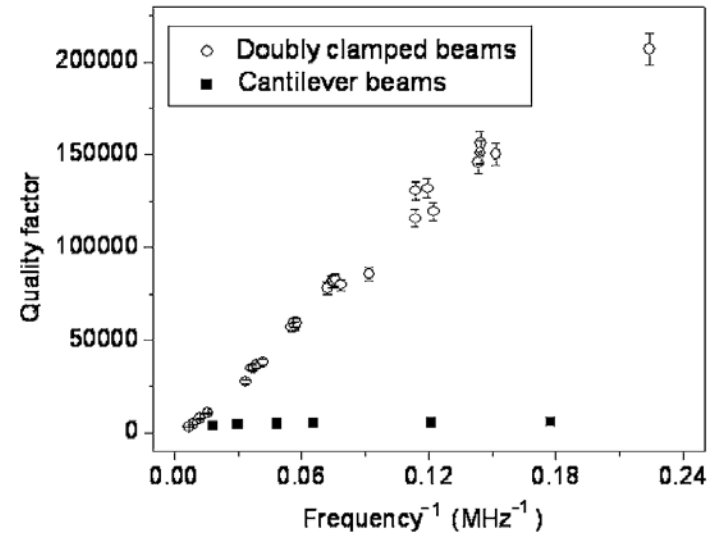


# Damping: Quality factors of highly stressed beams



Mechanical quality factor

$$Q = 2\pi \frac{\text{energy stored}}{\text{energy loss per oscillation}}$$



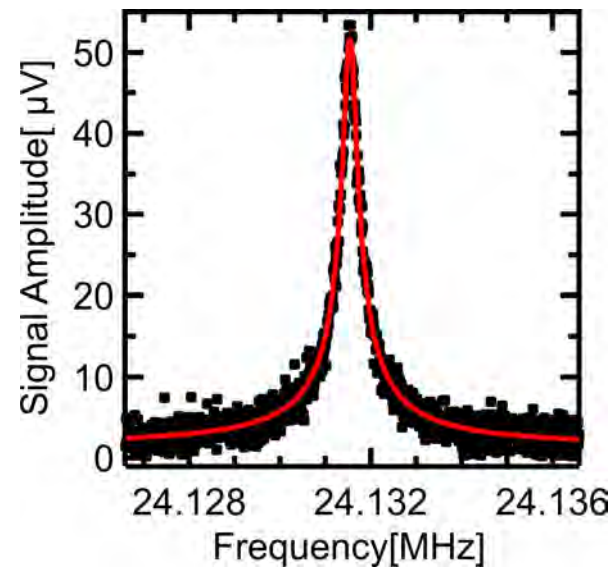
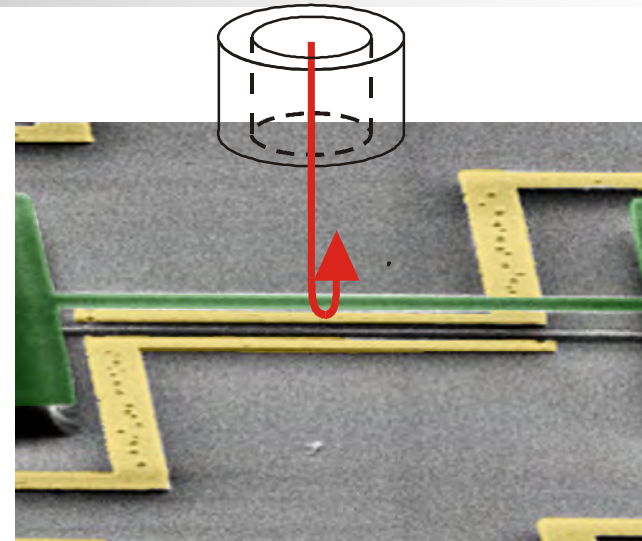
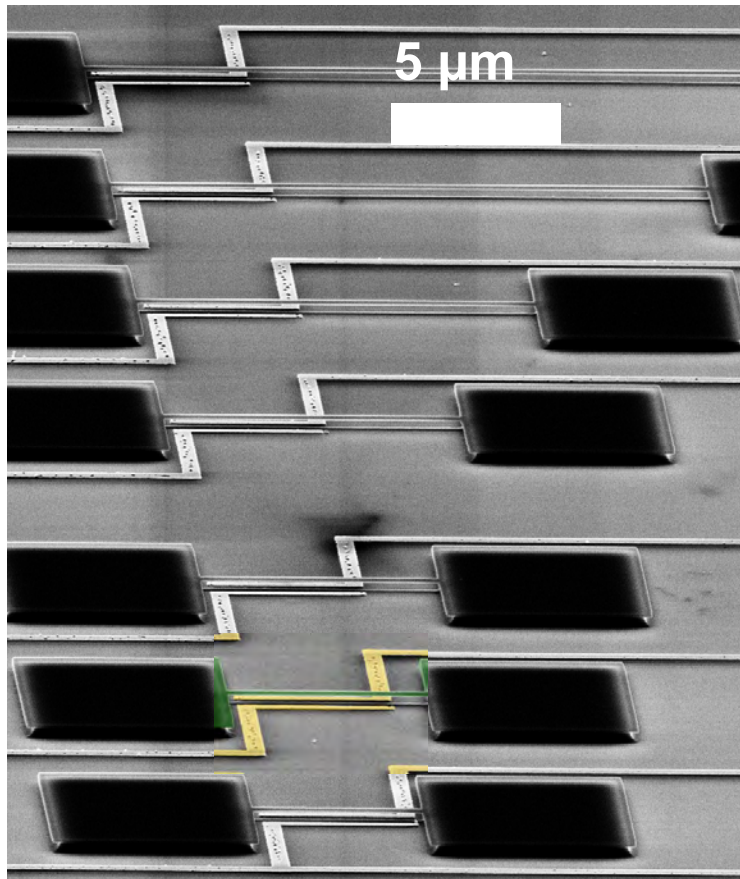
-> Stress increases Q

S. Verbride et al., J. Appl. Phys. **99**, 124304 (2006)

Mechanism?



# Exploring length and mode-dependence of Q-factor



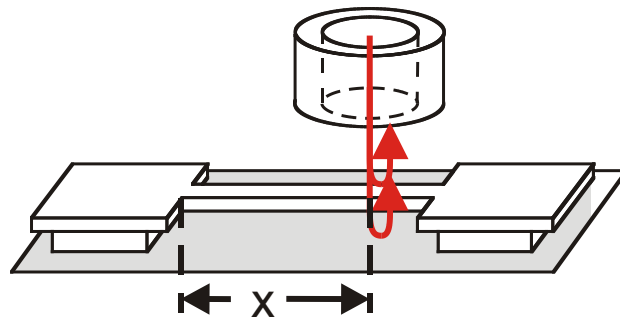
$f$ ,  $Q$  for different  
-> mode number  
-> beam length



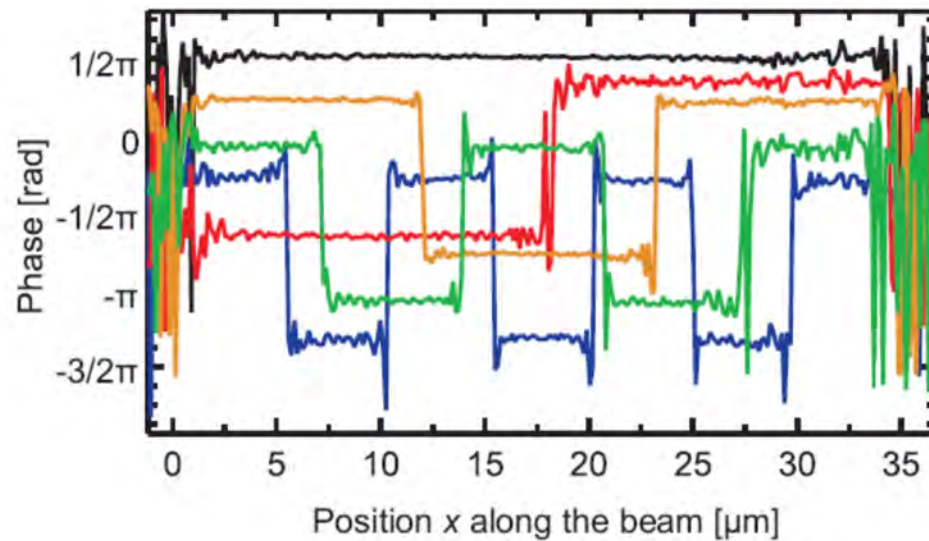


# Exploring frequency scaling and damping of harmonics

Each node of a vibrational modes yields a phase reversal:



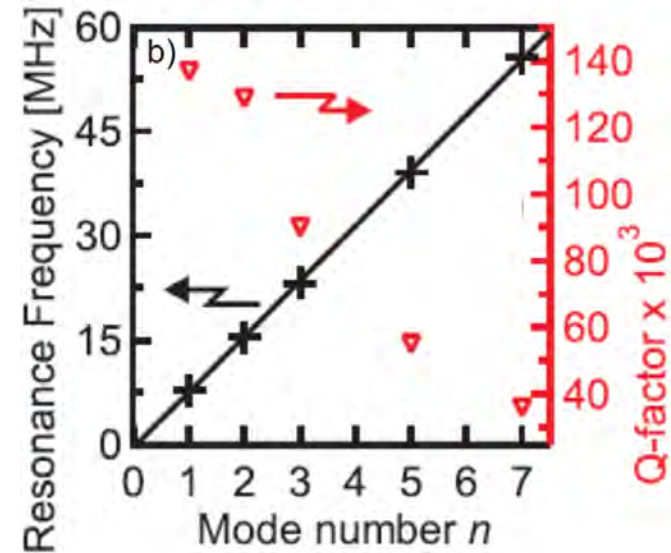
$n = 1, n = 2, n = 3, n = 5, n = 7$



- Bending rigidity:  $f \propto n^2$



- String-like:  $f \propto n$



Q. Unterreithmeier, S. Manus, J. P. Kotthaus,  
*Appl. Phys. Lett.* 94, 263104 (2009)



# Resonance frequency versus harmonic mode

$$\frac{1}{12} E h^2 \frac{\partial^4}{\partial x^4} u_n[x] - \sigma_0 \frac{\partial^2}{\partial x^2} u_n[x] - \rho (2\pi f_n)^2 u_n[x] = 0 \quad \frac{\partial}{\partial x} u_n[\pm l/2] = u_n[\pm l/2] = 0$$

Bending rigidity

Beam elongation

Rigid clamping points

Continuum mechanics with:

$u_n$ : Beam displacement

$h$ : Beam height

$\rho$ : Density

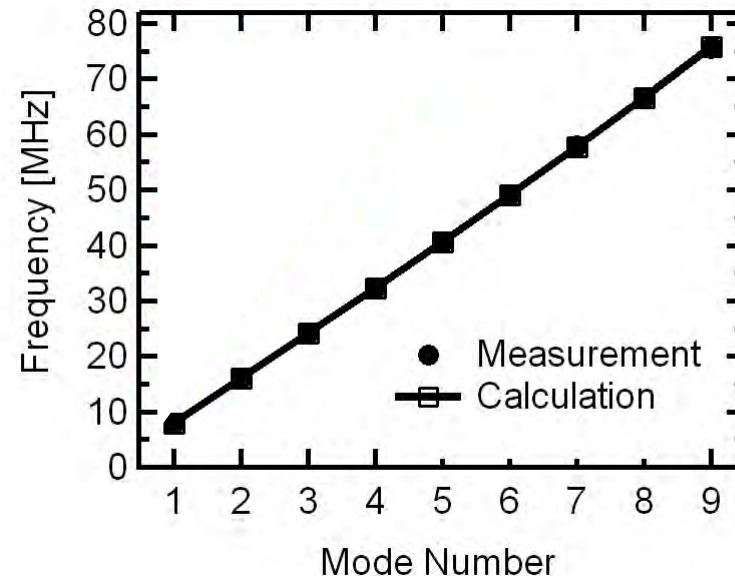
$f_n$ : Frequency (n-th Mode)

$l$ : Beam length

yields:

$E$ : Young's modulus

$\sigma_0$ : Pre-Stress



$E = 160$  GPa

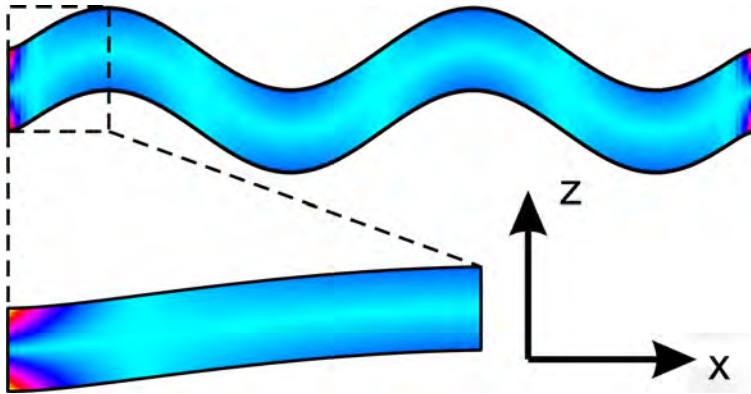
$\sigma_0 = 830$  MPa fit parameters



# A simple single parameter damping model

consistent with experimental findings

Strain caused by displacement



Strain  $\varepsilon$  and stress  $\sigma$  are out-of-phase

-> Complex Young's modulus

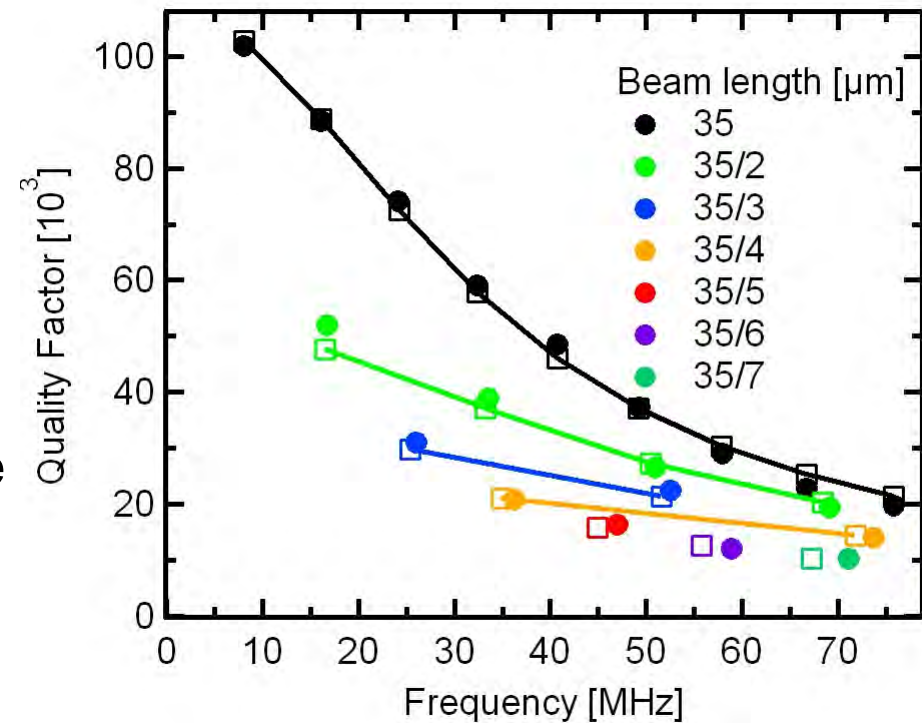
$$E = E_1 + i E_2$$

-> Energy loss per oscillation

$$\Delta U = \int_V dV \pi E_2 \varepsilon[x, z]^2$$

Assumption:

$E_2$  independent of  $x$ , mode, length



Q. Unterreithmeier, T. Faust, J. P. Kotthaus,  
Phys. Rev. Lett. 105, 027205 (2010)



# Elastic energy and mechanical quality factor vs stress

## Unstressed Beam

$$U = \int dV \frac{1}{2} E_1 \varepsilon[x,z]^2$$

$$\Delta U = \int dV \pi E_2 \varepsilon[x,z]^2 \quad Q = \frac{\text{Re}(E)}{\text{Im}(E)}$$

-> mode-independent Q

## Stressed Beam

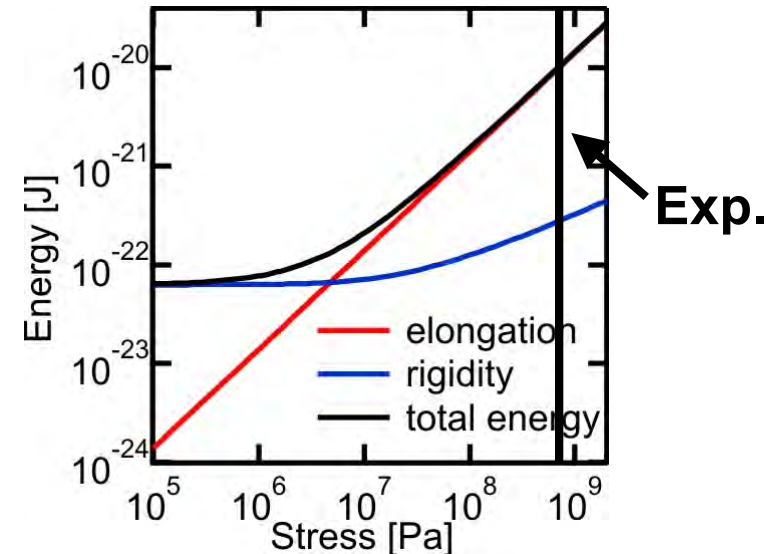
-> rigidity -> Young's modulus

-> elongation -> external stress

$$U_{\text{elongation}} = \frac{1}{2} \sigma_0 w h \int_l dx (\partial / (\partial x) u[x])^2$$

$$U_{\text{rigidity}} = \frac{1}{24} E_1 w h^3 \int_l dx (\partial^2 / (\partial x)^2 u[x])^2 \propto \Delta U$$

Q. Unterreithmeier, T. Faust, J. P. Kotthaus,  
Phys. Rev. Lett. 105, 027205 (2010)



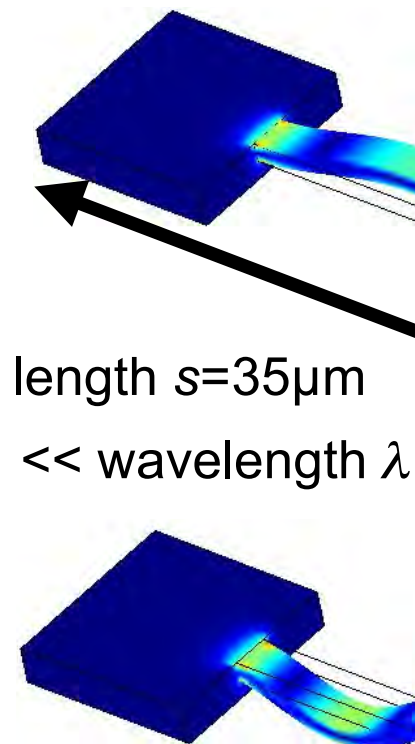
-> stress increases stored energy  
-> stress does not change local energy loss very much

**-> higher mechanical Q dominated by increased stored energy and not by reduced damping**

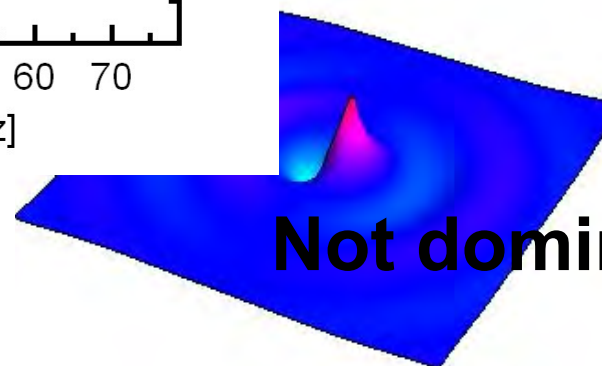
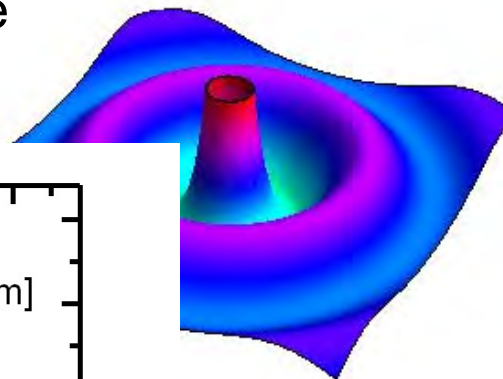
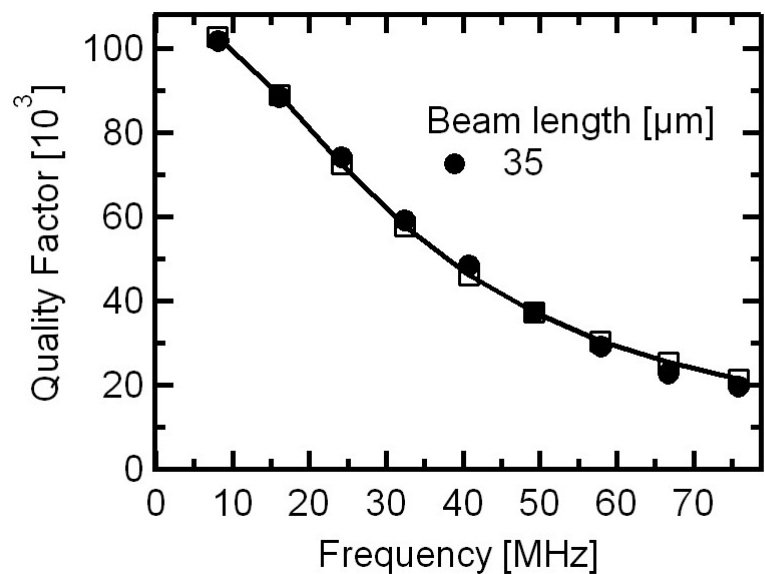


# Contribution of clamping losses to damping

Irradiation of acoustic waves into the substrate



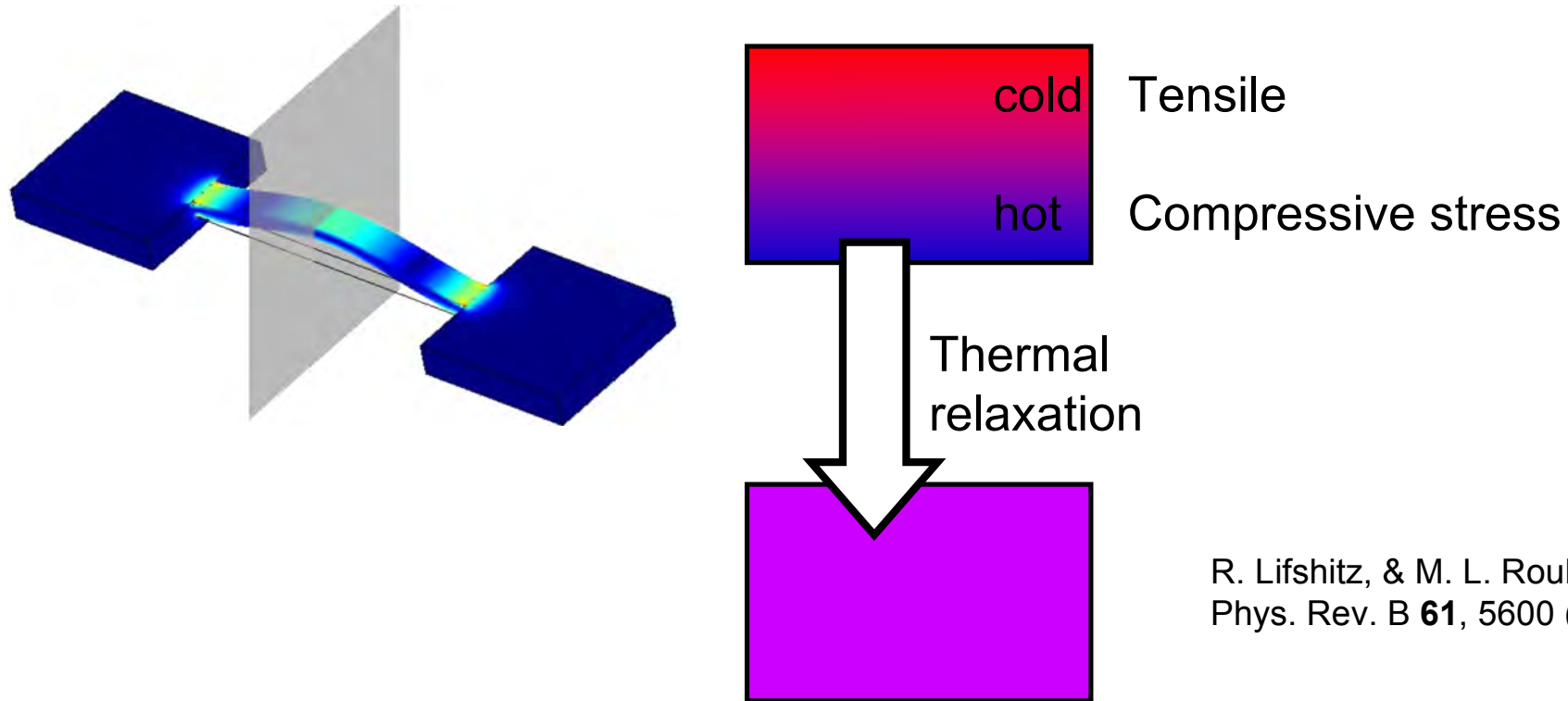
Symmetric mode  
monopole



I. Wilson-Rae,  
Phys. Rev. B77, 245418 (2008)



# Contribution of thermoeleastic damping



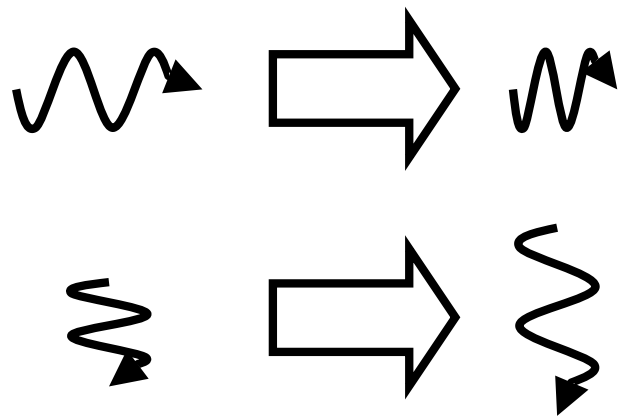
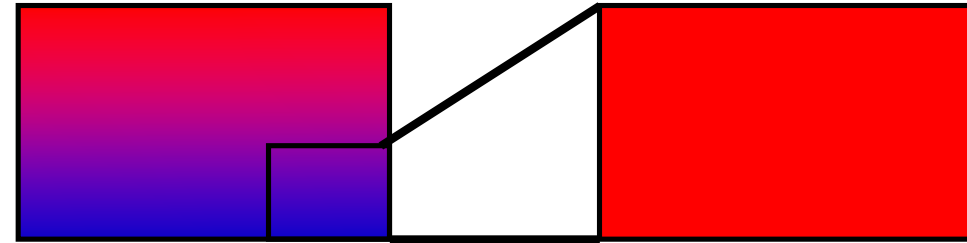
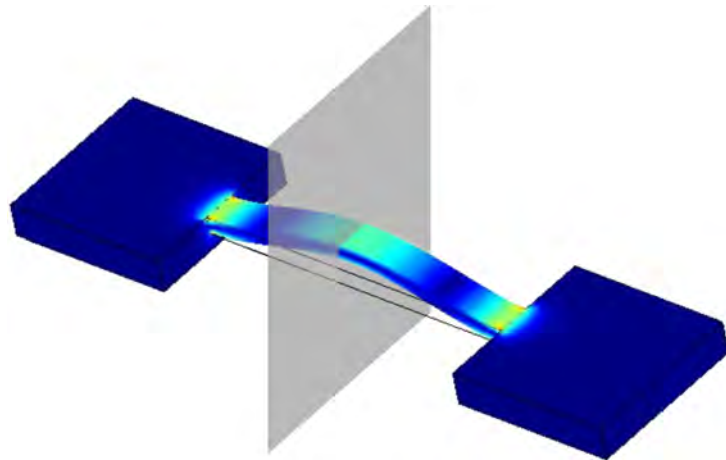
R. Lifshitz, & M. L. Roukes,  
Phys. Rev. B **61**, 5600 (2000)

