

Polariton Condensation

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Windsor 2010

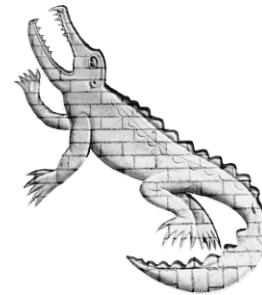
Collaborators

Theory

J. Keeling

P. B. Littlewood

F. M. Marchetti



Funding from



Engineering and Physical Sciences
Research Council

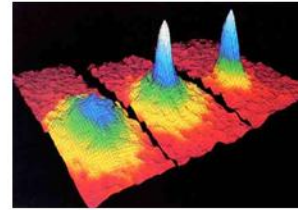
Macroscopic Quantum Coherence



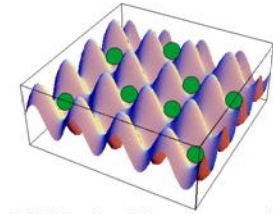
1924 BEC



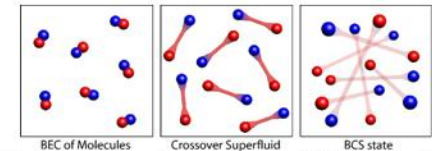
1957 BCS



1995 BEC in cold atoms



2002 Cold atoms in optical lattices



2004 Fermions and BCS-BEC



1910

1920

1930

1940

1950

1960

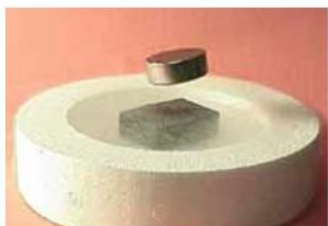
1970

1980

1990

2000

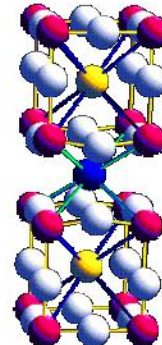
1911 Superconductivity



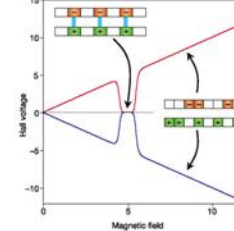
1938 Superfluid Helium



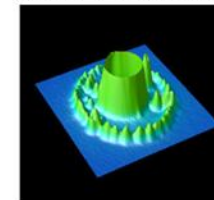
1986 High Tc



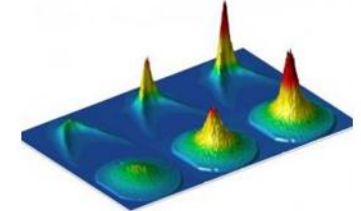
2004 QH Excitons



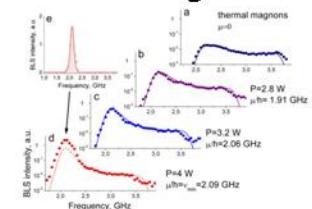
CQW Excitons ?



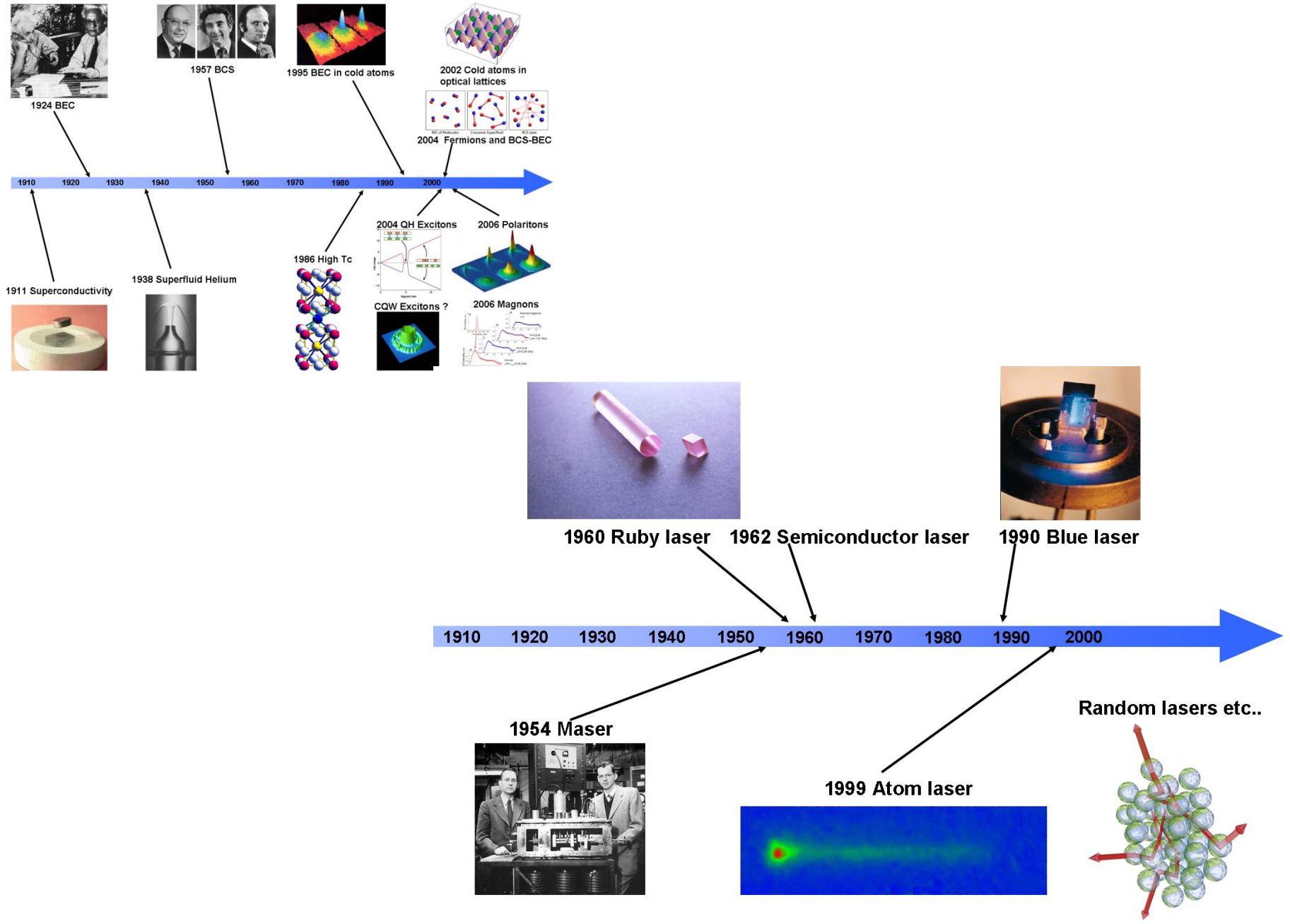
2006 Polaritons



2006 Magnons



Macroscopic Quantum Coherence



Outline

✓ Lecture 1:

Introduction: BEC-BCS, excitons, polaritons, experiments

✓ Lecture 2:

Part1: Quantum condensation in non-equilibrium
dissipative systems

- non-equilibrium field theory
- probes of dissipative BEC

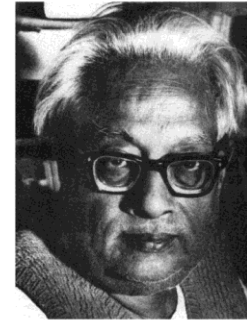
Part2: Superfluid properties

Bose-Einstein Condensation

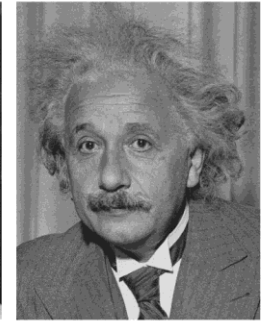
BEC = macroscopic occupation of a single quantum (ground) state of massive particles at thermal equilibrium

$$N = \int d\epsilon \frac{D(\epsilon)}{e^{\beta(\epsilon - \mu)} - 1}$$

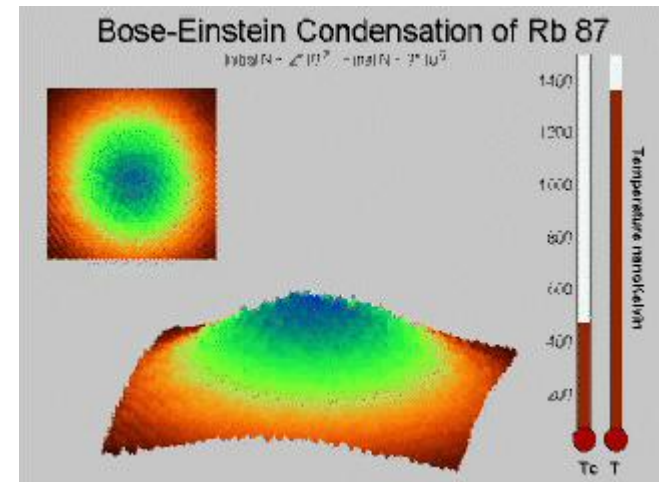
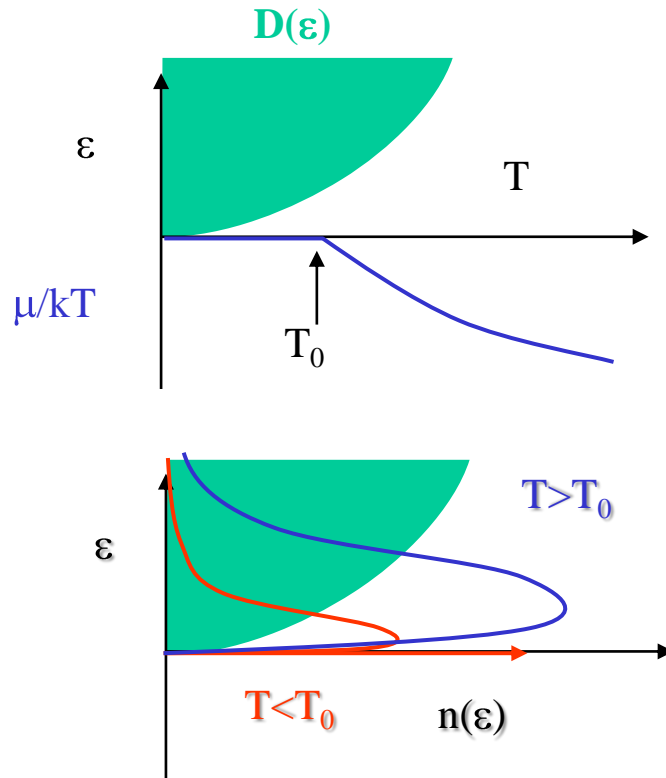
Bose-Einstein condensation * 1925