- > Very small damping
- > Thermal relaxation faster than oscillation (-> frequency dependence)

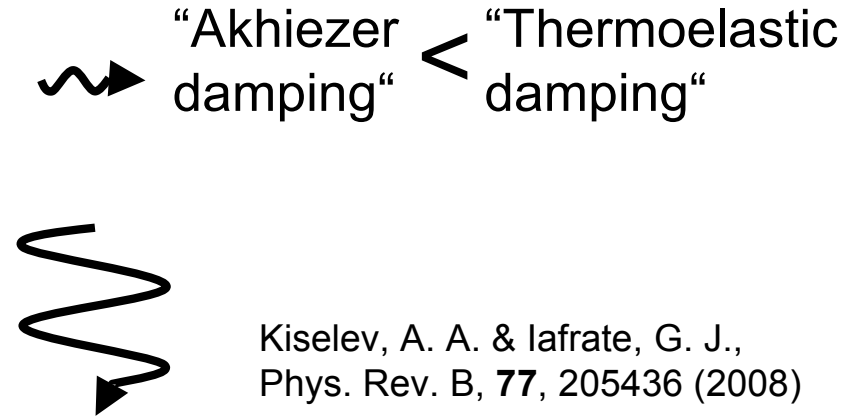
**Not dominant!**



# Contribution of the Akhiezer effect to damping



Thermal relaxation



Kiselev, A. A. & Iafrate, G. J.,  
Phys. Rev. B, **77**, 205436 (2008)

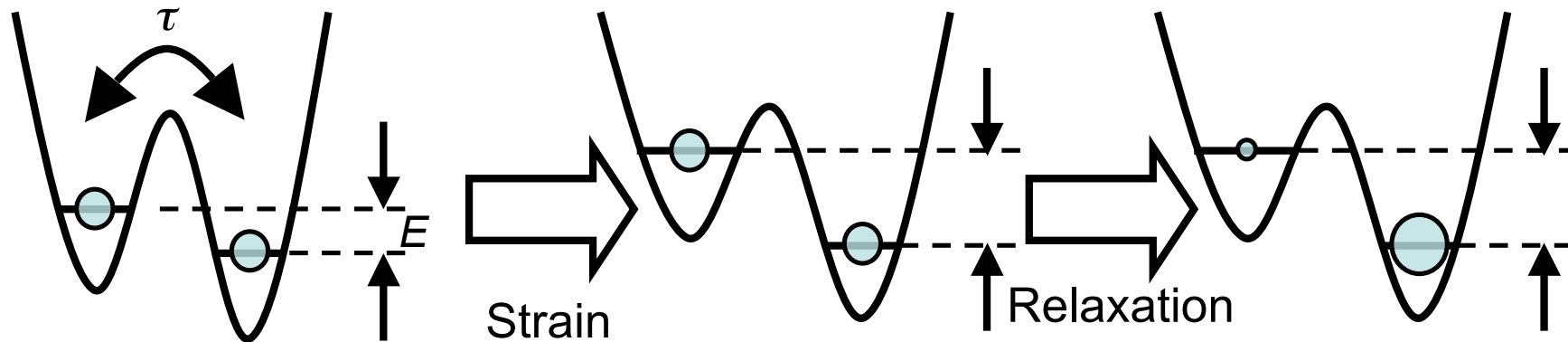
Different phonon modes are affected differently by strain  
-> each mode has different temperature

**Not dominant!**



# Damping via localized defect states

Long-wavelength oscillatory mode decays into energetically degenerate manifold of localized states



broad distribution in  $E, \tau$   
high temperature limit  
→ frequency independent energy loss

Magnitude well in the “glassy range” at “medium temperature”

**Most likely!**

D. R. Southworth et al.,  
Phys. Rev. Lett., **102**, 225503 (2009)  
R. Pohl, et al. Rev. Mod. Phys., **74**, 991 (2002)

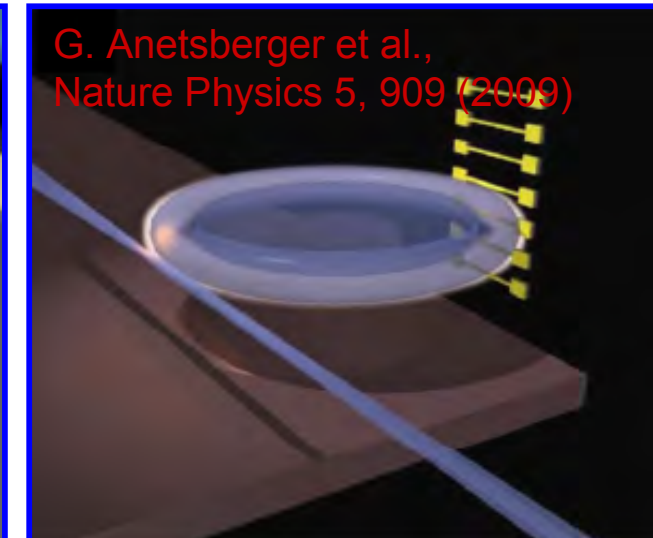
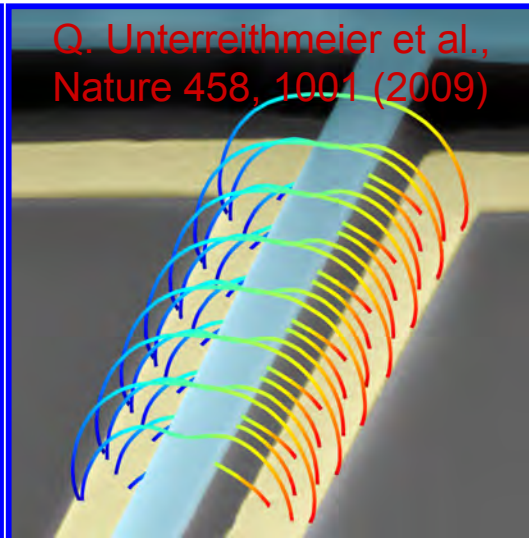
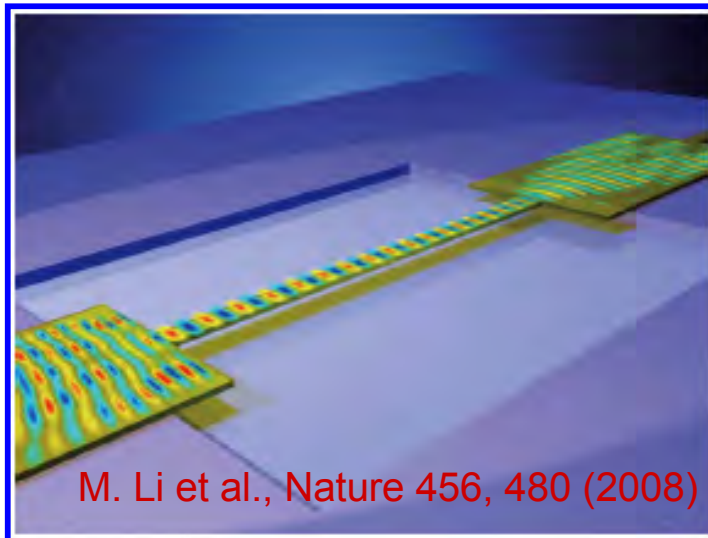
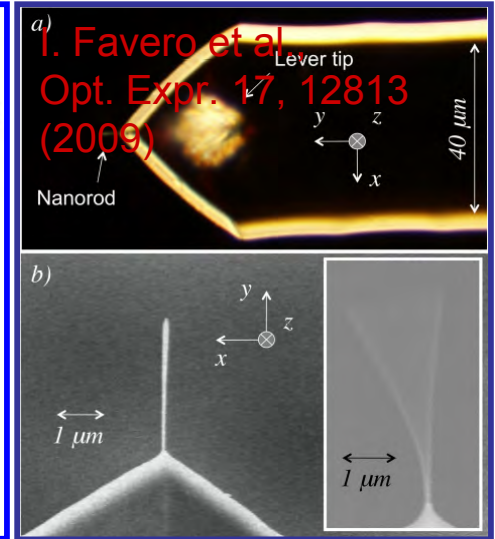
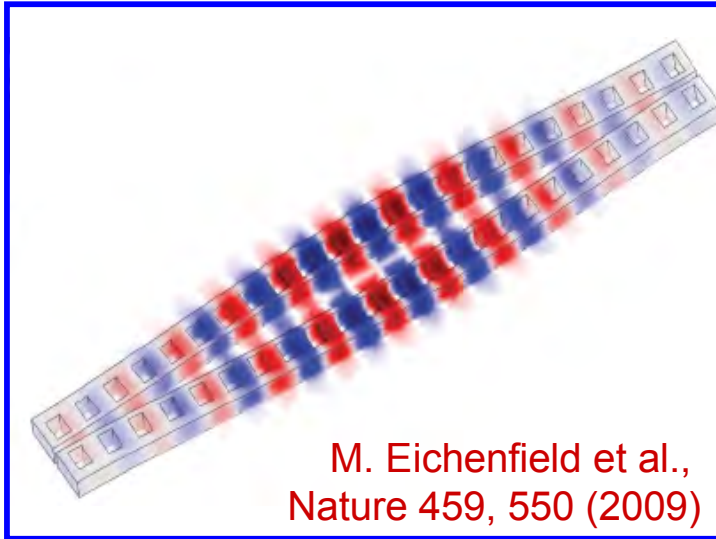
J. Jaeckle, Z. Phys. **257**, 212 (1972)





# Gradient forces in NanoOptoMechanical Systems

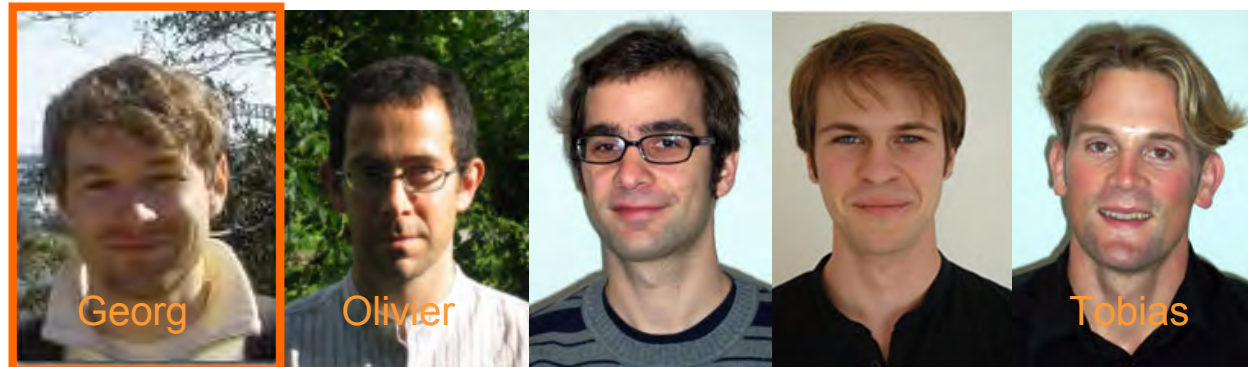
Recent examples of actuation, transduction and back-action