Satyendra Nath Bose



Albert Einstein

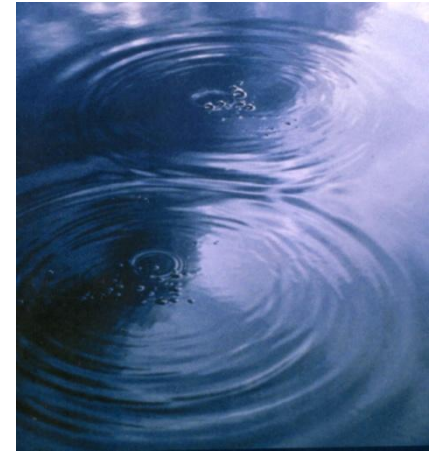


Bose-Einstein Condensation and Interactions

Macroscopic Phase Coherence

= macroscopic wave function
which arises from interactions

$$\psi e^{i\phi}$$



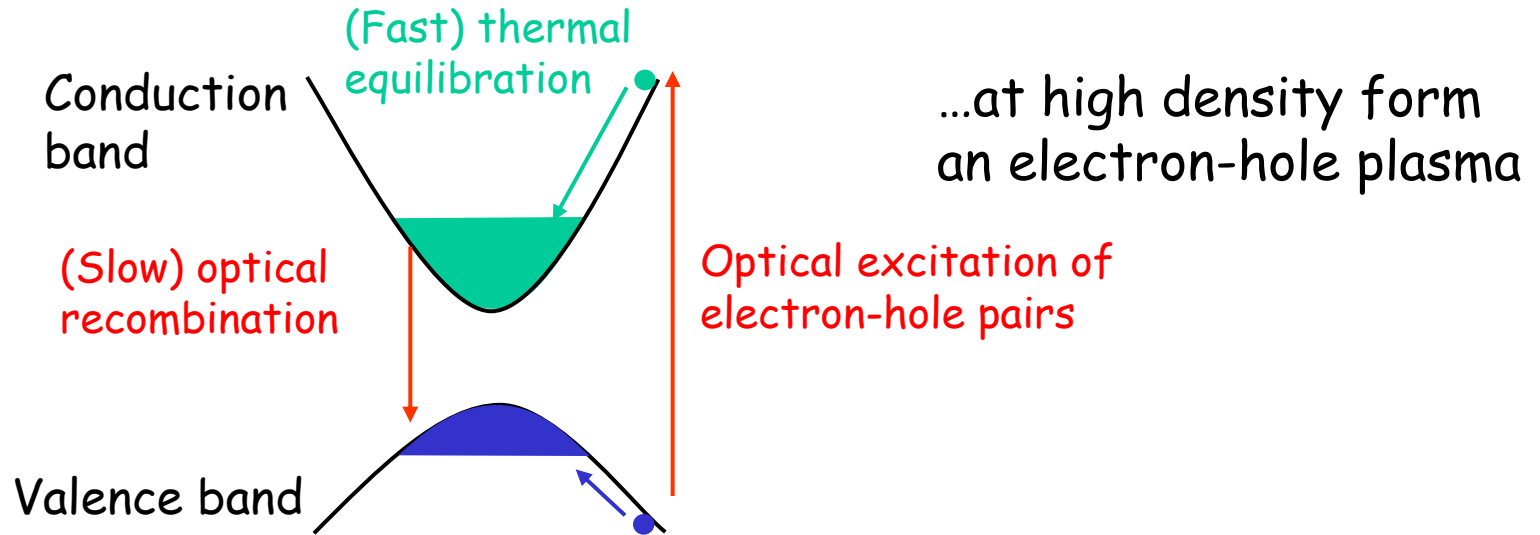
Superfluidity - linear sound mode with dispersion
and hence a superfluid stiffness c

$$\omega = cq$$



Excitons in Semiconductors

- ✓ Electron-hole pairs created by optical excitations ...



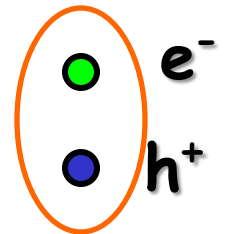
...at low densities can bind to form **excitons** (analogue of hydrogen)

- ✓ Binding is weak and radius is large

e.g. in GaAs ($m^* \sim 0.1 m_e$, $\epsilon = 13$)

Binding energy = 5 meV (13.6 eV for Hydrogen)

Bohr radius = 7 nm (0.05 nm for Hydrogen)



i.e. large compared to inter-atomic distances

Exciton Condensation

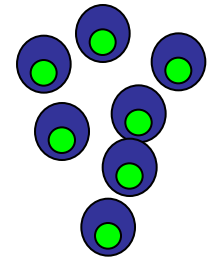
✓ At low densities ($n_{\text{exca}}^d \ll 1$) tightly bound excitons

- capacity to undergo **Bose-Einstein condensation**¹

Exciton mass is small, critical temperature

$$k_B T_C^{3D} \sim \frac{n_{\text{exc}}^{2/3} \hbar^2}{m_{\text{exc}}}$$

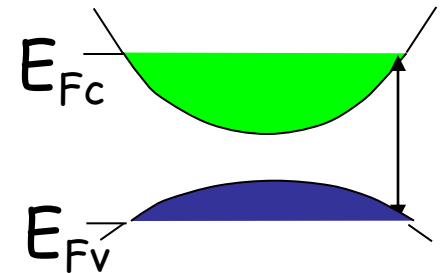
is large (ca. 1K at realistic densities)



BEC-like phase of excitons

✓ At high densities ($n_{\text{exca}}^d \sim 1$) electrons and holes unbind

- capacity to 'condense' into **excitonic insulator** phase² (two-component **BCS**)



BCS-like instability of Fermi surfaces

¹Keldysh and Kozlov '68

²Keldysh and Kopaev '64

BCS-BEC crossover

Keldysh and Kopayev '64
Eagles '69, Leggett '80

Same $|\Psi\rangle$ can describe BEC of bosons at low density \strong interaction and BCS state of fermions at high density \weak interactions.

$$|\Psi_{\text{BCS}}\rangle = \prod_k \left[u_k + v_k a_{k\uparrow}^\dagger a_{-k\downarrow}^\dagger \right] |\text{vac}\rangle \quad v_k/u_k = \phi_k$$

Pair wave-function

Why? It is a coherent state $|\Psi\rangle = e^{\sum_k \phi_k a_{k\uparrow}^\dagger a_{-k\downarrow}^\dagger} |\text{vac}\rangle$

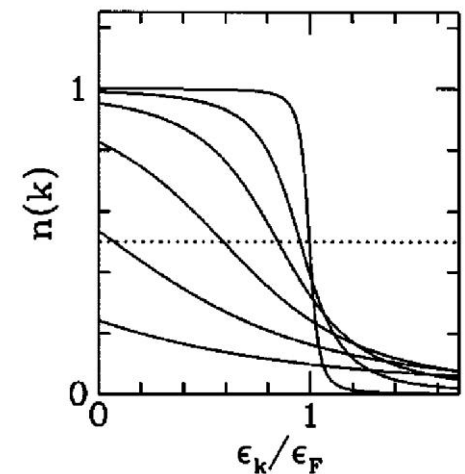
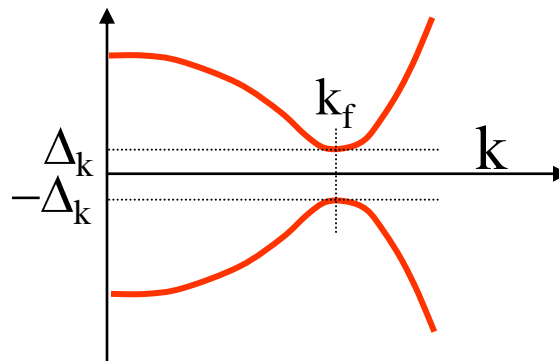
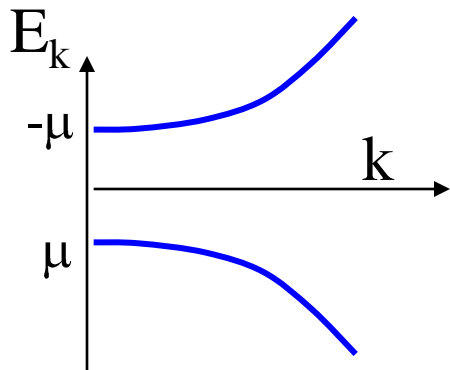
Gap equation

$$\Delta_k = \sum_{k'} \frac{1}{2E_{k'}} V_{kk'} \Delta_{k'}$$

Density equation

$$N = \sum_k \left(1 - \frac{\epsilon_k}{E_k} \right)$$

$$E_k = \sqrt{(\epsilon_k - \mu)^2 + |\Delta_k|^2} \quad E_{\text{min}} = \begin{cases} \sqrt{|\mu|^2 + |\Delta|^2}, & \mu < 0 \\ |\Delta|, & \mu > 0 \end{cases}$$

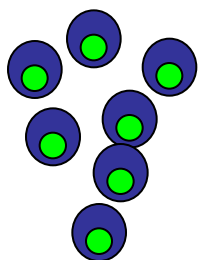


Randeria

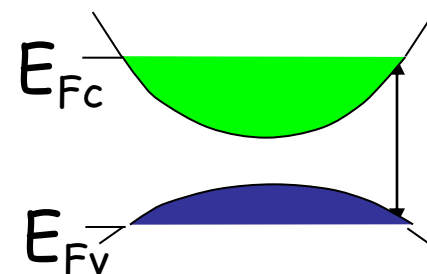
Mean-field Theory of Exciton Condensation

Keldysh and Kopayev '64

$$\hat{H} = \sum_k \epsilon_k (a_{Ck}^\dagger a_{Ck} - a_{Vk}^\dagger a_{Vk}) + \hat{V}_{\text{Coulomb}}$$



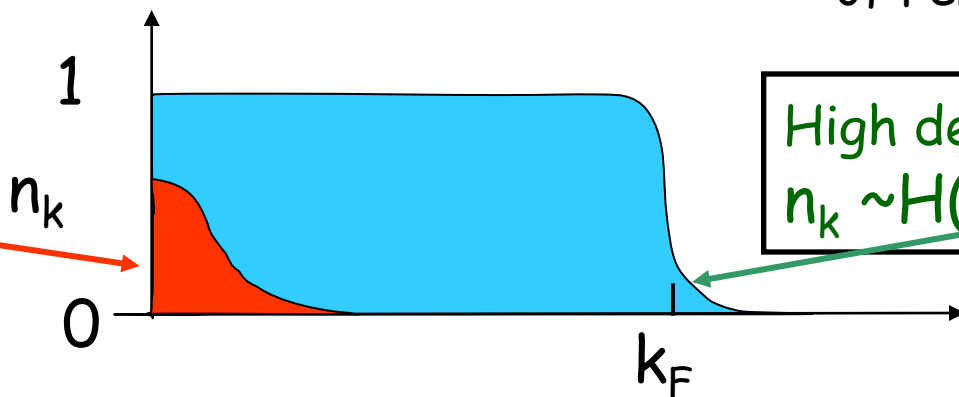
$$|\Psi\rangle = \prod_k [u_k + v_k a_{Ck}^\dagger a_{Vk}] |0\rangle$$



BEC-like phase
of excitons

BCS-like instability
of Fermi surfaces

Low density
 $n_k \sim n^{1/2} f_k$



High density
 $n_k \sim H(k_f - k)$

BCS-BEC crossover driven by change in excitonic density

Experiments towards BEC of Excitons

✓ Early attempts

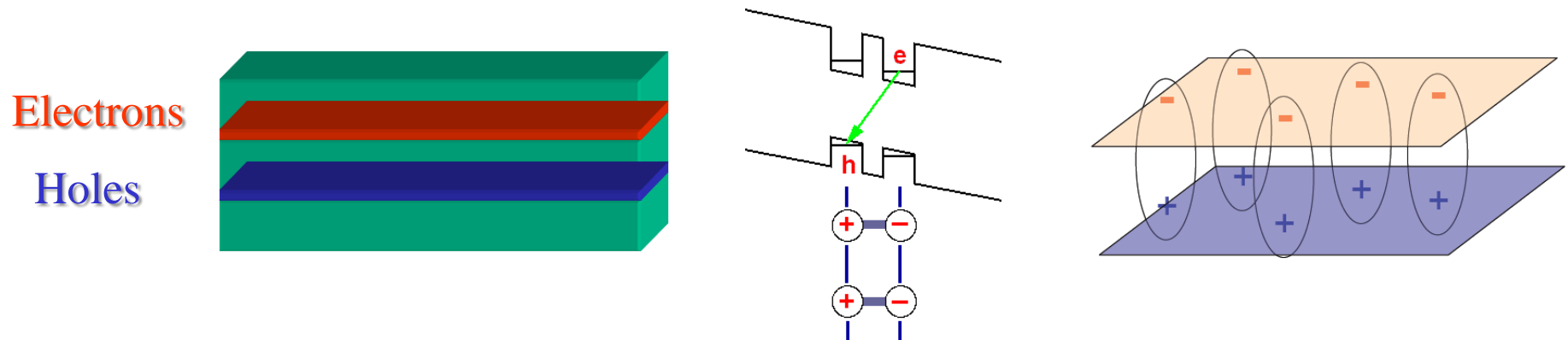
- Cu_2O dipole-forbidden excitons
- Biexcitons in CuCl

Obstacle: Auger recombination

✓ New promising candidates

- Indirect excitons in coupled quantum wells

Butov et al PRL (2001), Nature (2002), Snoke et al, Nature (2002);



- bias across QWs leads to **long-lived** spatially indirect excitons
- coherence of excitons would show in photoluminescence

Experiments towards BEC of Excitons

✓ Early attempts

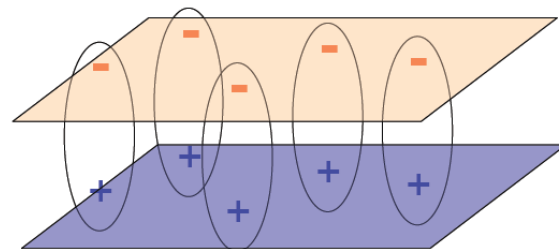
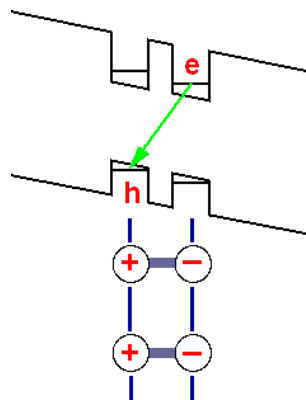
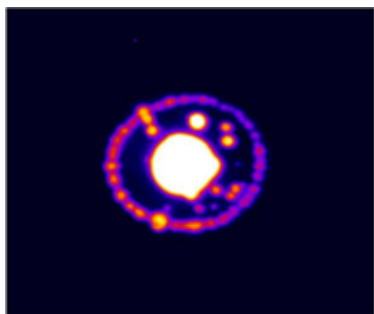
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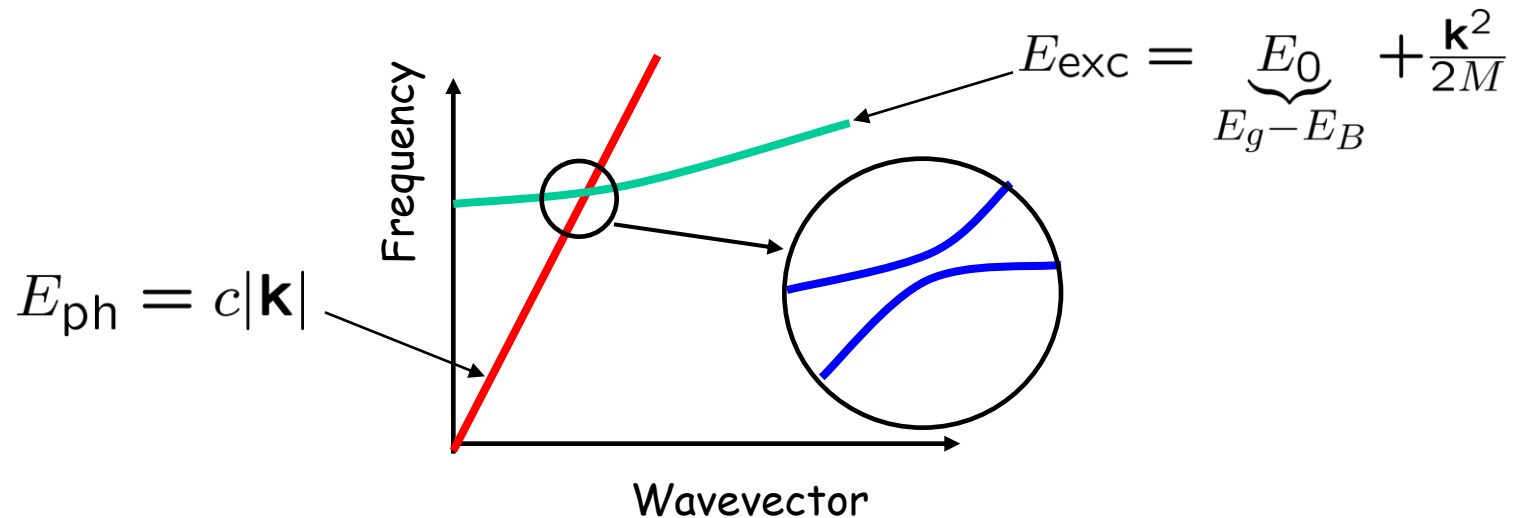
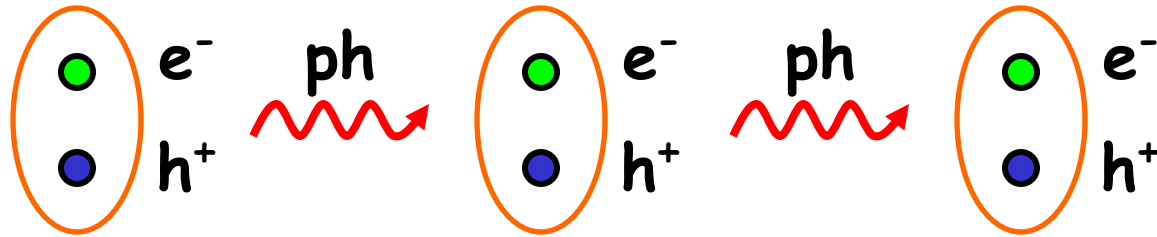


- bias across QWs leads to **long-lived** spatially indirect excitons
- coherence of excitons would show in photoluminescence
- fragmentation pattern observed requires **non-linear (stimulated) process**¹

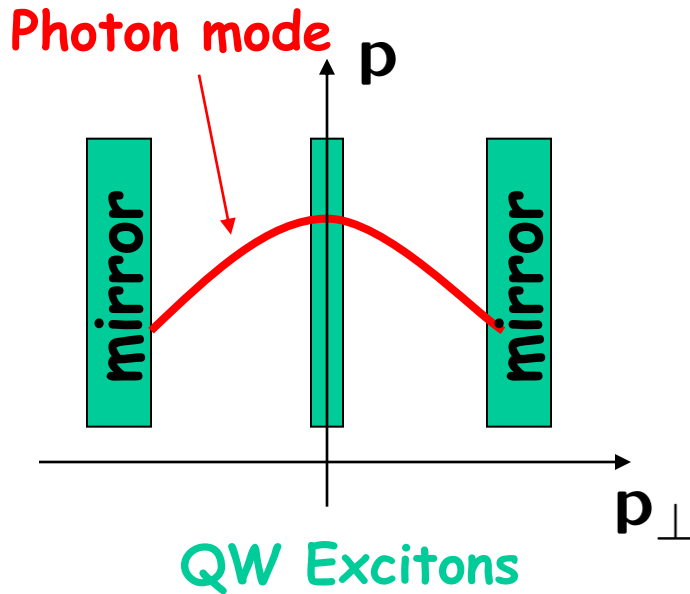
¹L. S. Levitov et al, Phys. Rev. Lett. **94**, 176404 (2005)

Polaritons

- ✓ Strong exciton-photon interaction - polariton
- ✓ Polaritons [J.J. Hopfield *Phys Rev* 112, 1555 (1958)]
= mixed modes of excitonic polarisation and light



Microcavity Polaritons



$$\begin{pmatrix} E_{\text{exc}} & g \\ g & E_{\text{ph}} \end{pmatrix}$$

dipole coupling

normal modes

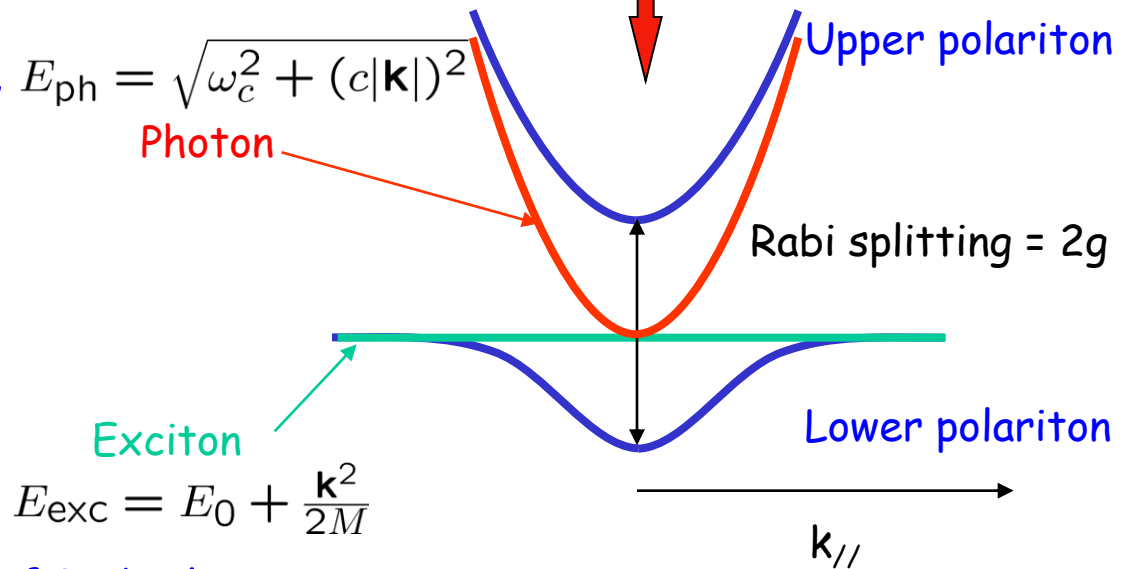
- ✓ Optical microcavities allow
 - to confine the optical modes
 - to control the interactions with the electronic polarisation

$$E_{\text{ph}} = \sqrt{\omega_c^2 + (c|\mathbf{k}|)^2}$$

Photon

Exciton

$$E_{\text{exc}} = E_0 + \frac{\mathbf{k}^2}{2M}$$

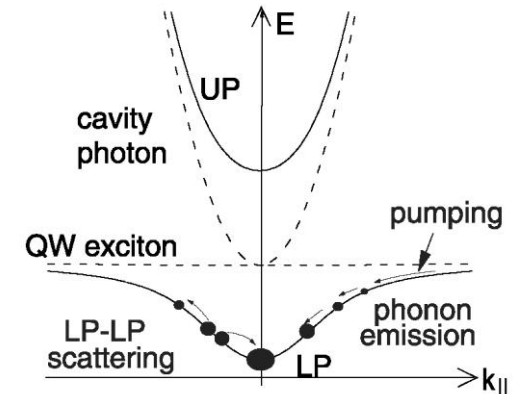
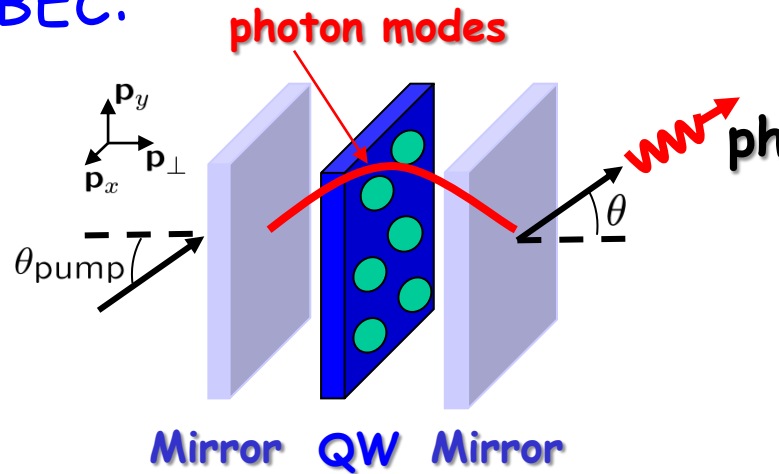