# Cavity - Nanomechanics via optical gradient forces

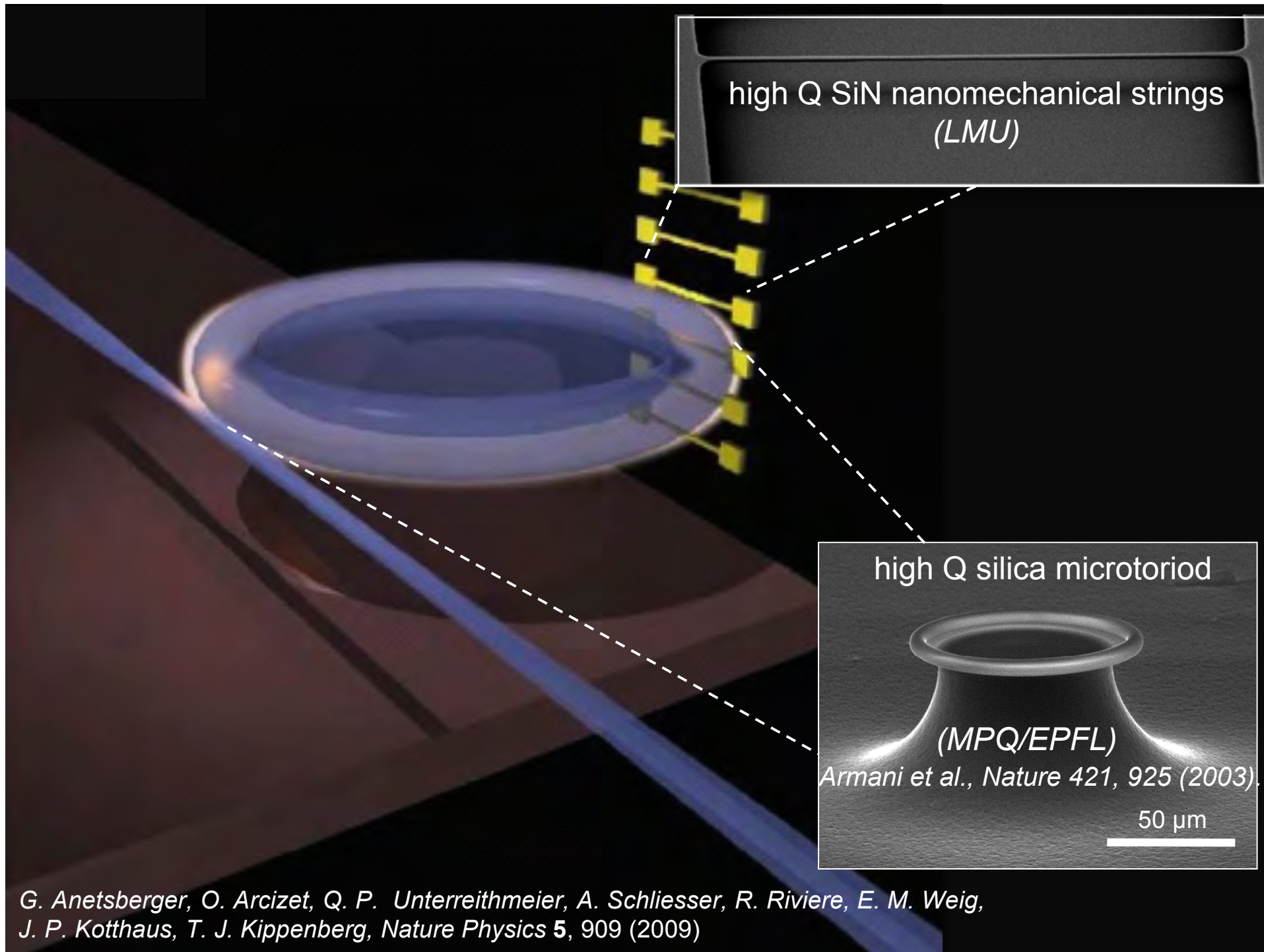
A stimulating -enabled MPQ-LMU collaboration between

The Kippenberg team: Georg Anetsberger, Oliver Arizet et al.



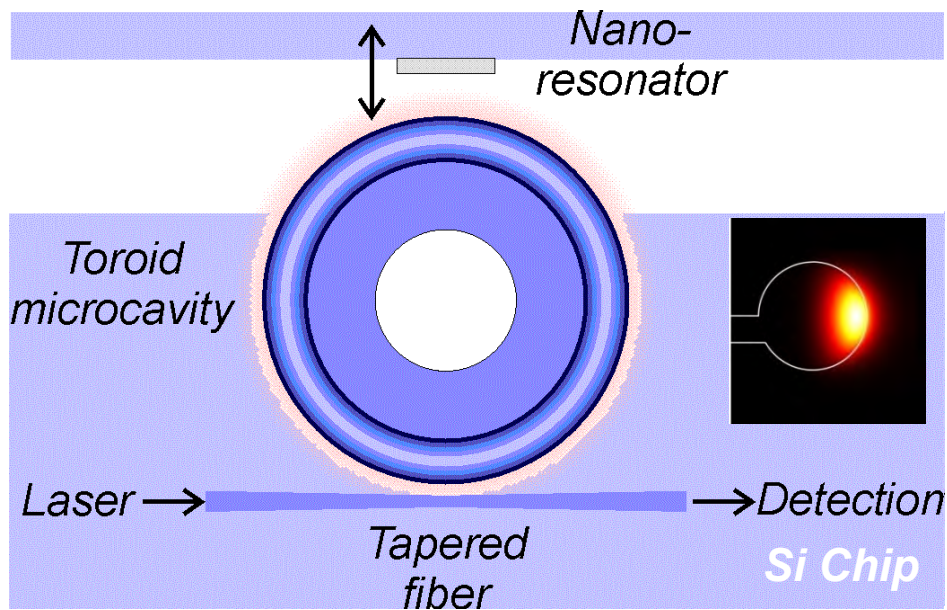
The Kotthaus team: Quirin Unterreithmeier, Eva Weig et al.





# Concept

Achieve sub-wavelength resolution using optical near-fields



*Challenges:*

Microfabrication:

- „edge cavities“

Positioning:

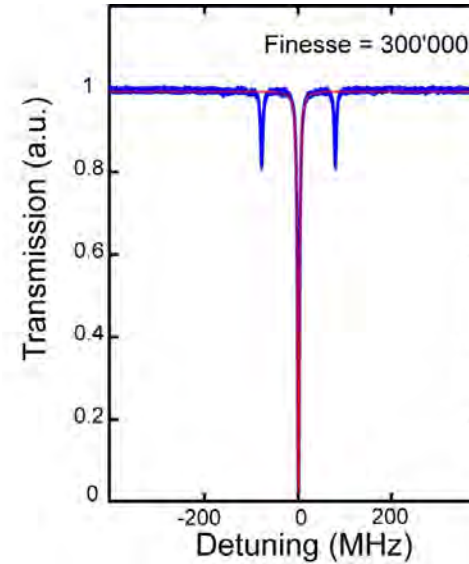
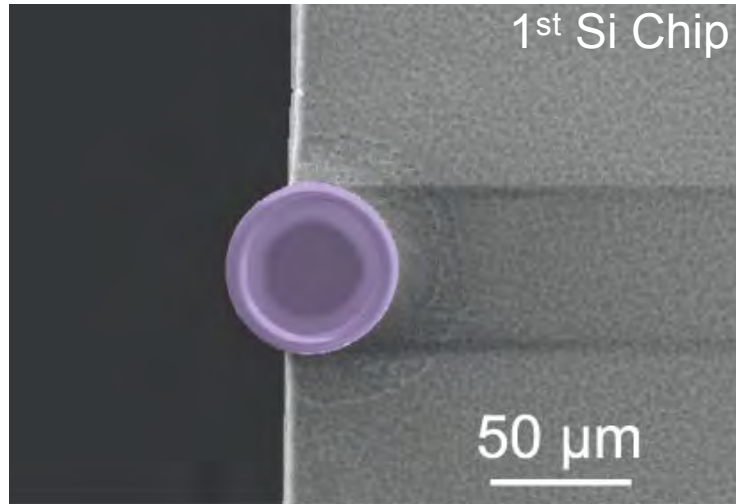
- alignment of nanoresonator chip parallel to chip  $<0.5^\circ$
- nanopositioning of fiber *and* resonator
- optical imaging

Absorption?

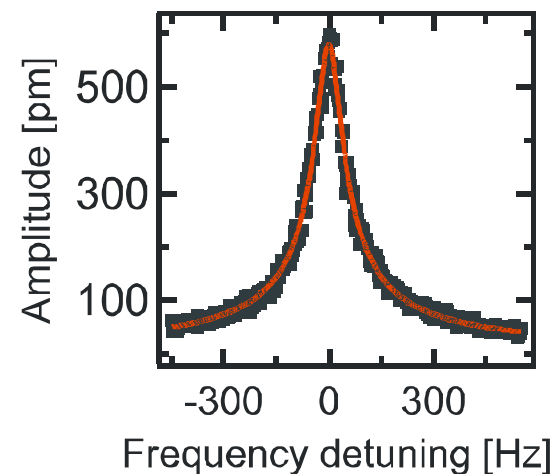
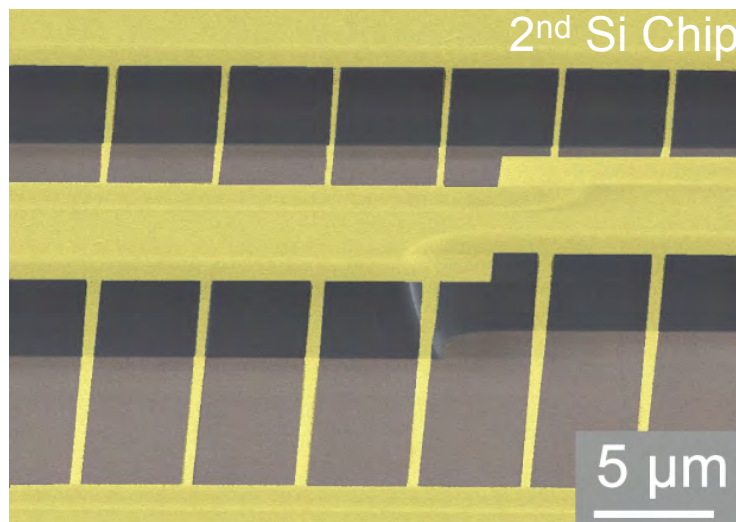


# Fabrication of high Q optical and mechanical resonators

Independent fabrication of cavity and resonator on two separate chips



Silica microtoroid



Strained SiN strings

typ.  
100nm $\times$ 500nm $\times$ 30 $\mu\text{m}$

$$\Omega_m/2\pi = 5-15 \text{ MHz}$$

$$Q_m = 10^4-10^5$$

$$m_{\text{eff}} = 0.9-5 \text{ pg}$$



# Static optomechanical coupling vs. distance

Interaction with the resonator induces a static shift in cavity frequency

Approaching the resonator in the toroid plane

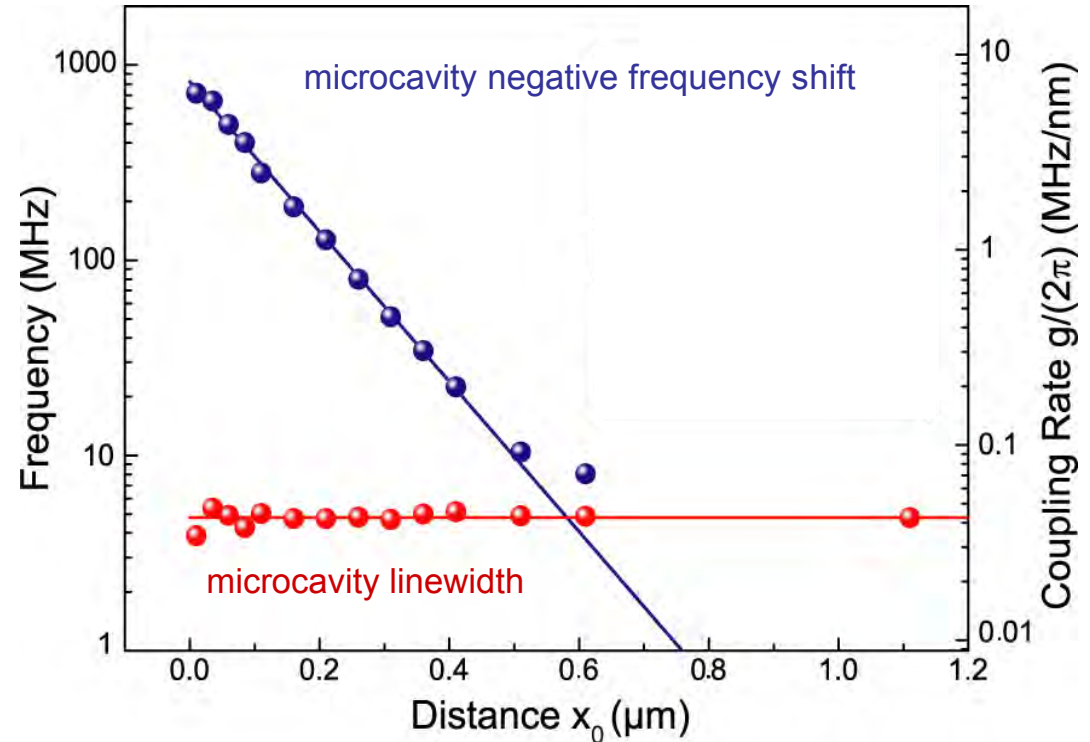
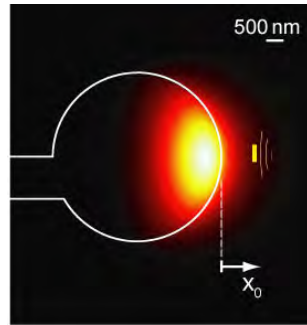
Cavity frequency shift

$$\delta\omega \propto \exp -x/x_0$$

$$\delta\omega = \underbrace{\frac{d\omega}{dx}}_{g(x_0)} \bigg|_{x_0} \delta x$$

static coupling rate:

$$g(x_0) = \frac{d\omega}{dx} \bigg|_{x_0}$$



⇒ purely dispersive coupling

⇒ optomechanical coupling rate  $g/(2\pi)$  up to 10 MHz/nm

frequency shifts up to 1 GHz obtained without degrading optical finesse



# Dynamic optomechanical coupling

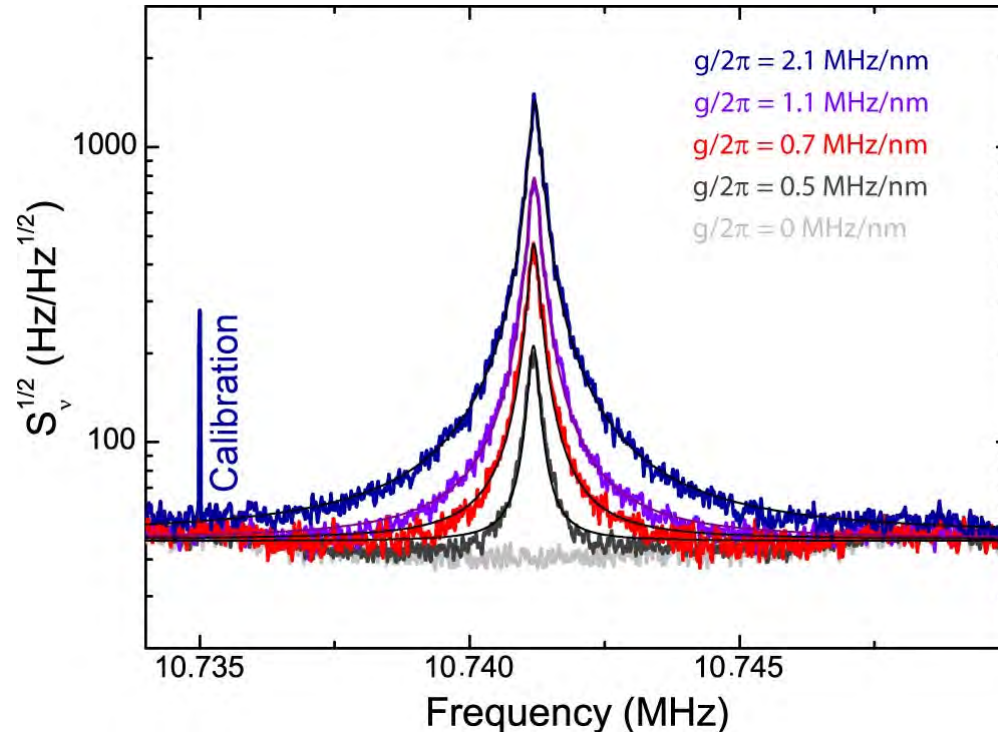
Transduction of Brownian motion of the resonator into cavity frequency noise

Brownian motion imprinted  
on cavity resonance frequency:

$$\delta\omega = \underbrace{\frac{d\omega}{dx}}_{g(x_0)} \bigg|_{x_0} \delta x$$

Dynamic measurement  
of coupling rate:

$$g(x_0) = \sqrt{\frac{S_{\omega\omega}}{S_{xx}}}$$



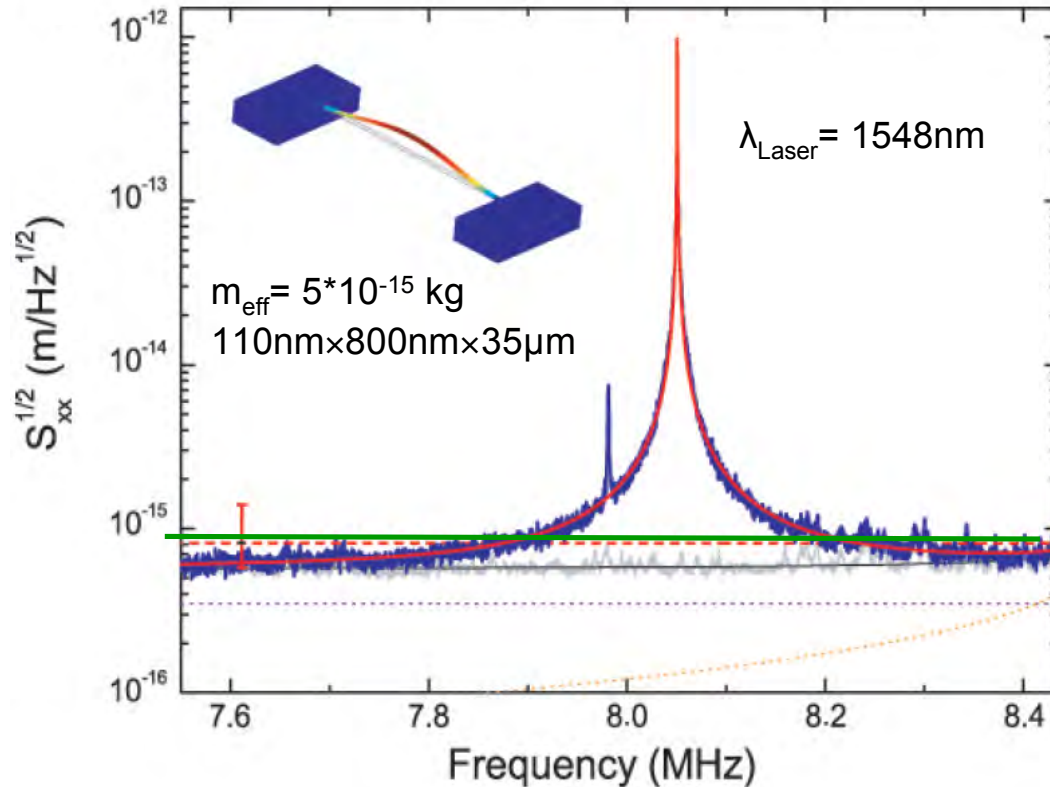
⇒ good agreement with statically determined values

⇒ dispersive coupling with optomechanical coupling rate  $g/(2\pi)$  up to 10 MHz/nm



# Quantum limited displacement sensitivity

with sub-femtometer resolution of a nanomechanical resonator at room temperature



$$\langle x(t)^2 \rangle_{\text{SQL}} = \frac{\hbar}{2m\Omega_m}$$

$$\sqrt{S_{xx}^{\text{SQL}}} = \frac{2\hbar Q}{m\Omega_m^2}$$

Standard quantum limit:

$$\sqrt{S_{xx}^{\text{SQL}}} = 820 \text{ am/Hz}^{1/2}$$

Displacement imprecision:

$$\sqrt{S_{xx}^{\text{exp}}} = 570 \text{ am/Hz}^{1/2} \text{ at } 65 \mu\text{W}$$

Laser shot noise:

$$\sqrt{S_{xx}^{\text{shot}}} = 350 \text{ am/Hz}^{1/2}$$

⇒ state of the art in nanomechanical displacement sensing:

room temperature:	300 fm/Hz <sup>1/2</sup>	interferometric	[N. O. Azak et al., APL 91, 093112 (2007)]
	50 am/Hz <sup>1/2</sup>	photonic crystal	[M.Eichenfield et al., Nature 459, 550 (2009)]
quantum limited:	5 fm/Hz <sup>1/2</sup>	supercond. circuit	[J.D.Teufel et al., Nat. Nanotech.4, 820 (2009)]

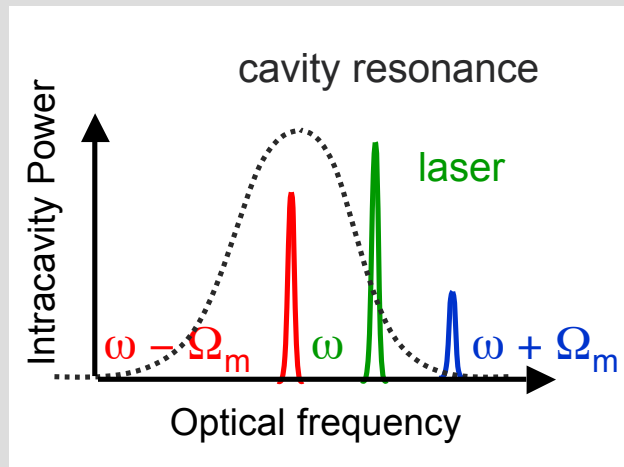




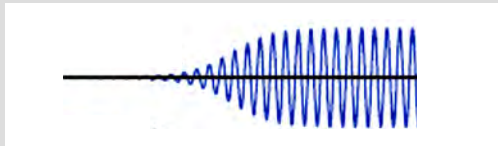
# Dynamical back action on nanomechanical resonators

via the radiation-pressure-induced optical dipole force

## Blue detuned laser

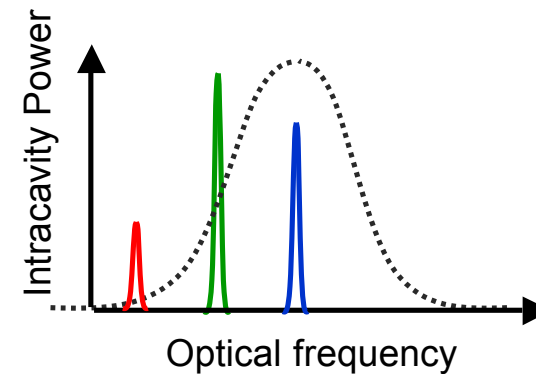


- Stokes processes dominate, net energy transfer from cavity to resonator
- Optomechanical driving



Resolved sideband regime:  
 $\Omega_m \gtrsim \kappa$

## Red detuned laser



- Anti-Stokes processes dominate, net energy transfer from resonator to cavity
- Optomechanical cooling



# Dynamical back action on the nanomechanical resonator

## Radiation-pressure-induced coherent self-oscillation



Linewidth narrowing:

- Net energy increase corresponds to reduced damping

$$\Gamma = \Gamma_m + \Gamma_{ba} \quad \text{with} \quad \Gamma_{ba} \propto -g^2 \cdot P_{in}$$



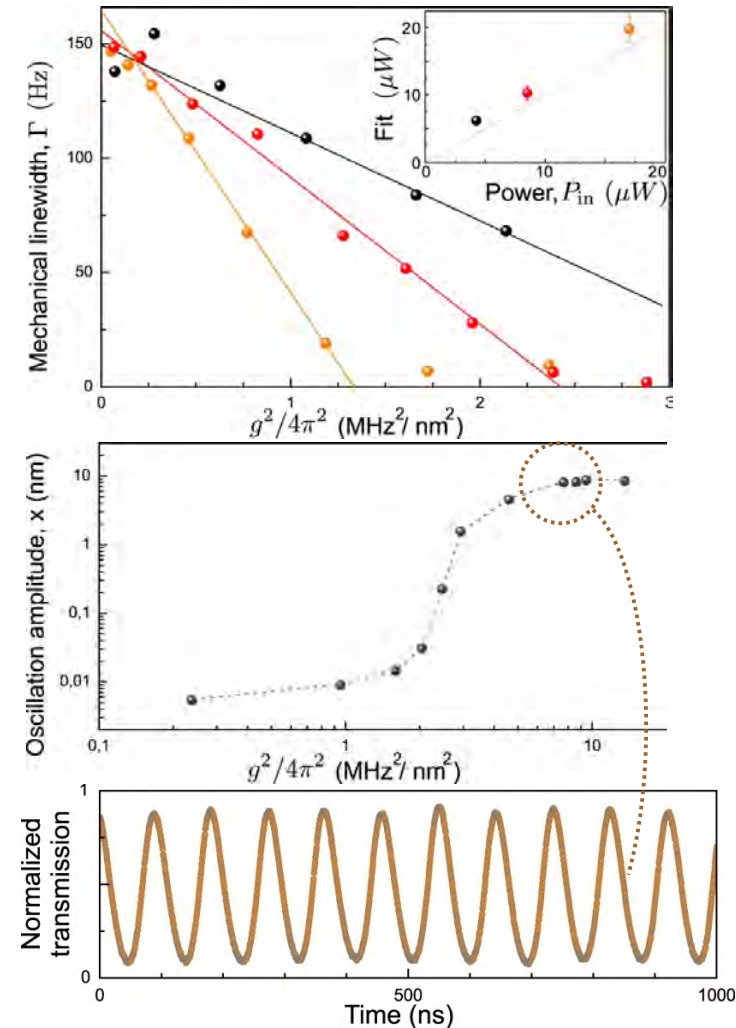
Oscillation threshold and saturation:

- Zero damping at threshold

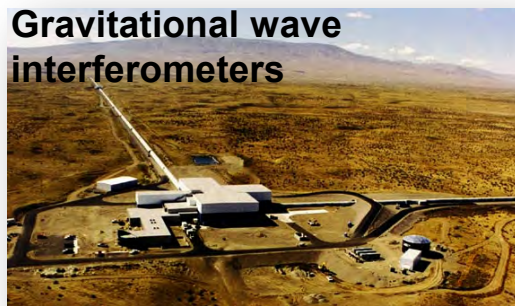
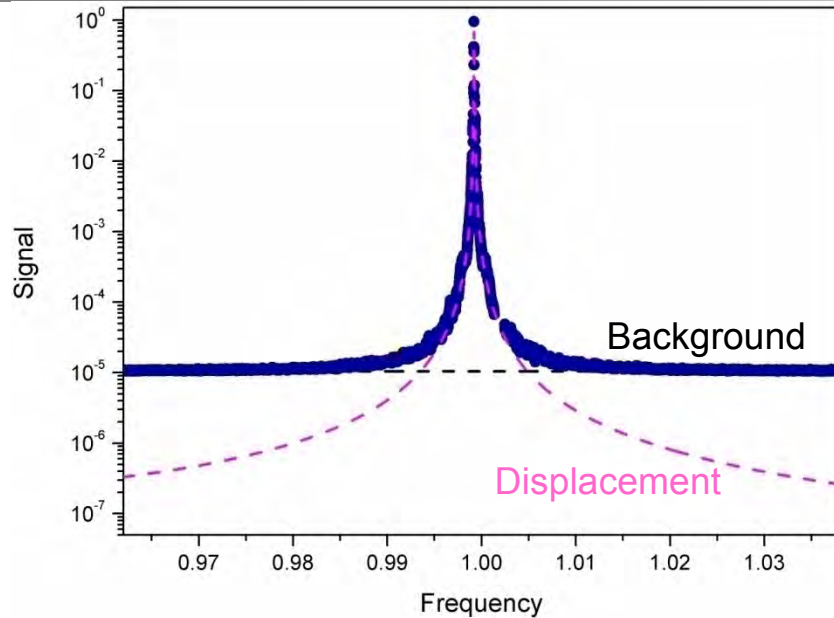


Coherent oscillation:

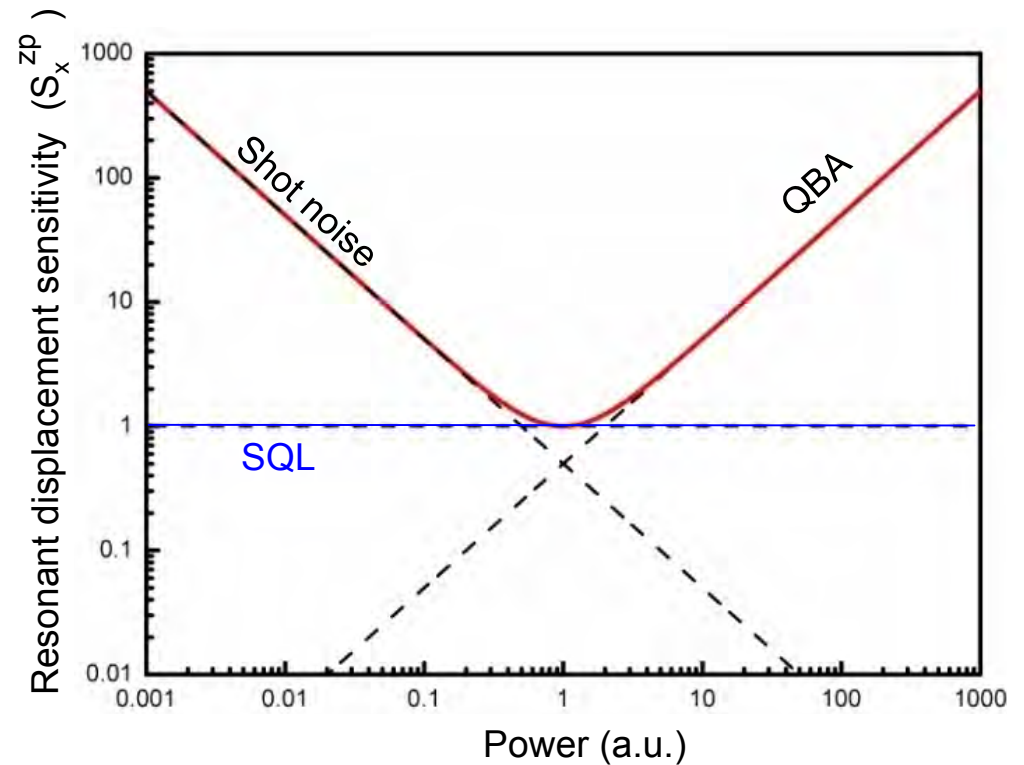
- Radiation pressure induced self-oscillation



# Quantum limits for continuous position measurement



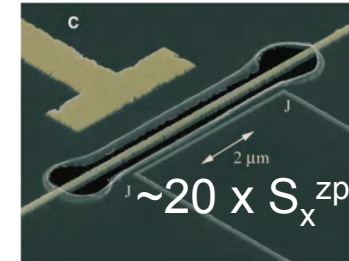
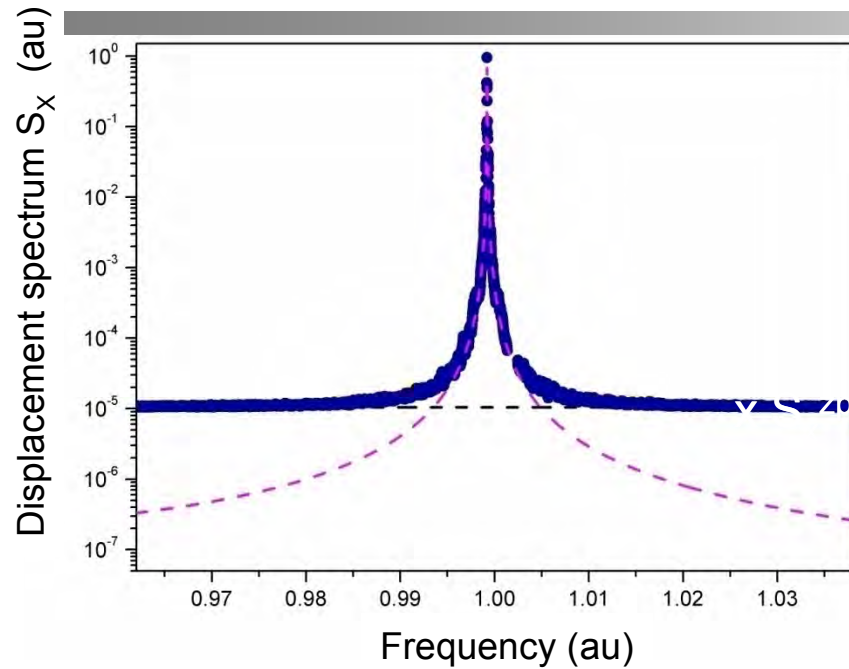
Caves, Phys.Rev. D, 23, 1693 (1981).  
Tittonen et al. PRA, 59, 1038 (1999).



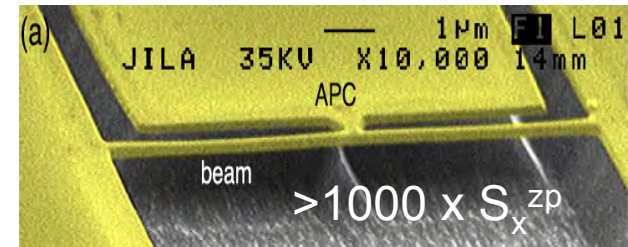
- So far only transducers based on optical cavities are close to shot-noise limit
- Not directly applicable to nanomechanical oscillators due to diffraction



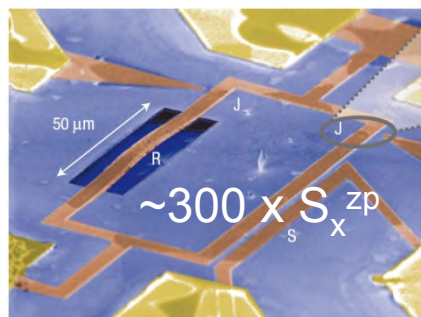
# Recent transducers sensitivities for nanomechanical motion



M. D. LaHaye et al., Science, **304**, 74 (2004)

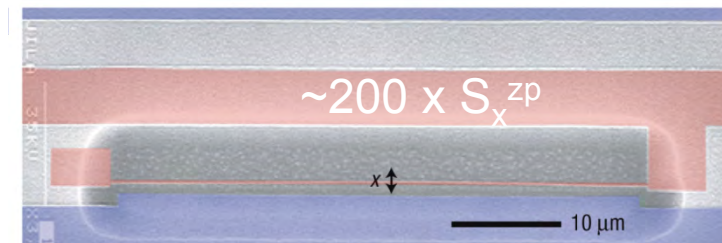


N. E. Flowers-Jacobs, PRL **98**, 096804 (2007)



S. Etaki et al., Nature Physics **4**, 785 (2008)

## Microwave cavity



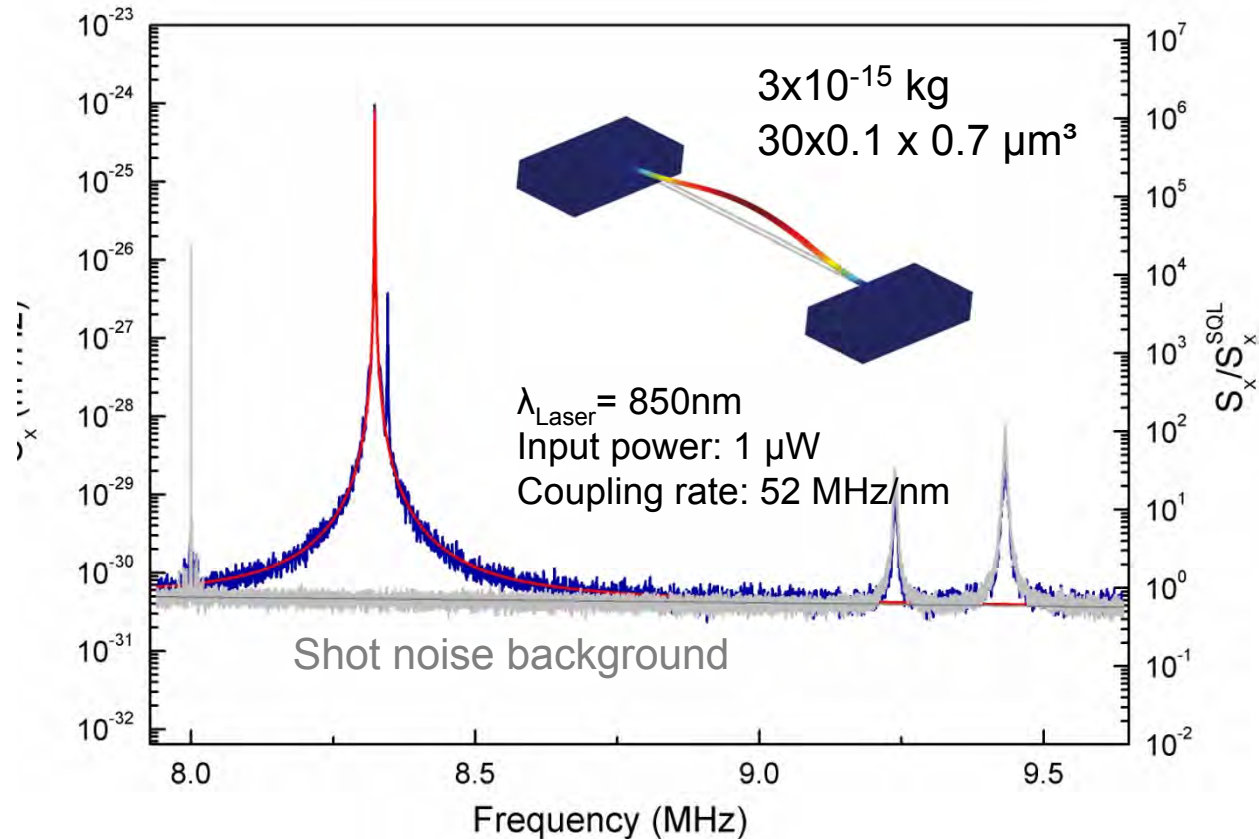
C. A. Regal et al., Nature Physics, **4**, 555 (2008)



Imprecision larger than zero-point motion



# Imprecision below the SQL



Shot noise limited imprecision:

$$(600 \text{ am}/\sqrt{\text{Hz}})^2$$

0.5 x SQL

300 K optical measurement of displacement with an imprecision of 0.5xSQL, expected to go below 0.1xSQL at  $T < 30\text{K}$ , as limited by thermorefractive noise at 300 K

G. Anetsberger et al., submitted

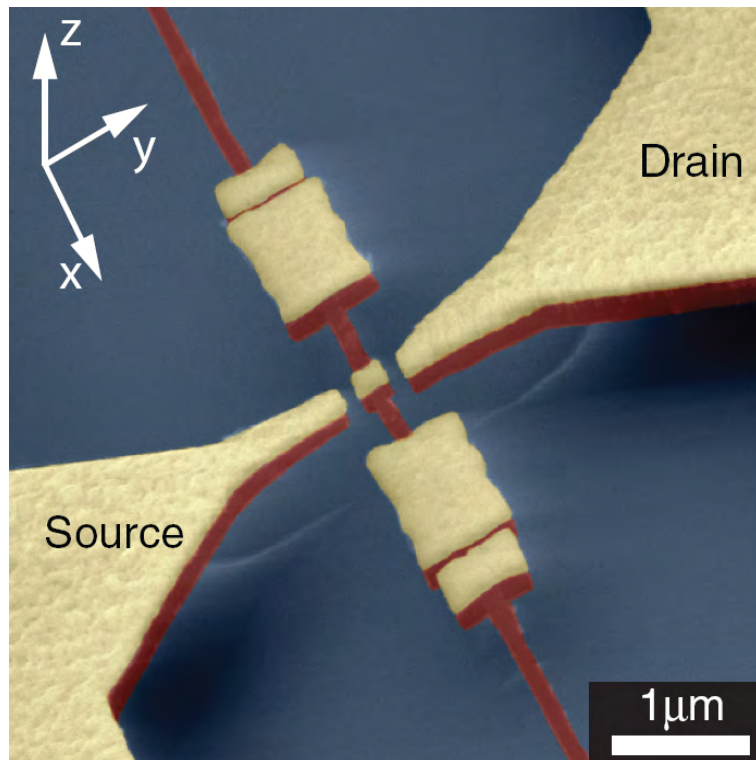
Optically achieved 300 K-value comparable to imprecision of 0.4' SQL recently

measured with microwave cavity at 130m mK  
 Opens route to explore quantum back-action and back-action evading techniques