- ✓ Polariton mass = 10^{-9} mass of Rubidium atom

- ✓ Experimentally realised: C. Weisbuch et al. *PRL* **69**, 3314 (1992)

Early Experiments - towards BEC

✓ Towards BEC:



- Nonlinear growth of emission without bleaching of polariton line much below the population inversion **not a photon laser!**

Pau et al, *PRA* **54**, 1789 (1996); Dang et al. *PRL* **81**, 3920 (1998); Senellart et al, *PRL* **82**, 1233 (1999), Savvidis et al. *PRL* **84** 1547 (2000), Stevenson et al. *PRL* **85** 3680 (2000)

- Decrease of the second order coherence function $g^{(2)}$ **coherence?**

- Narrowing of the $N(\theta)$ photon distribution **spatial coherence?**

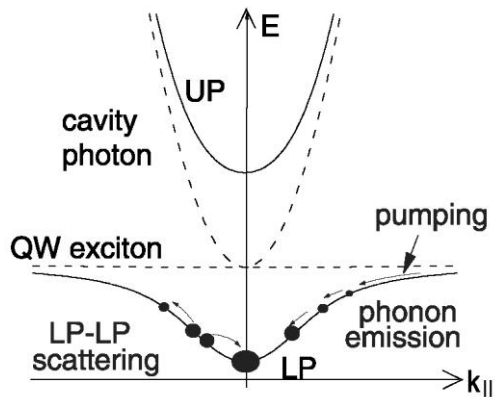
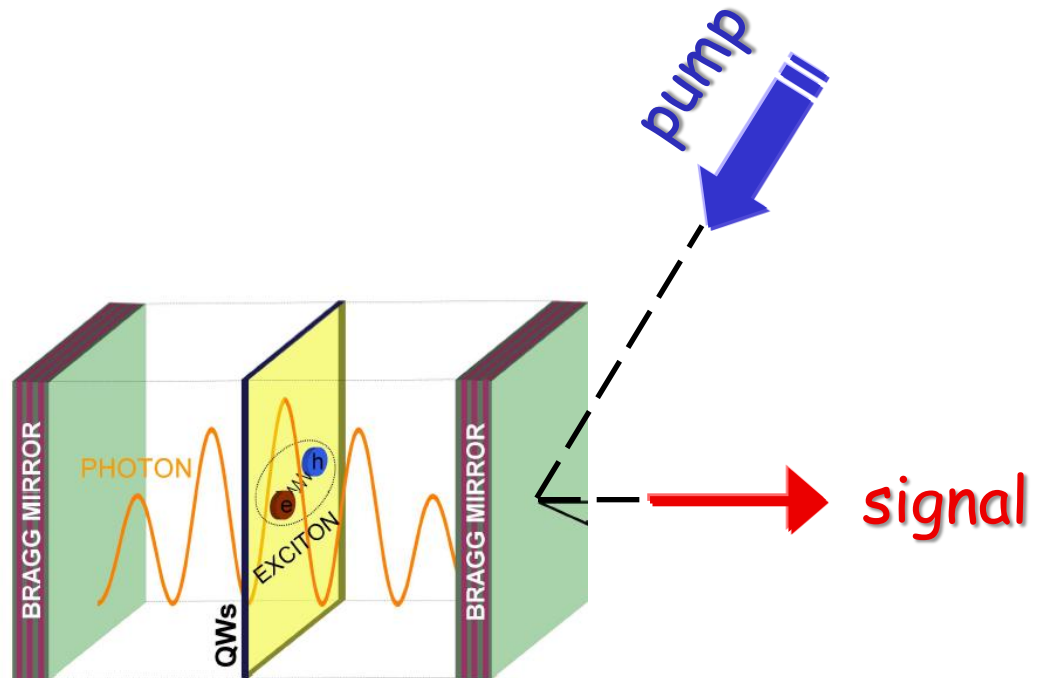
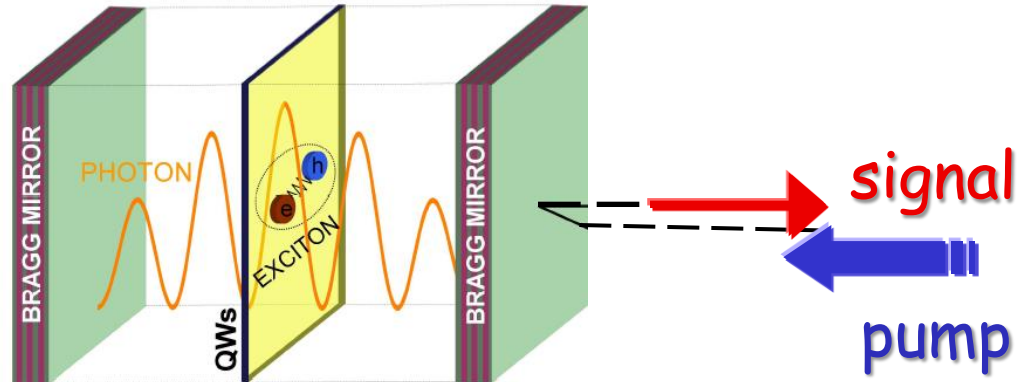
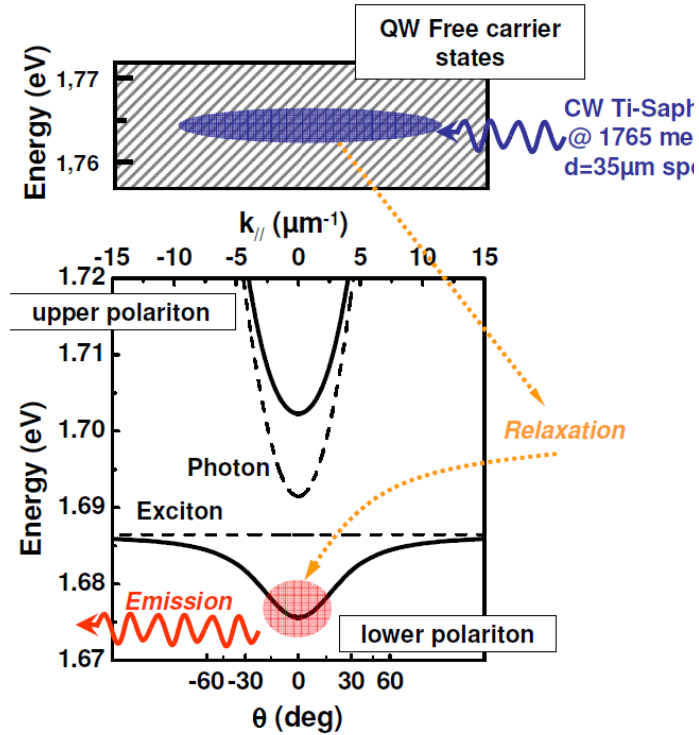
Deng et al. *Science* **298** 199 (2002), *PNAS* **100** 15318 (2003)

- Interference fringes

Richard et al. *Phys. Rev. Lett.* **94**, 187401 (2005)

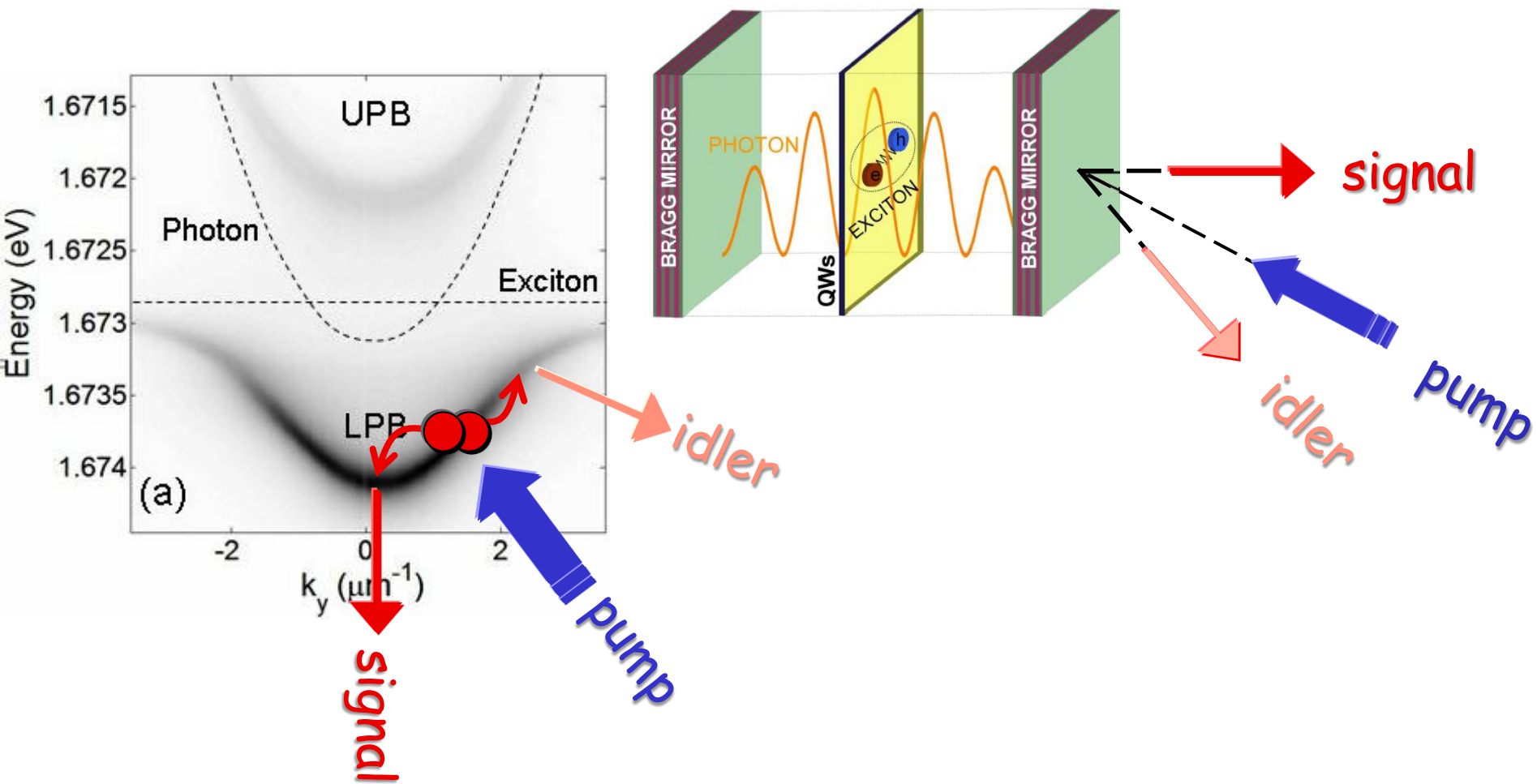
Different Pumping Schemes

Incoherent



Different Pumping Schemes

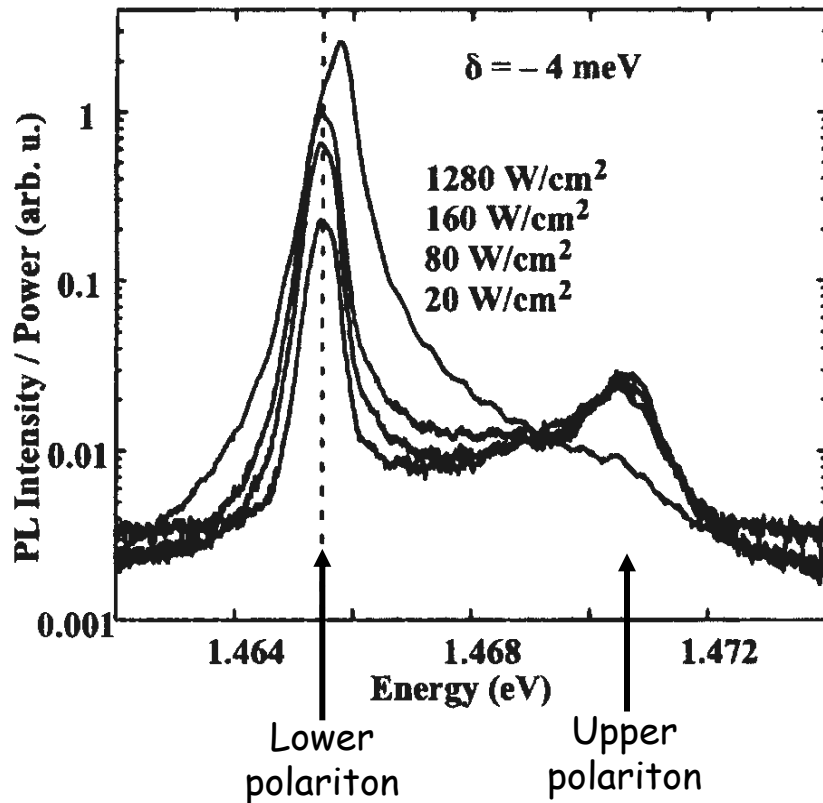
Parametric



Bosonic Stimulation

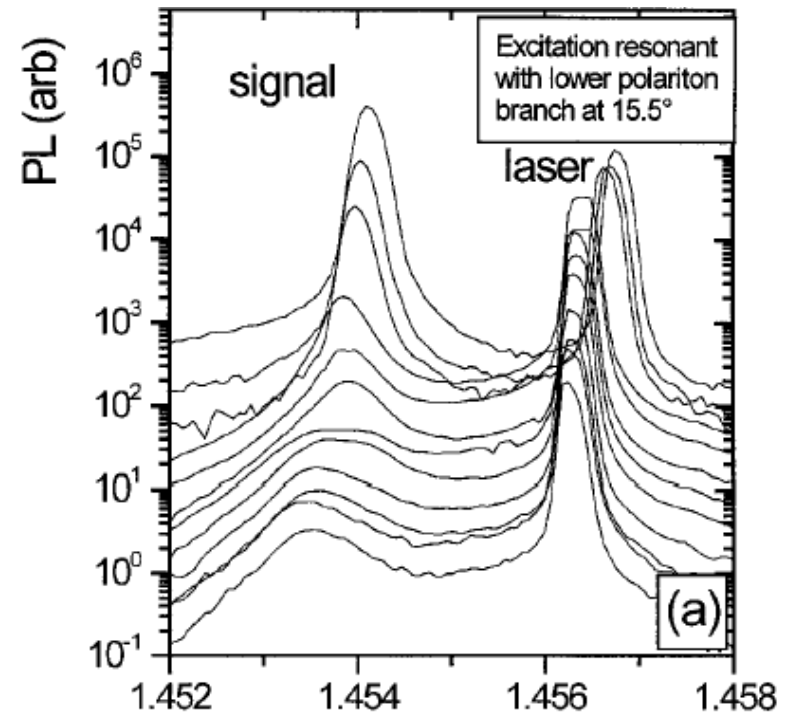
Incoherent

PL normalised to pump intensity



Senellart & Bloch, PRL 82, 1233 (1999)

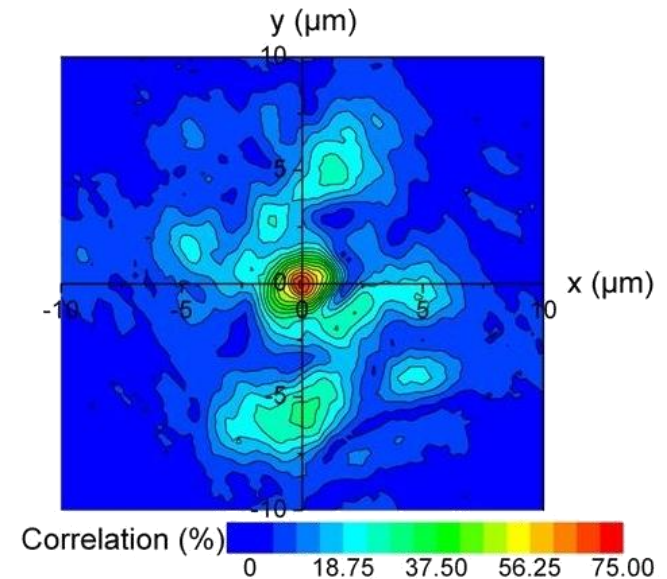
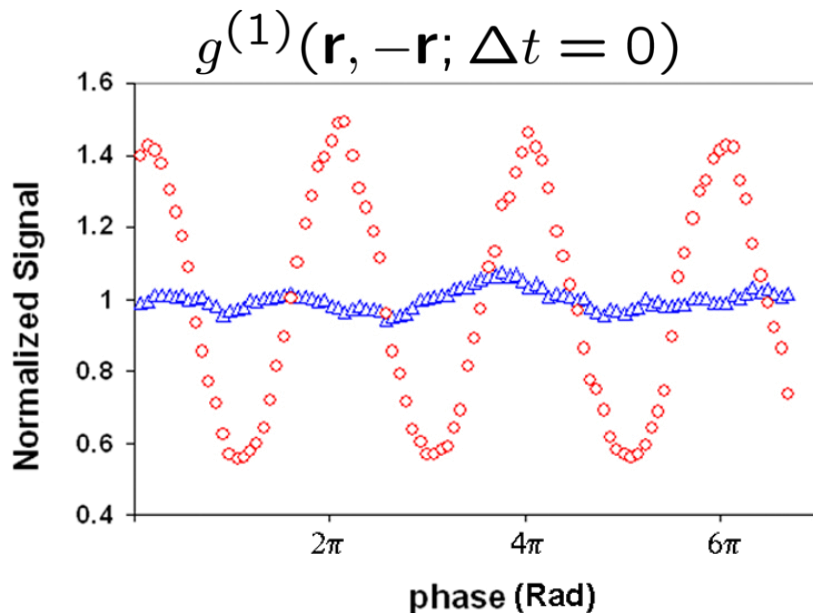
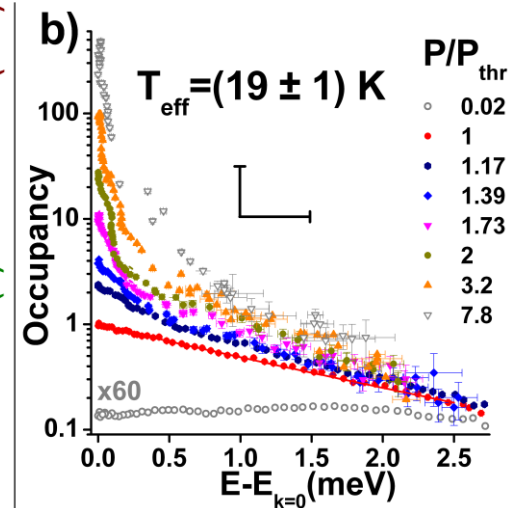
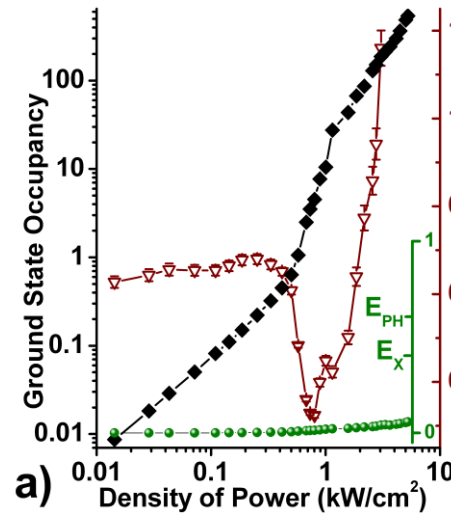
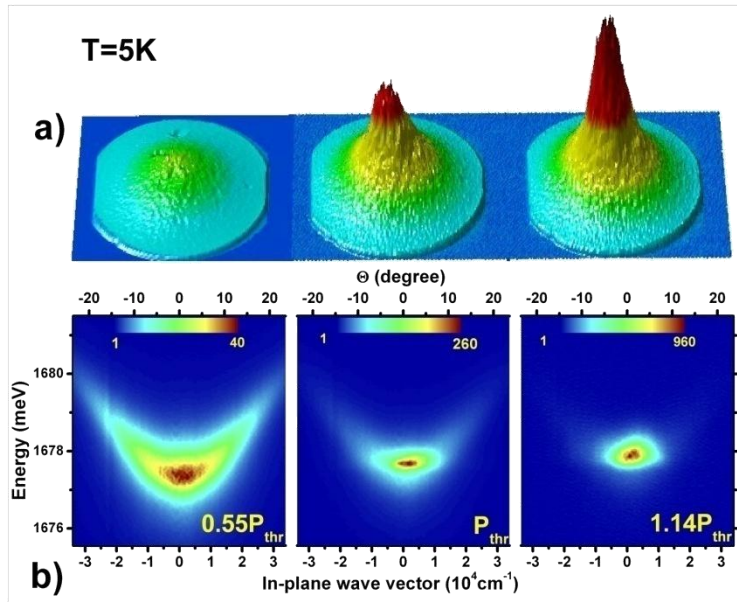
Parametric



Stevenson *et al.* PRL 85 3680 (2000)

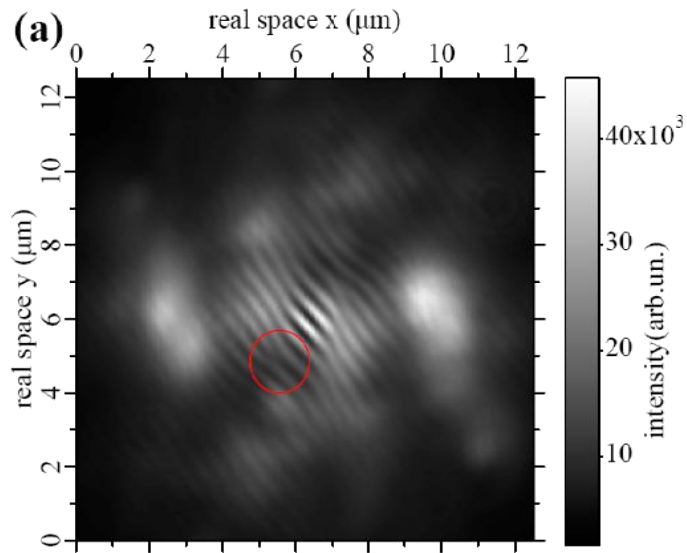
Evidences of Condensation in CdTe

Kasprzak et al., *Nature* **443**, 409 (2006)