J. D. Teufel et al., Nature Nanotechnology 4, 820 (2009)



# Nanomechanical charge transport

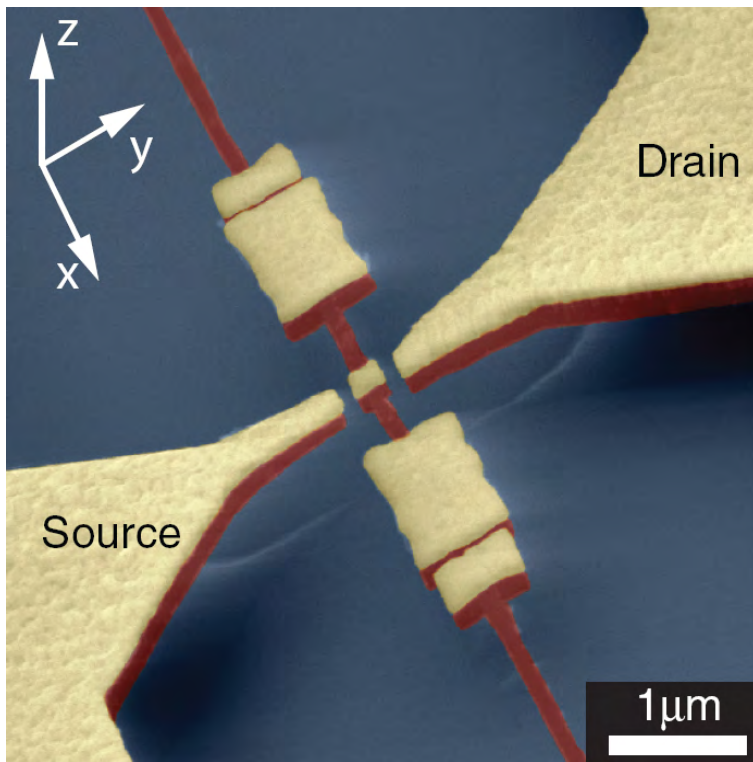


in collaboration with  
Daniel König and Eva Maria Weig



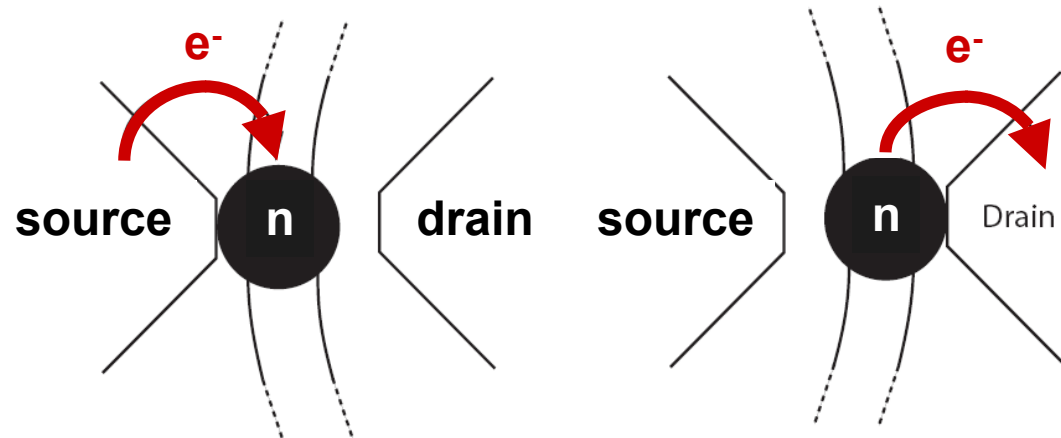
# A Nanomechanical charge shuttle

The concept of nanomechanical (single) electron transport



Mechanical actuation of an electrical current:

$$\bar{I}_{sd} = 2 \cdot \bar{n} \cdot e \cdot f$$



as theoretically proposed by

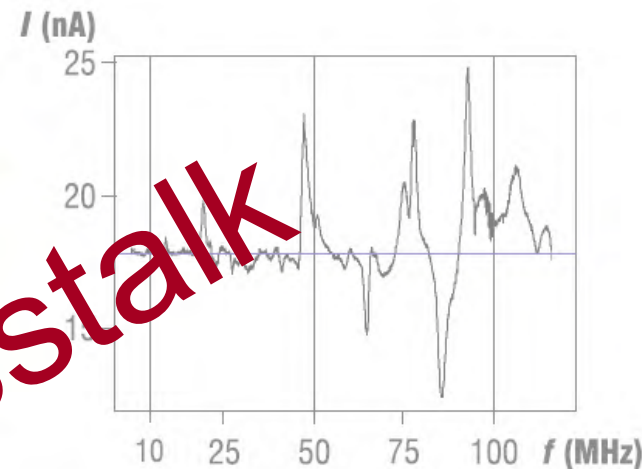
*L. Y. Gorelik et al., PRL 80, 4526 (1998)*



# A short history of shuttles

The quest of finding the right actuation mechanism to enter the Coulomb blockade regime

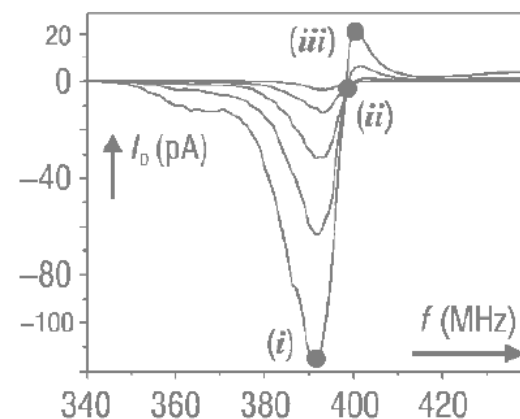
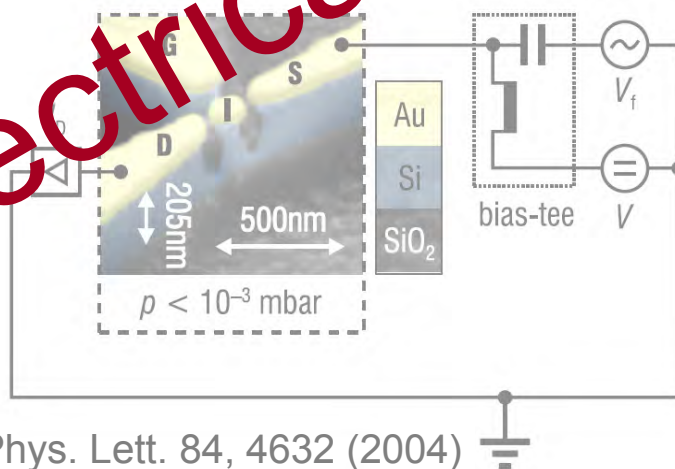
ac drive via auxilliary gates:



A. Erbe et al., Phys. Rev. Lett. 89, 096106 (2001)  
 or: D. Scheible et al., NJP 12, 023019 (2010)

electrical crosstalk

direct ac drive:



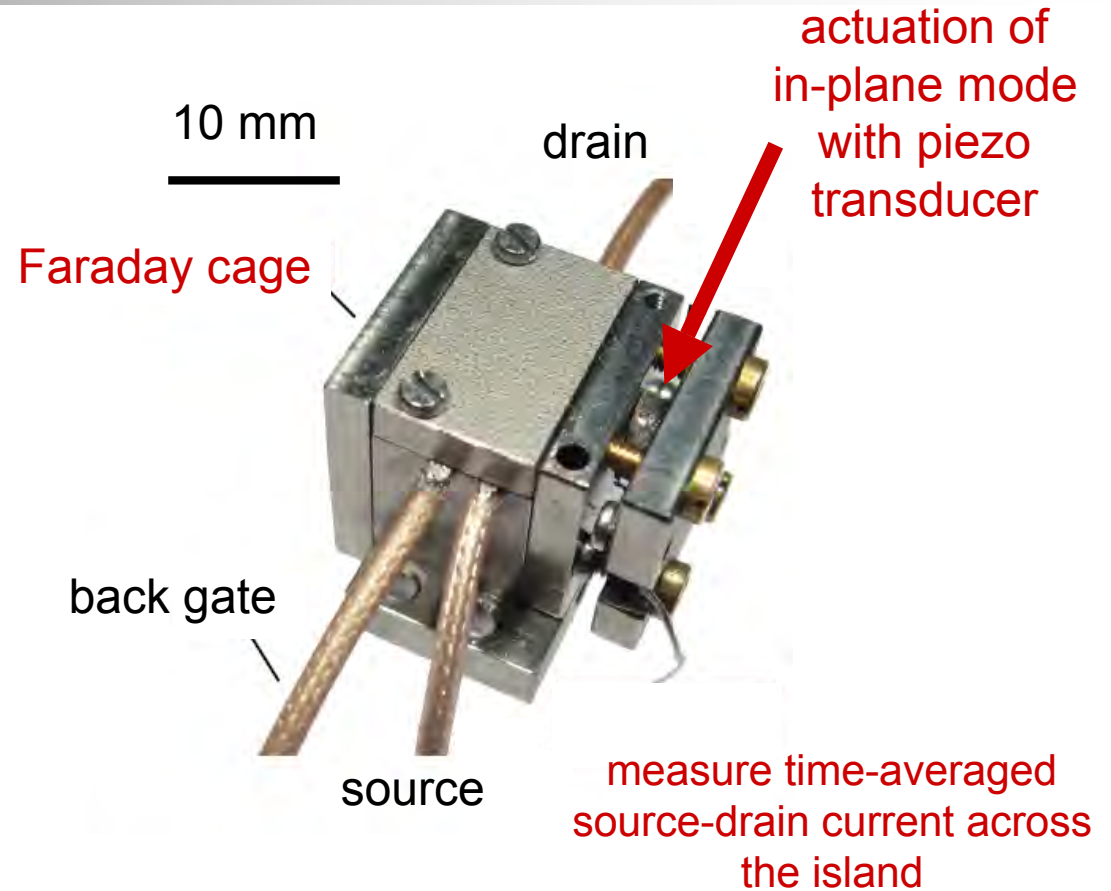
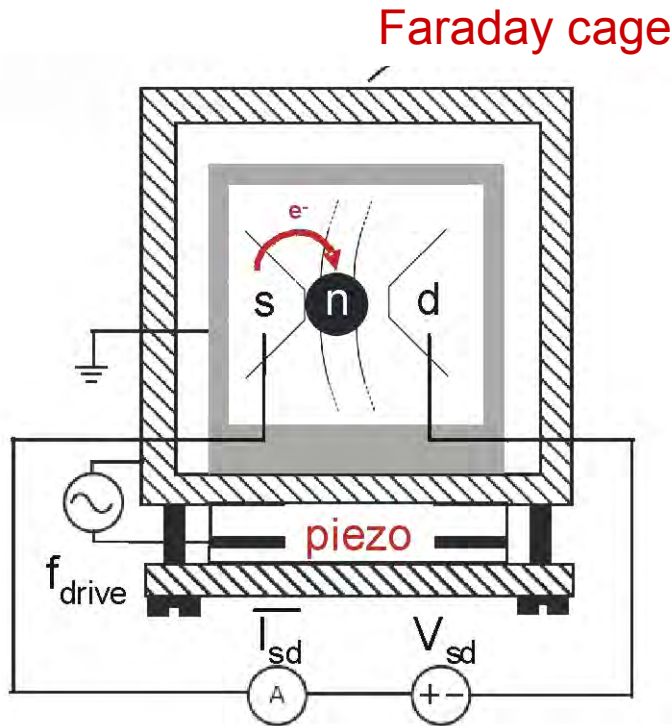
D. Scheible et al., Appl. Phys. Lett. 84, 4632 (2004)





# Inertial actuation of the shuttle

using acoustic waves produced by a piezo transducer shielded by a Faraday cage



Faraday cage ensures complete decoupling from the drive signal

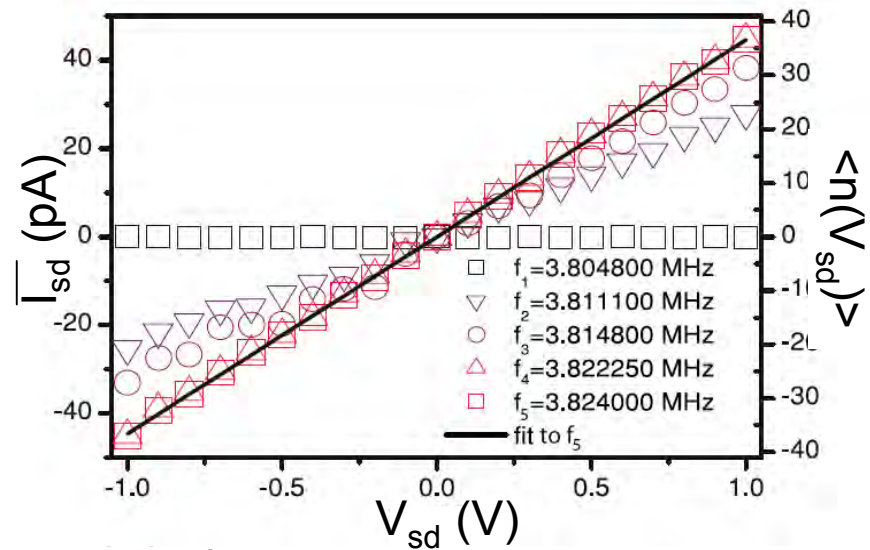
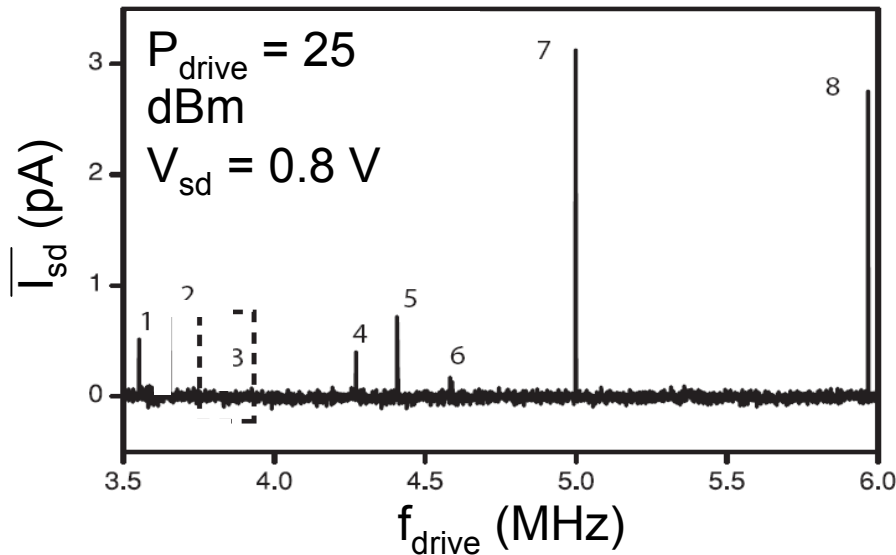
König, Weig, Kotthaus, *Nature Nanotechnology* 3, 482 (2008)



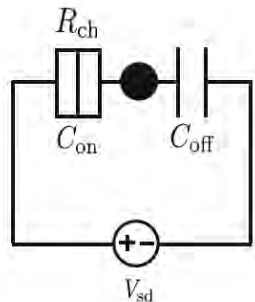
# Transport characterization of individual shuttles

Not all shuttles display stable mechanical trajectories giving rise to charge transport

Piezo-driven electron shuttling at  $T = 20$  K:



**model:** single electron box



*high-temperature regime*

$$\Rightarrow C_{\text{off}} = 5.94 \text{ aF}$$

no transport (off-resonant)

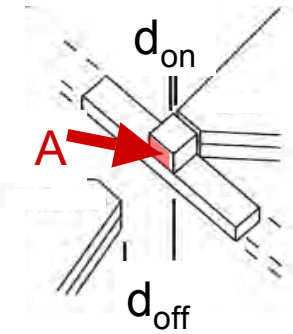
subharmonic / irregular dynamics:  
transport mechanically limited