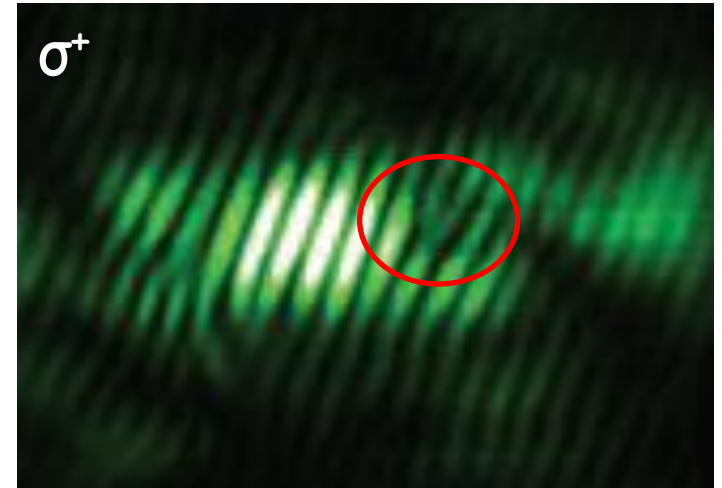


State of the Art

Vortices and half vortices

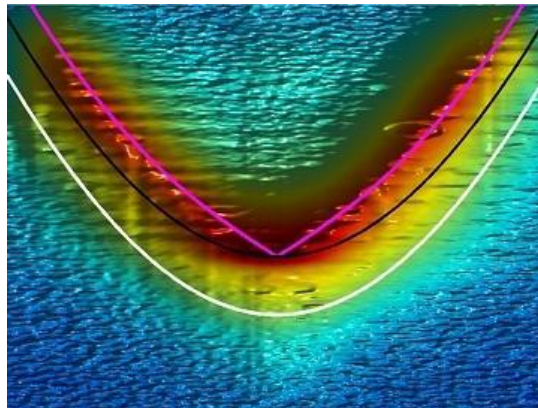


K. G. Lagoudakis et al, Nature Physics (2008)



Science 326, 974 (2009)

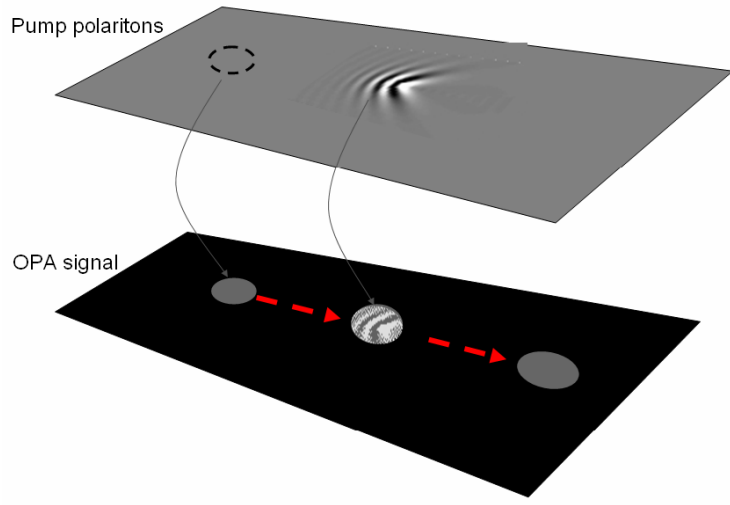
Bogoliubov Excitation Spectrum



S. Utsunomiya et al, Nature Physics (2008)

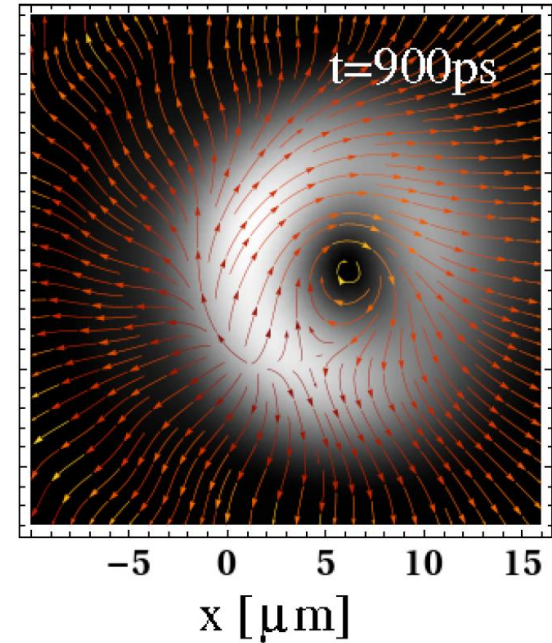
State of the Art

Flow via obstacle



Amo, Sanvitto, et al, *Nature* 2009

Persistent Quantised Currents



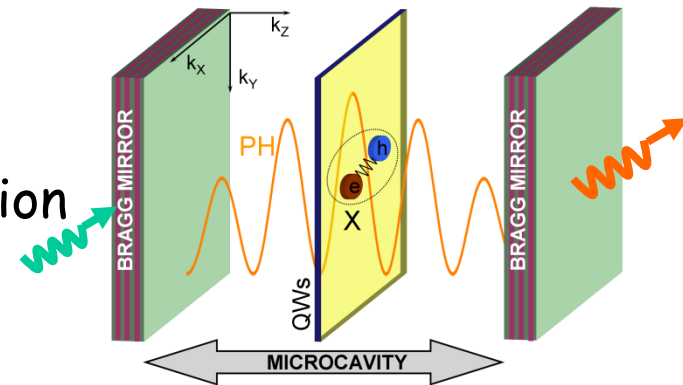
[Sanvitto, Marchetti, Szymanska *et al.*,
Nat. Phys. 2010 arxiv/0907.2371]

GaN Polariton Lasing - room temperature effects

S. Christopoulos et al, *PRL* **98**, 126405 (2007)

Polaritons' Special Features

- ✓ 2D system but ... finite size
- ✓ Internal polariton structure and strong interactions
 - photonic component make polaritons easily overlap
- ✓ Phase diagram - what is the most important?
 - Kosterlitz-Thouless - interactions dominated?
 - "finite size" BEC - confinement dominated?
 - something else?
- ✓ Continues pump and decay
 - non-equilibrium steady-state condensation
- ✓ Excitonic and Photonic disorder



The Phase Diagram

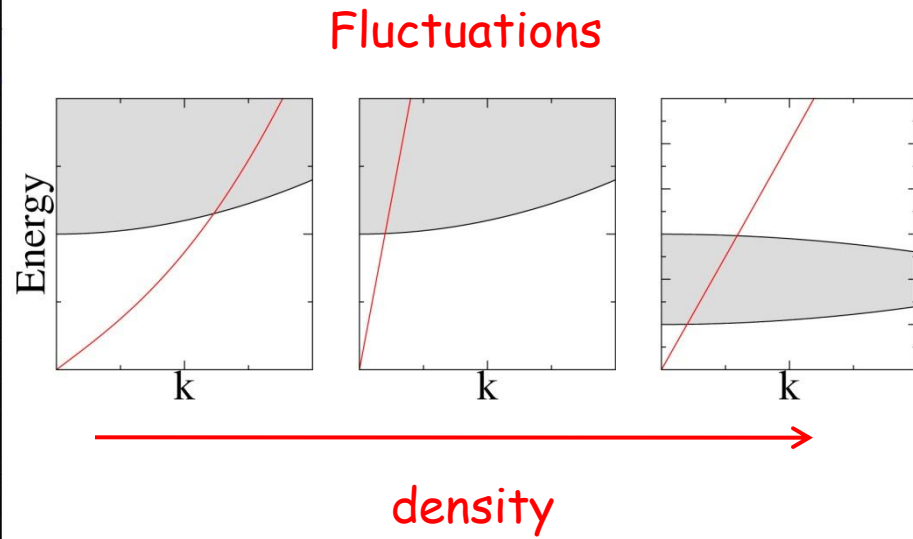
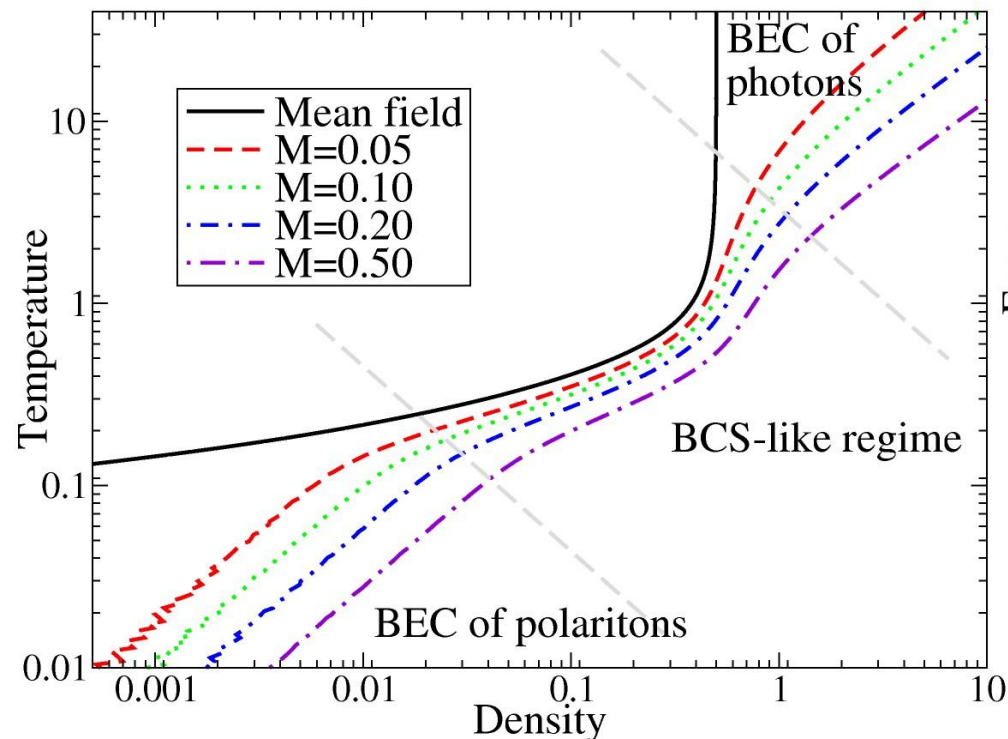
✓ Mean-field

$$|\Psi\rangle = e^{\lambda(\psi_0^\dagger + \sum_{\alpha} X_{\alpha} b_{\alpha}^\dagger a_{\alpha})} \prod_{\alpha} a_{\alpha}^\dagger |0\rangle = e^{\lambda\psi_0^\dagger} \prod_{\alpha} (v_{\alpha} b_{\alpha}^\dagger + u_{\alpha} a_{\alpha}^\dagger) |0\rangle$$

Two coupled order parameters

{ Coherent photon field $\langle\psi\rangle$
 Exciton condensate $\sum_{\alpha} \langle a_{\alpha}^\dagger b_{\alpha}\rangle$