$2\pi$ -periodic dynamics:  
transport capacitively limited

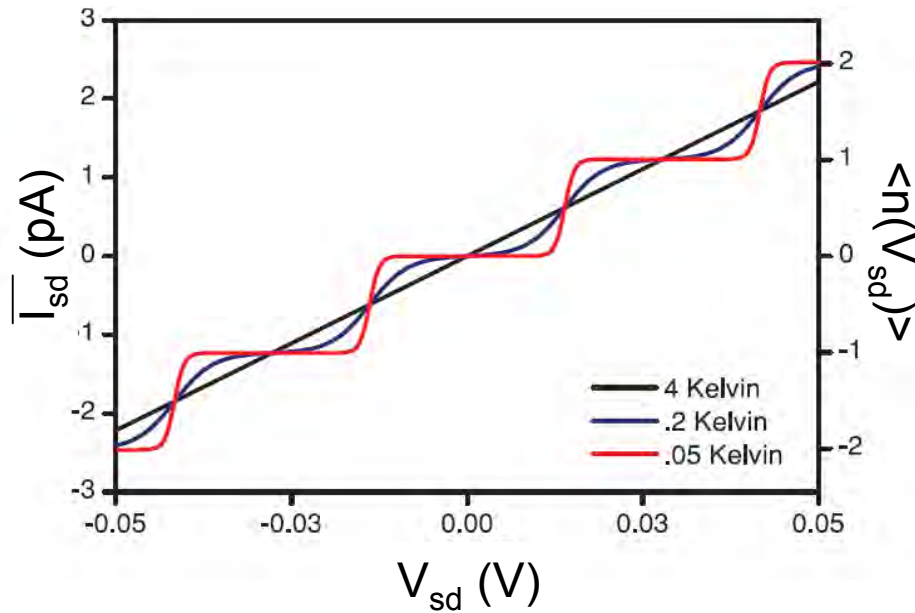


# A mechanical *single* electron shuttle?

Prerequisites for entering the Coulomb blockade regime



island cross section area  
 $A = 140 \text{ nm} \times 60 \text{ nm}$



Coulomb blockade at 200 mK

“Coulomb blockade”

fixed electron number on the island:  
 thermal energy must not exceed the  
 charging energy

$$k_B T \ll e^2/2C_\Sigma$$

lower temperatures

larger charging energy

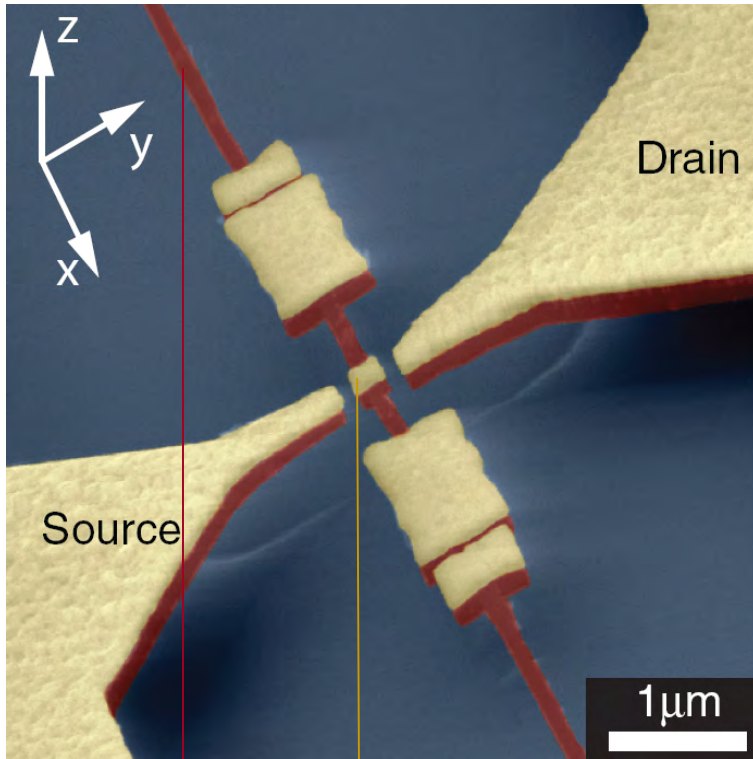
non-dissipative  
 actuation scheme

smaller island



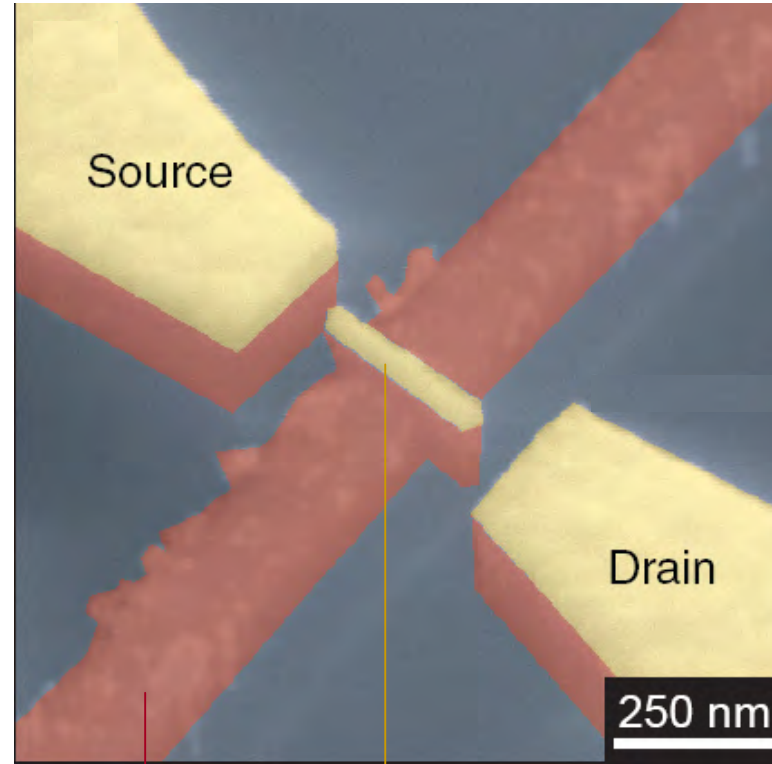
# Nanomechanical charge shuttle

The concept of nanomechanical (single) electron transport



island:  
170 nm x 140 nm x 60 nm

resonator:  
14 μm x 70 nm x 110 nm



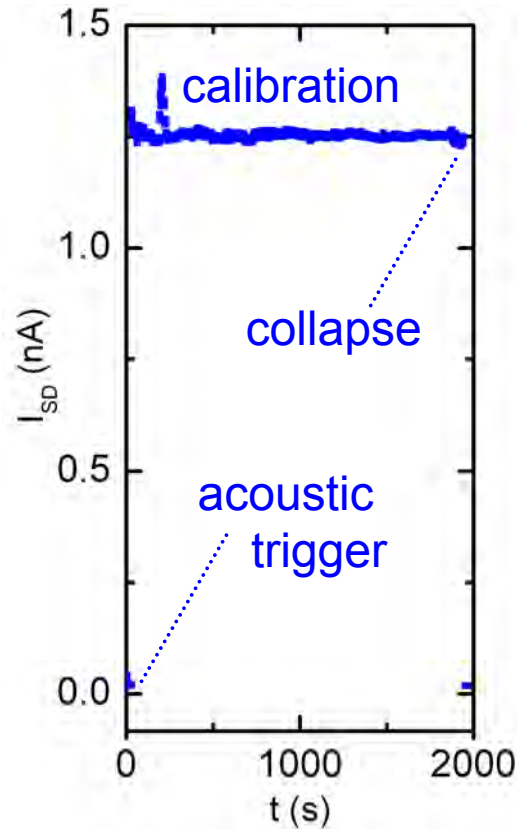
island:  
270 nm x 30 nm x 20 nm ÷ 250

resonator:  
14 μm x 130 nm x 110 nm  vs.

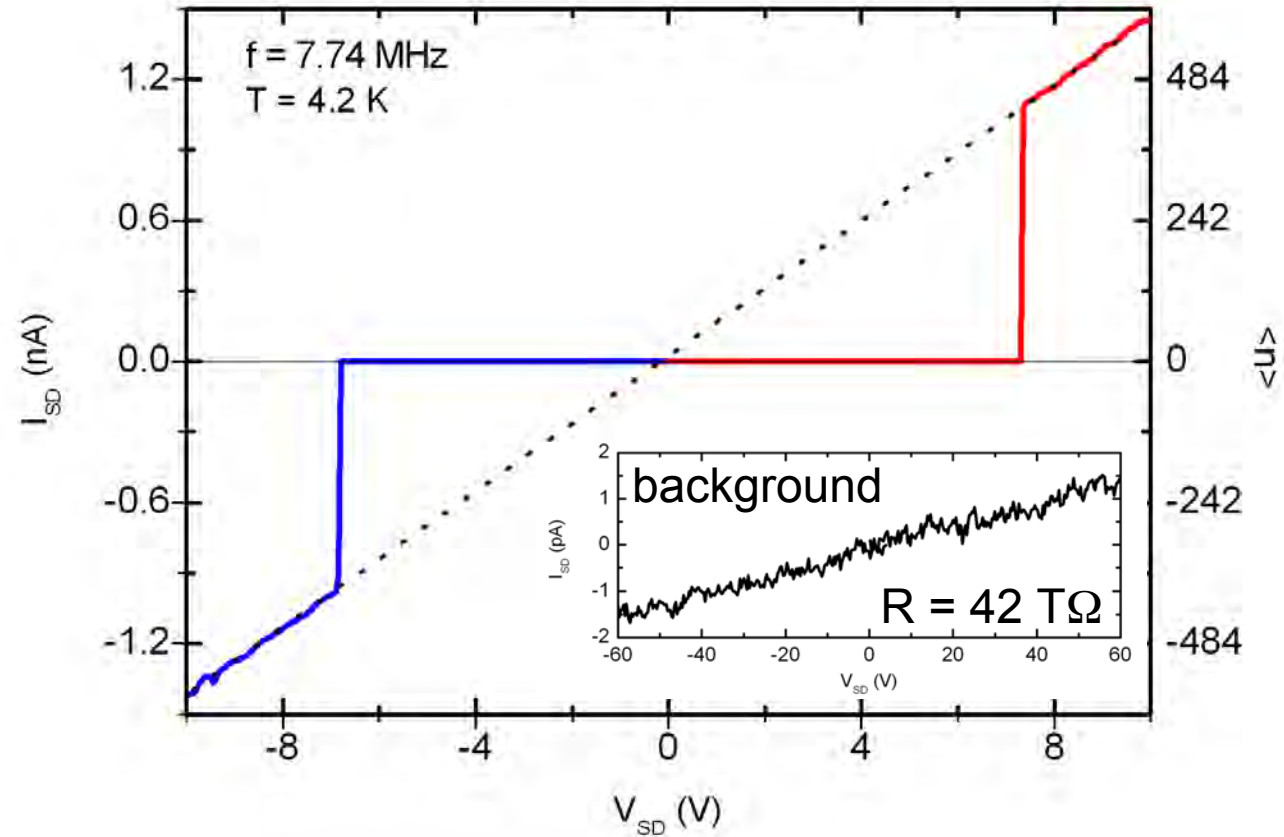


# Voltage-induced self-oscillation

Self-sustained shuttling for bias voltage exceeding shuttle dissipation threshold



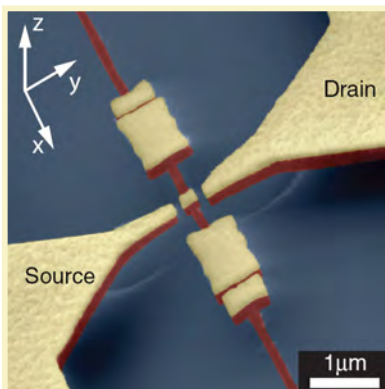
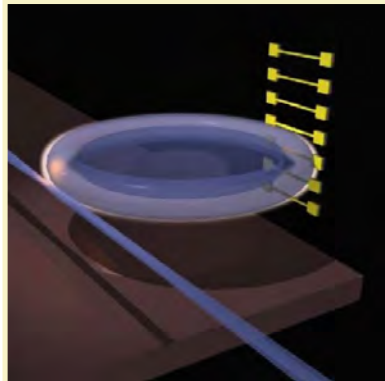
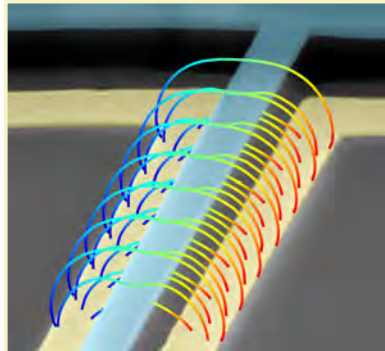
$$V_{SD} = 12 \text{ V}$$



- mechanically dissipated energy  $P_{\text{diss}} = 2\text{-}8 \text{ nW}$
- no field emission up to  $V_{DC} = 60 \text{ V}$
- operation at 4.2 K



# SUMMARY



## Transduction via dielectric gradient fields

- External yet local actuation of dielectric resonators
- Integrated optoelectronic detection
- Control of linear and non-linear dynamics
- High  $Q$  modes of dielectric resonators understood
- Progress towards an understanding of damping
- On route to scalable and efficient on-chip EMI

## Near-field cavity nano-optomechanics

- Platform extending dispersive cavity optomechanics to the nanoscale
- Dynamical back action on nanomechanical oscillators
- Imprecision of motion detection at 300K below SQL

## Nanomechanical charge shuttle

- Capacitance controlled electron shuttling demonstrated
- Self-oscillation observed
- Approaching Coulomb blockade regime

**Thank you,  
for your attention!**