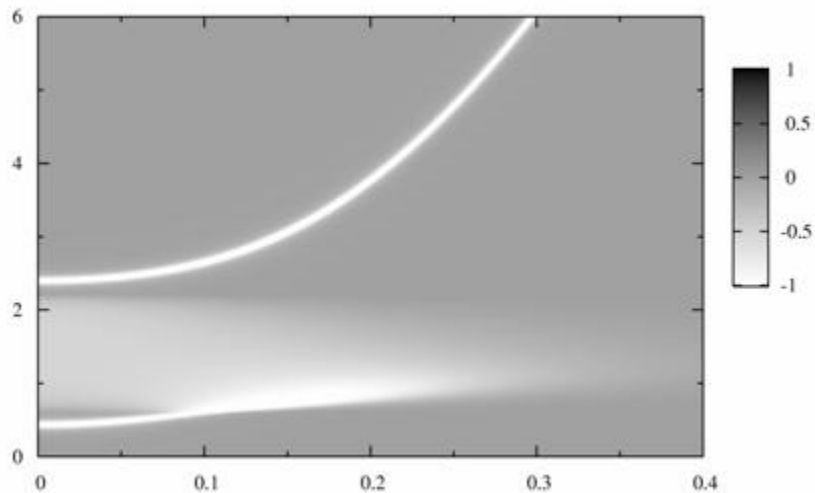
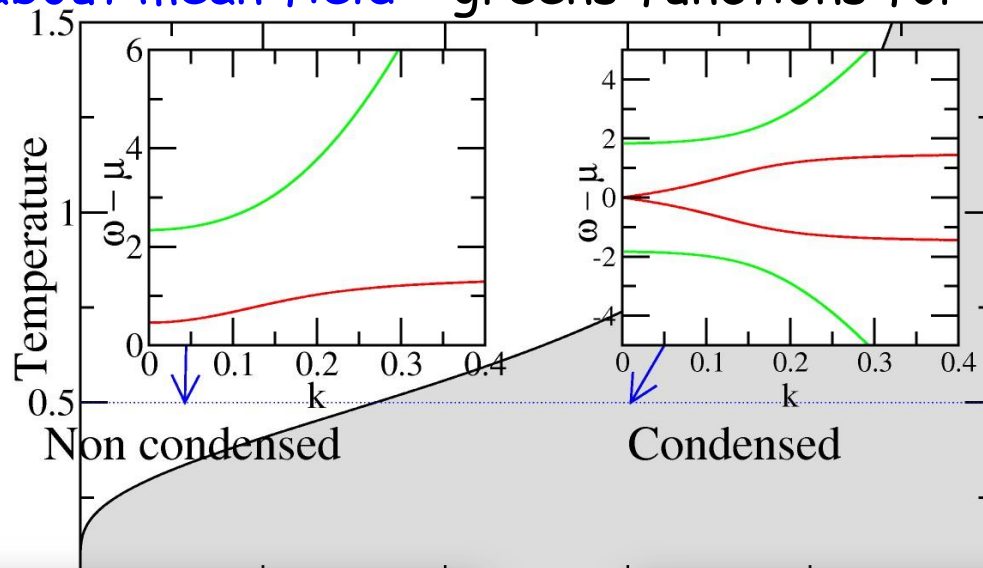
✓ Mean-field + fluctuations : **BEC-BCS-BEC** crossover with changing density



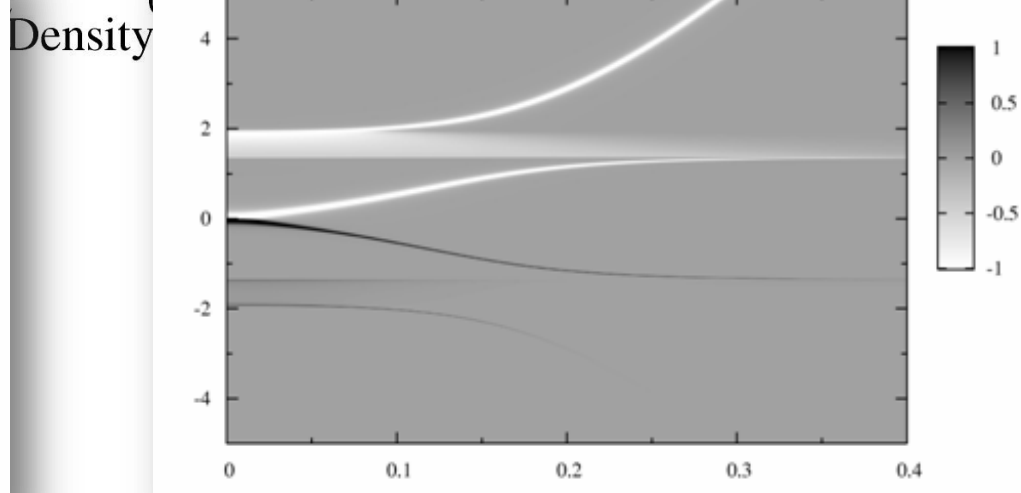
Fluctuation Spectrum and Collective Modes

Keeling et al. *Phys. Rev. Lett.* **93**, 226403 (2004)

Fluctuations about mean field - greens functions for photon response

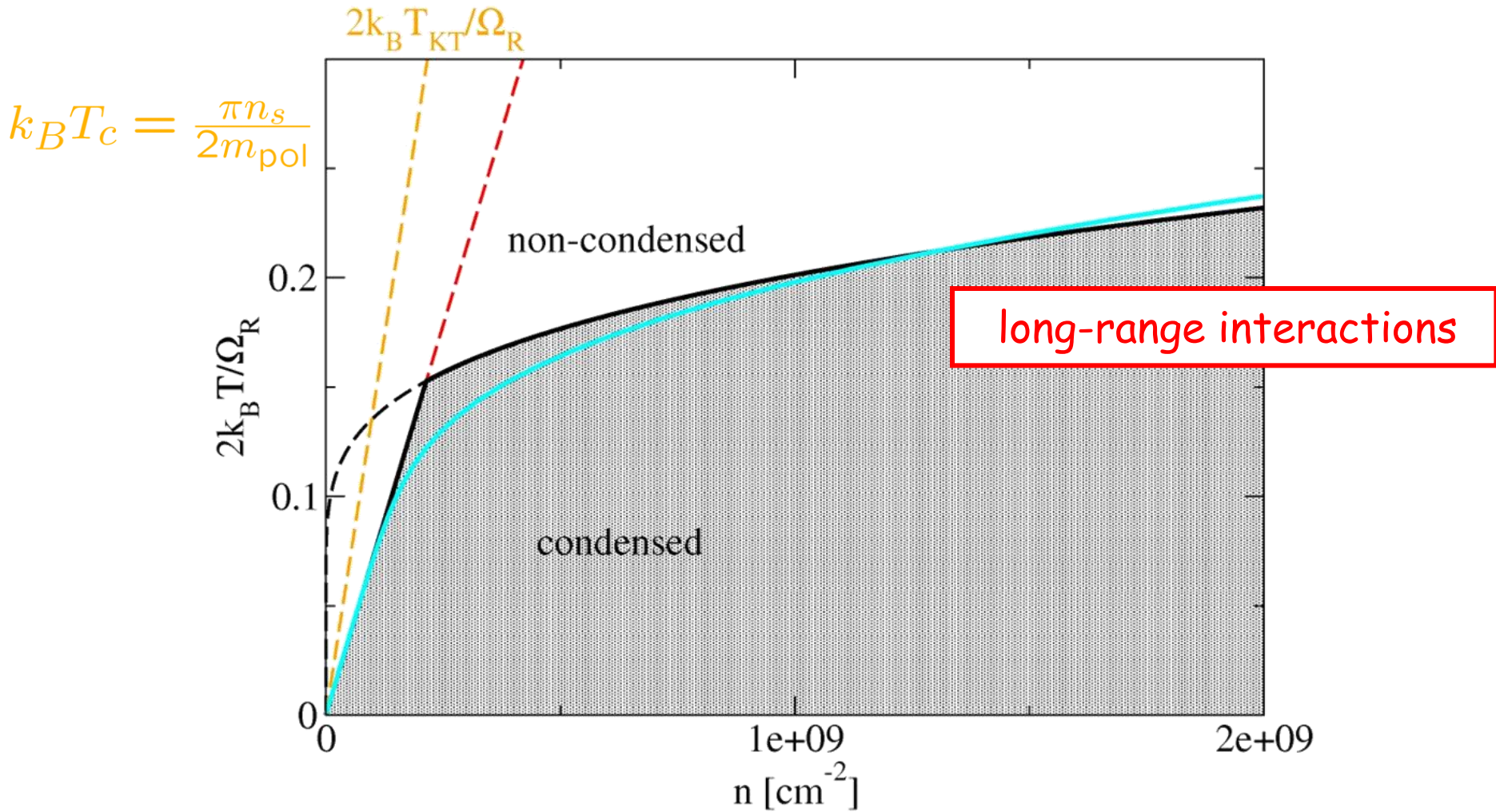


Uncondensed Spectra: polariton dispersion



Condensed Spectra: phase and amplitude modes

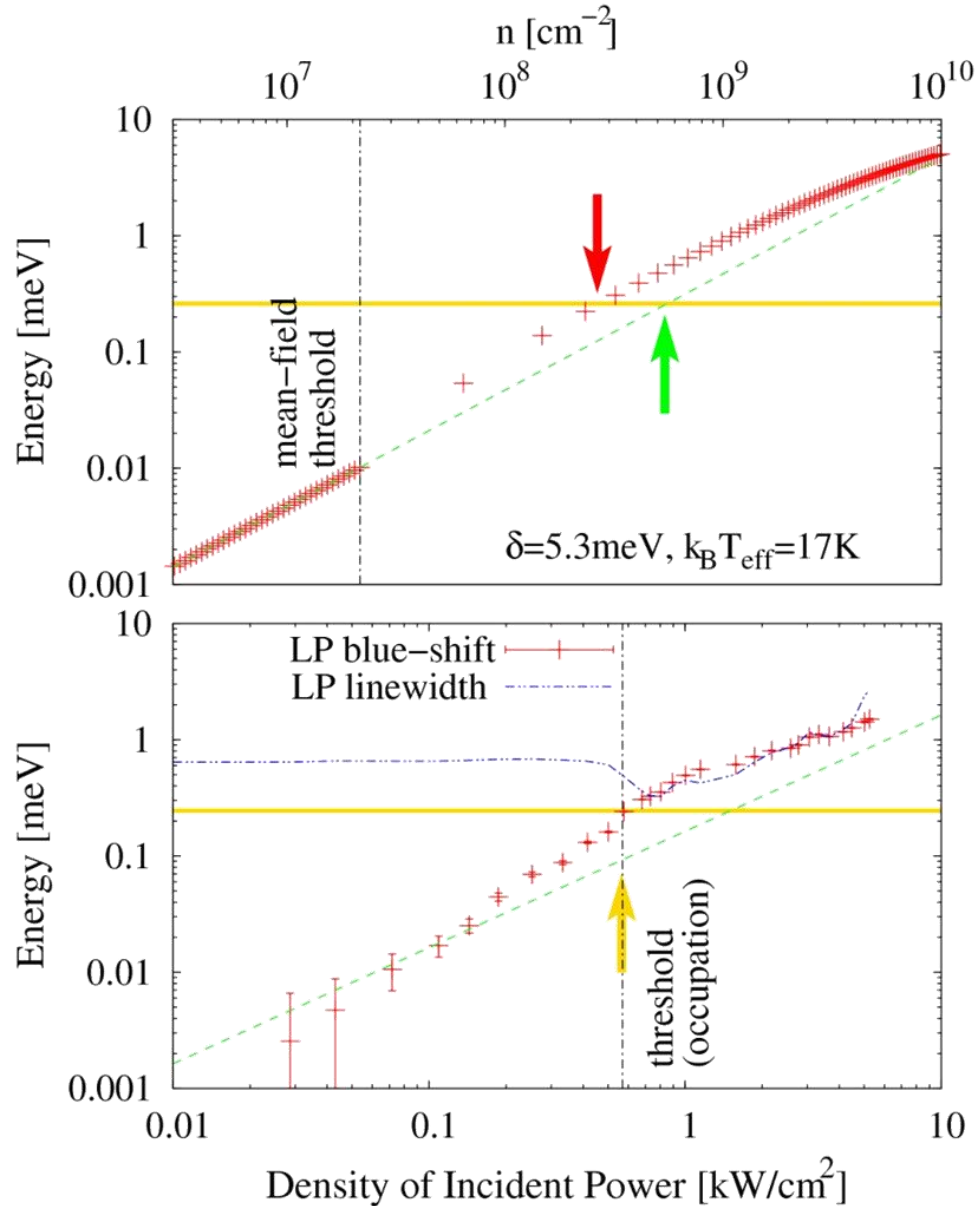
Beyond mean field: Interaction driven or dilute gas?



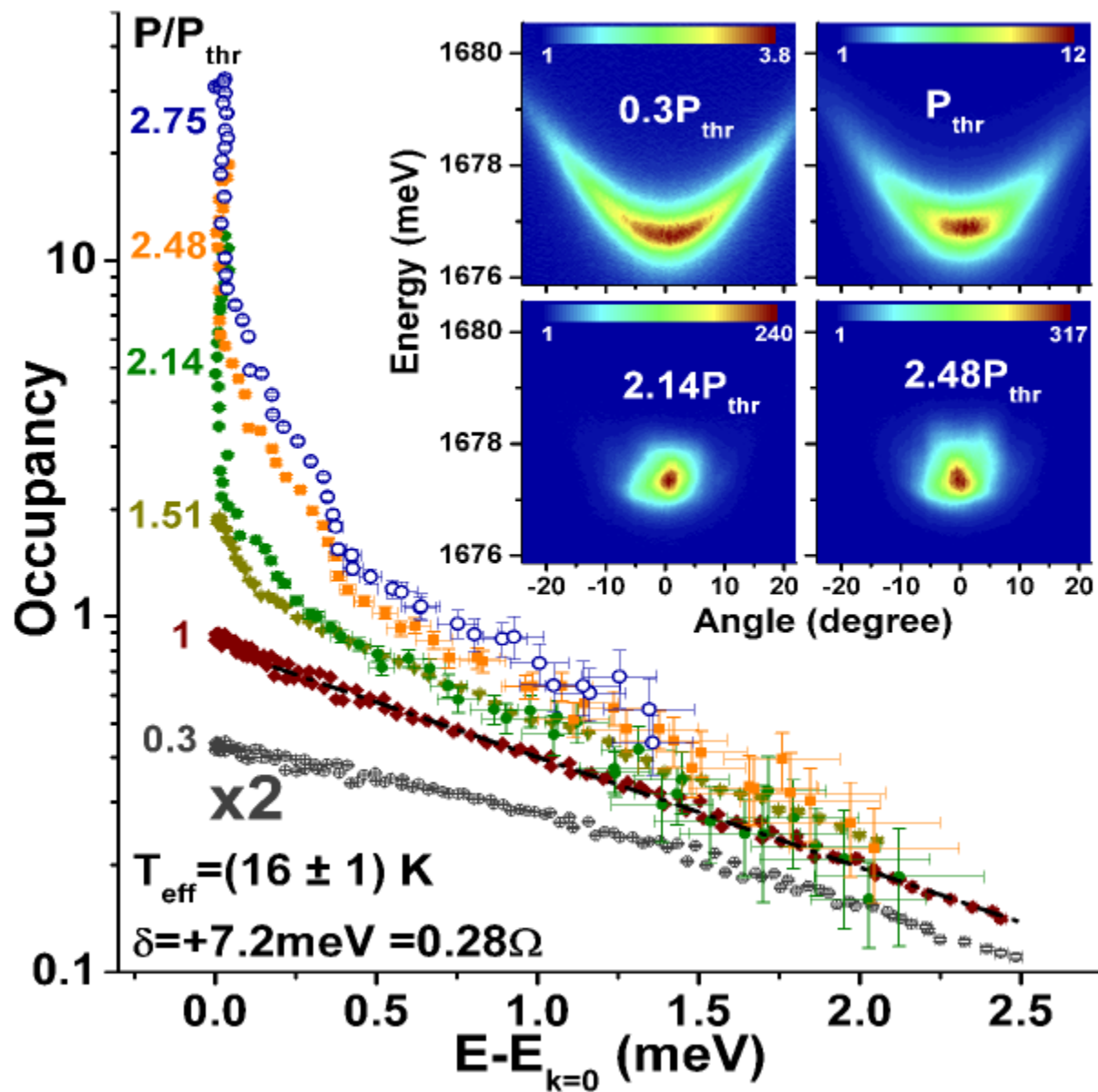
When $k_B T_c \sim \Omega_R$, deviations from BEC of structureless polaritons

J. Keeling et al, *PRL* **93**, 226403 (2004)
F.M. Marchetti et al, *PRL* **96**, 066405 (2006)

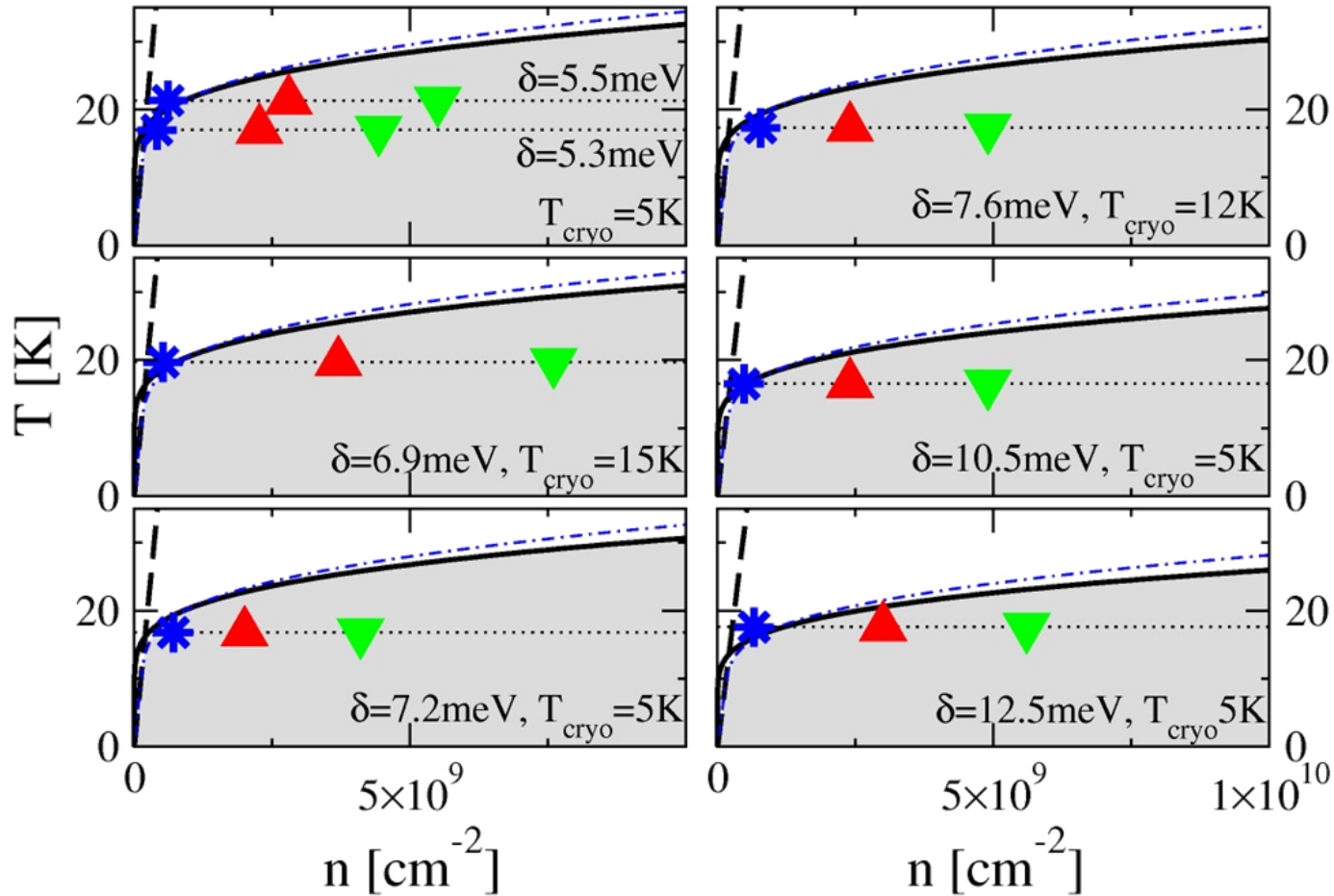
How to Estimate Density?



How to Estimate Temperature?



Data on the Phase Diagram



F.M. Marchetti et al, *Phys. Rev. B* **77**, 235313 (2008)

✓ Experiments on CdTe in the crossover between a fluctuation dominated WIBG and a mean-field-like collective state.

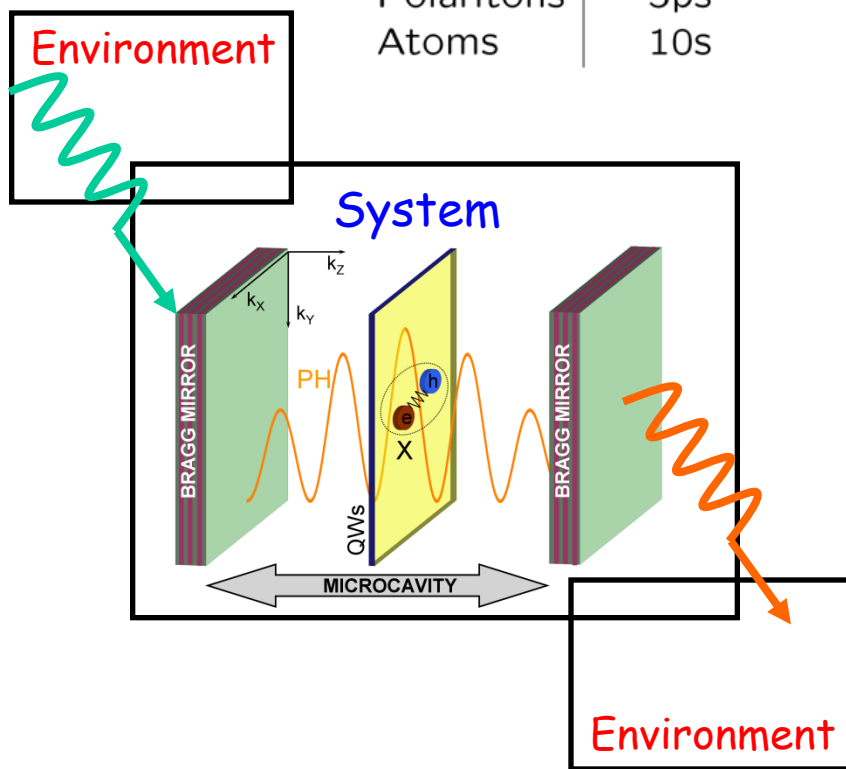
✓ Not easy to move away from this regime:

T polaritons different from T lattice

Condensation in Dissipative Systems

✓ Open systems in contact with environment

	Lifetime	Thermalisation	Linewidth	Temperature
Polaritons	5ps	0.5ps	0.5meV	20K
Atoms	10s	1ms	2.5×10^{-13} meV	10^{-8} K



Concepts: BEC in novel conditions, robustness to dephasing